

The Power of Isolation



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Safety-critical Real-time Systems





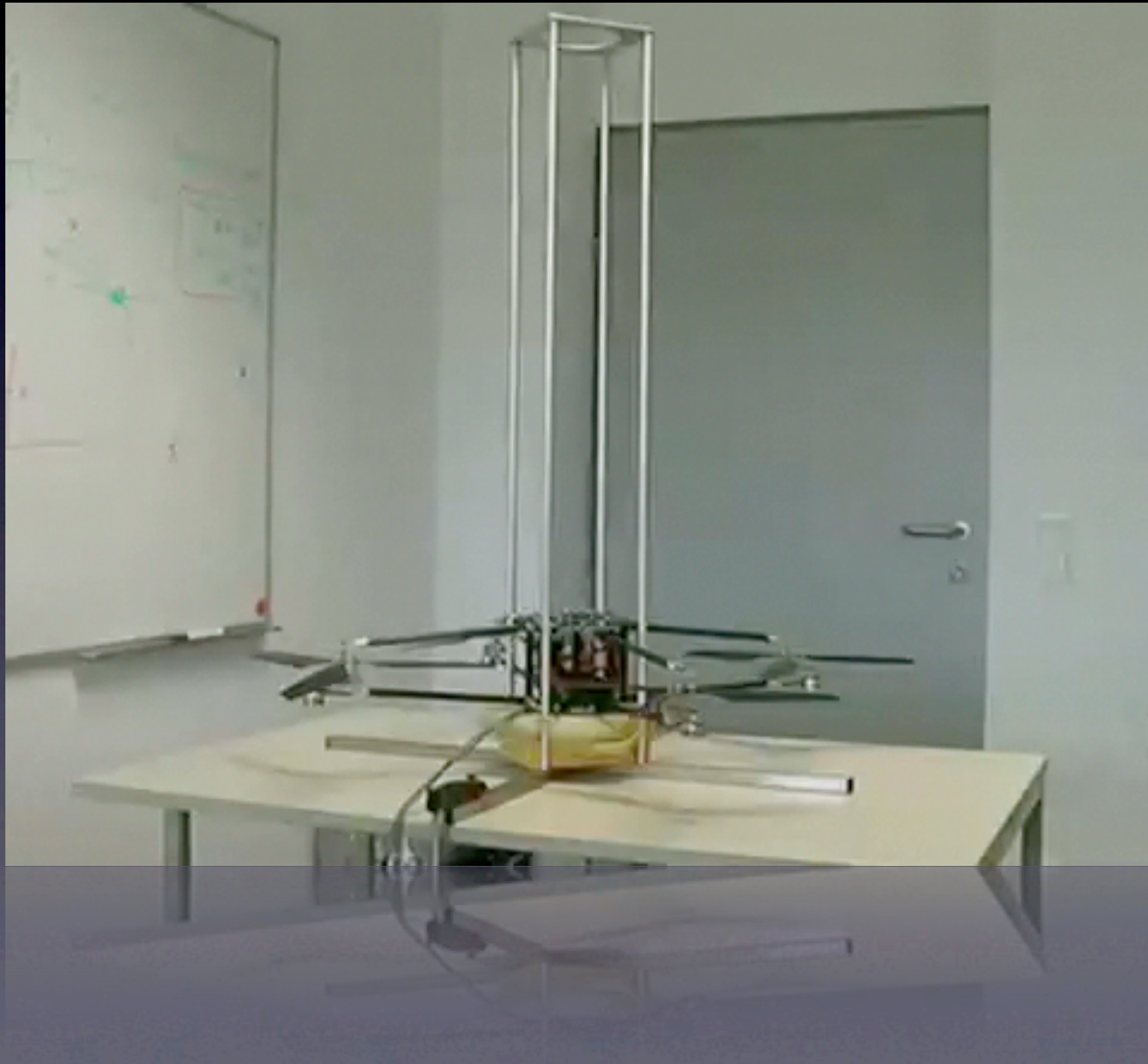
Safety-critical Real-time Systems



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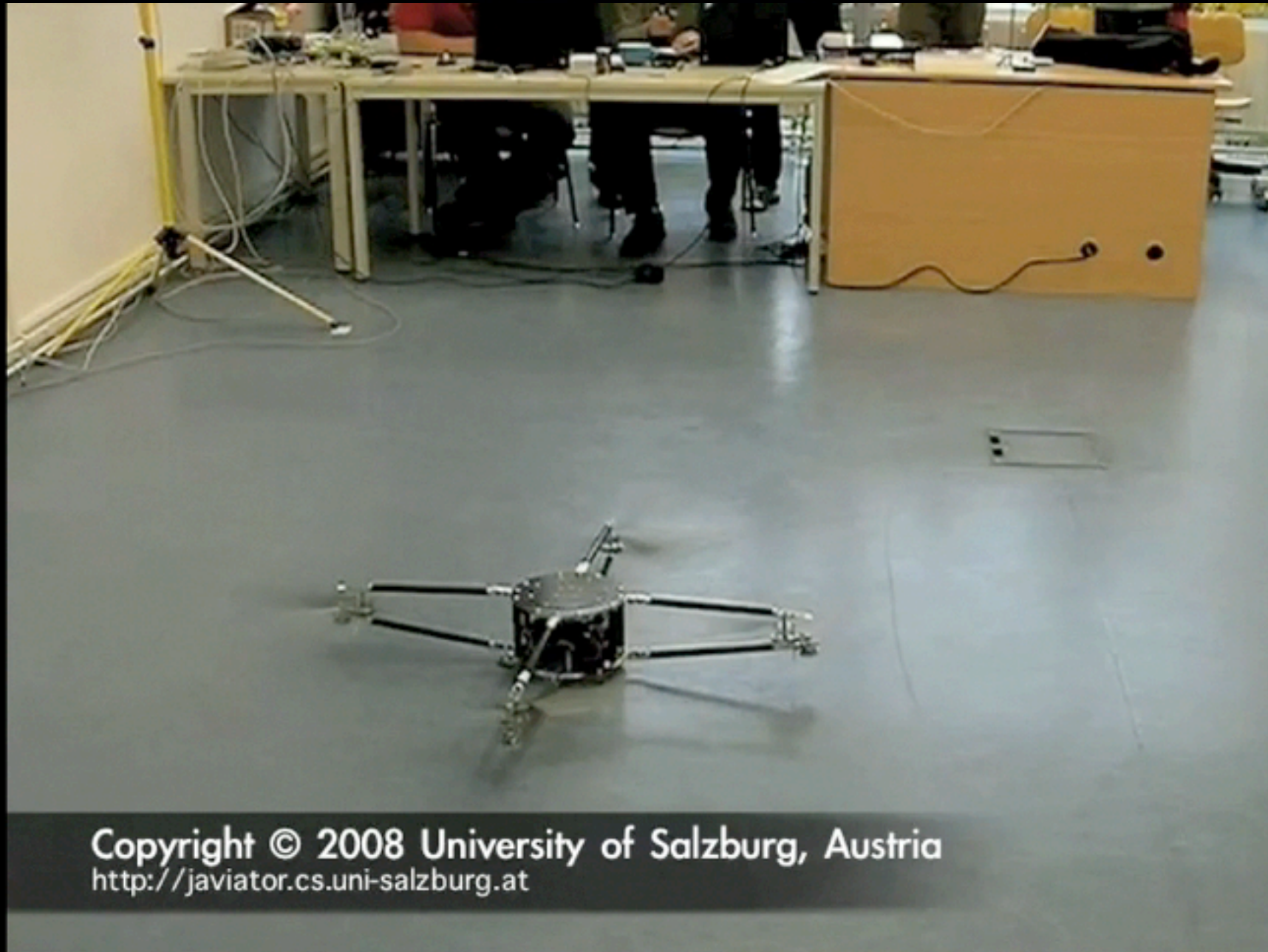


When things go wrong





When things go right...



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Isolation



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Important aspects for isolation: **time** **space**



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Temporal isolation through CBS [Abeni04], VBS [Craciunas12]



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Spatial isolation through memory management/hardware



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Power isolation?



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Power isolation?

Is power consumption compositional?



Isolation

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Temporal isolation through CBS [Abeni04], VBS [Craciunas12]

Spatial isolation through memory management/hardware

Power isolation?

Is power consumption compositional?

Problem: non-linear relationship of power consumption and processor frequency



Power-aware Real-time Systems



Power-aware Real-time Systems

Adapt system performance to system load



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Adapt system performance to system load

Dynamic Voltage and Frequency Scaling [Pillai01]



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$$p(f) = c_0 + c_1 f^\alpha \quad [\text{Mosse05}]$$



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- Scaling the frequency results in modified execution time
- Deadlines remain the same
- Minimize power while maintaining the real-time properties



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$$f > U f_{max} \quad [\text{Pillai01}]$$



Approaches



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Measuring the power consumption [Pathak11]



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Controlling the power consumption [Cao08]



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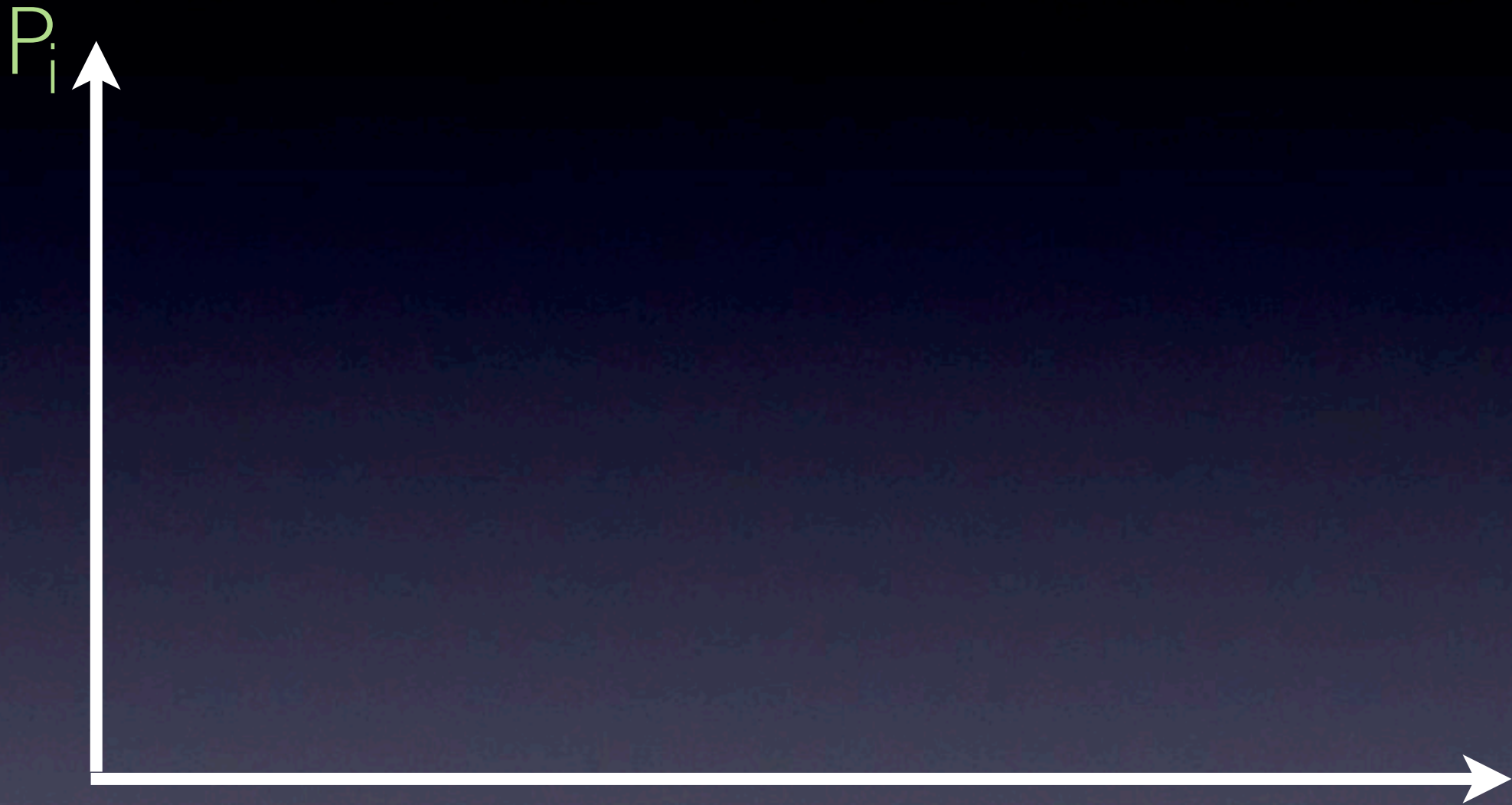
Controlling is fine, but we do not want to interfere in the schedule



Our approach

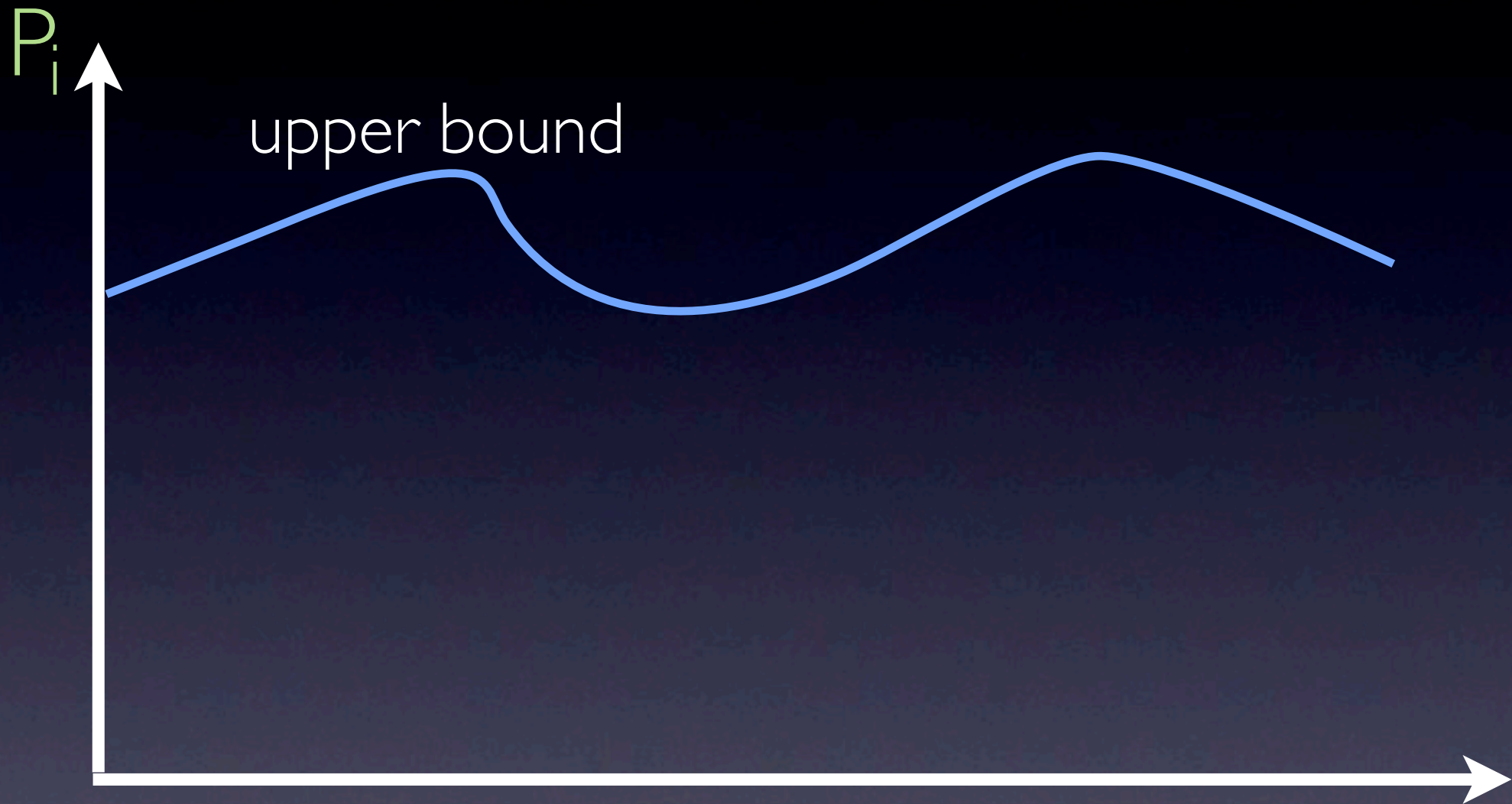


Our approach



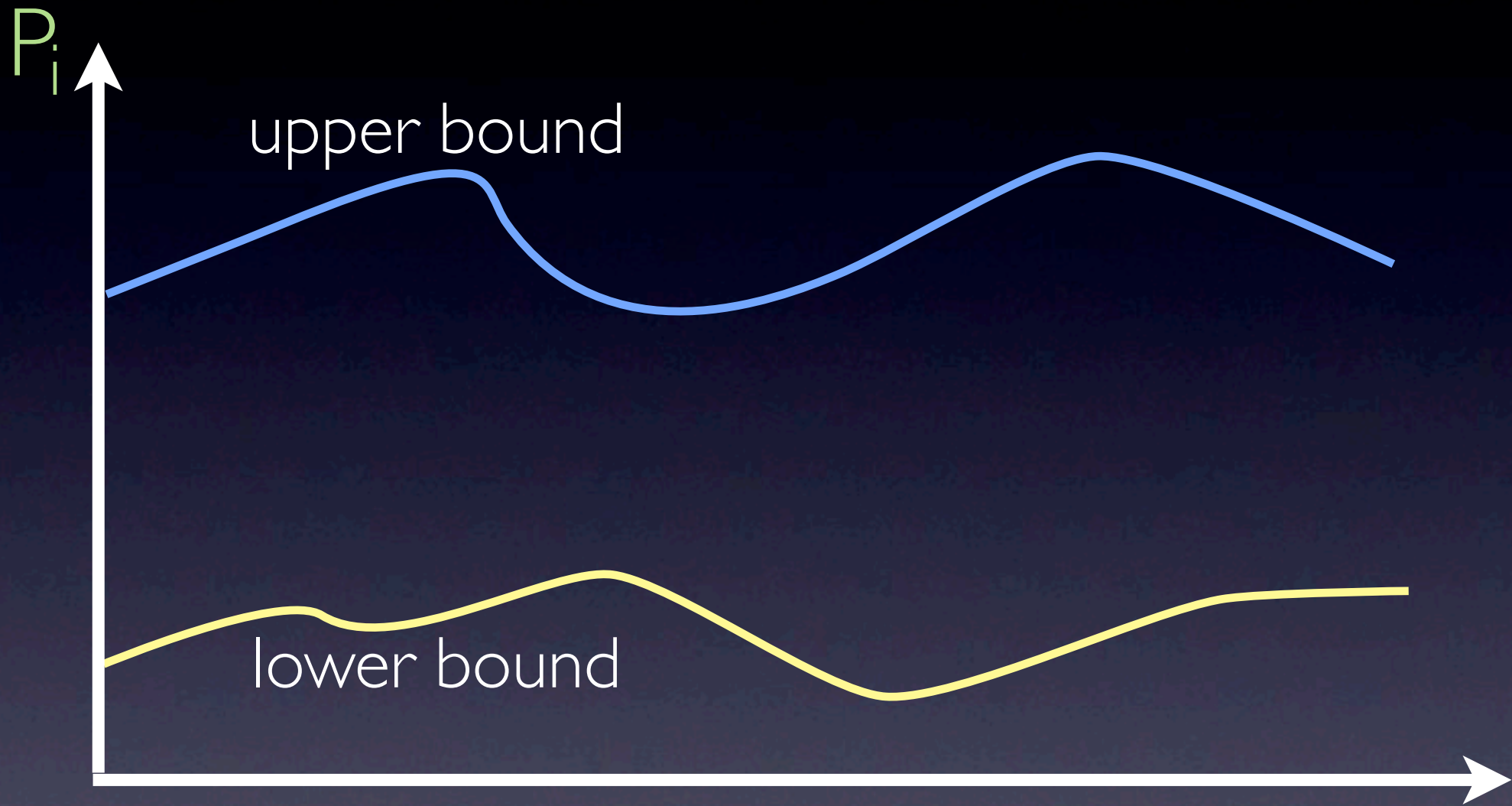


Our approach



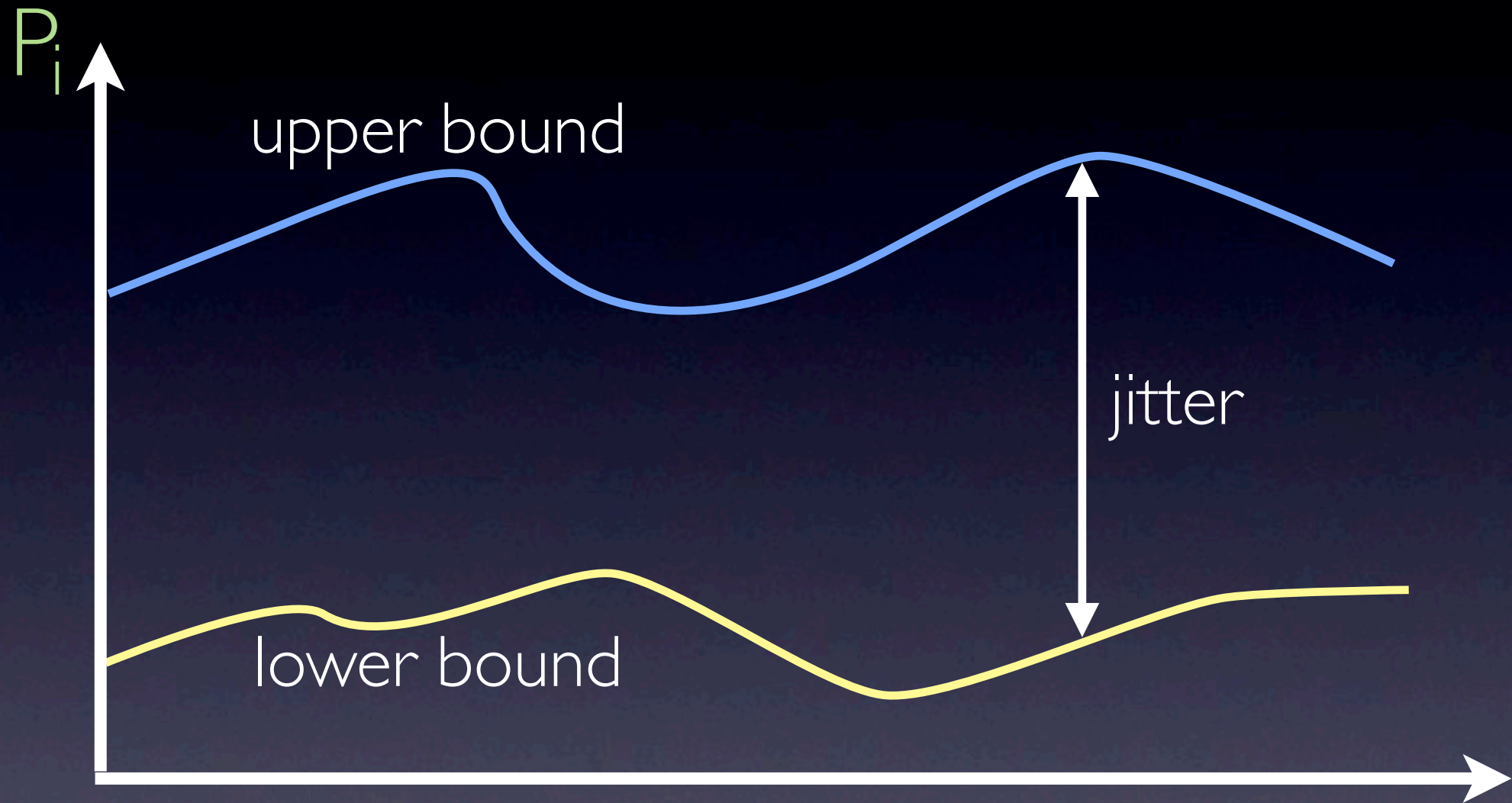


Our approach



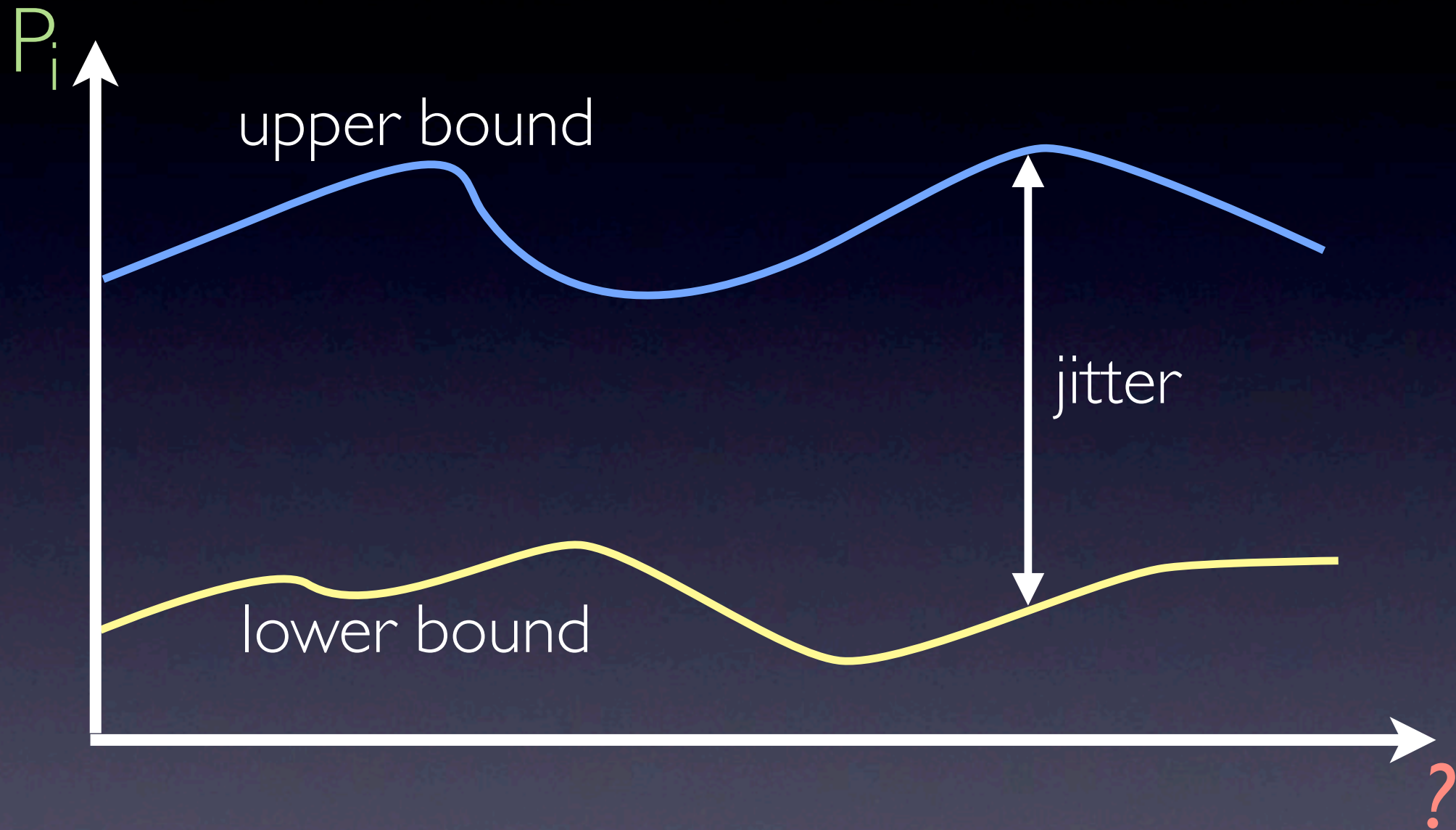


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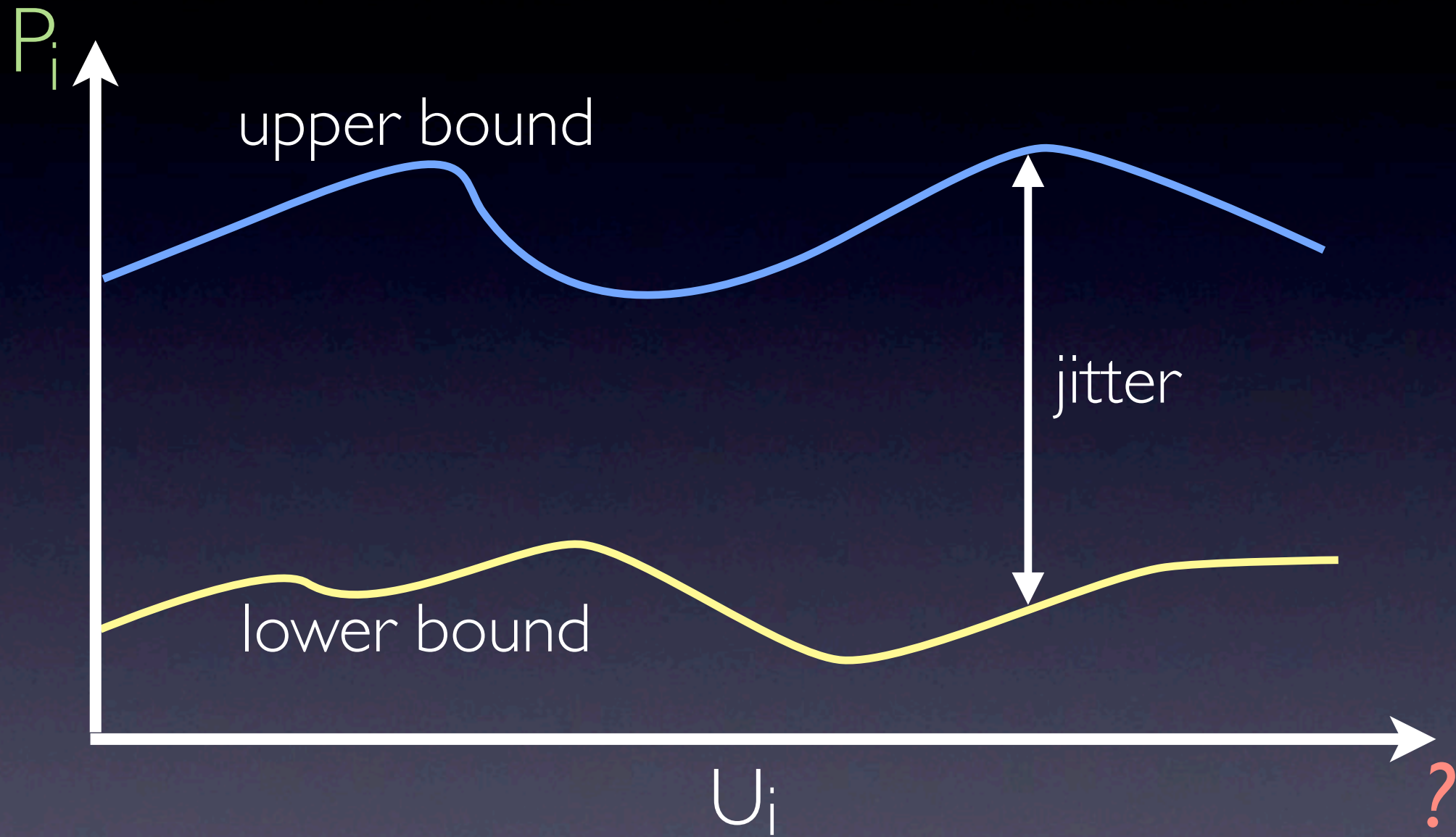


Our approach



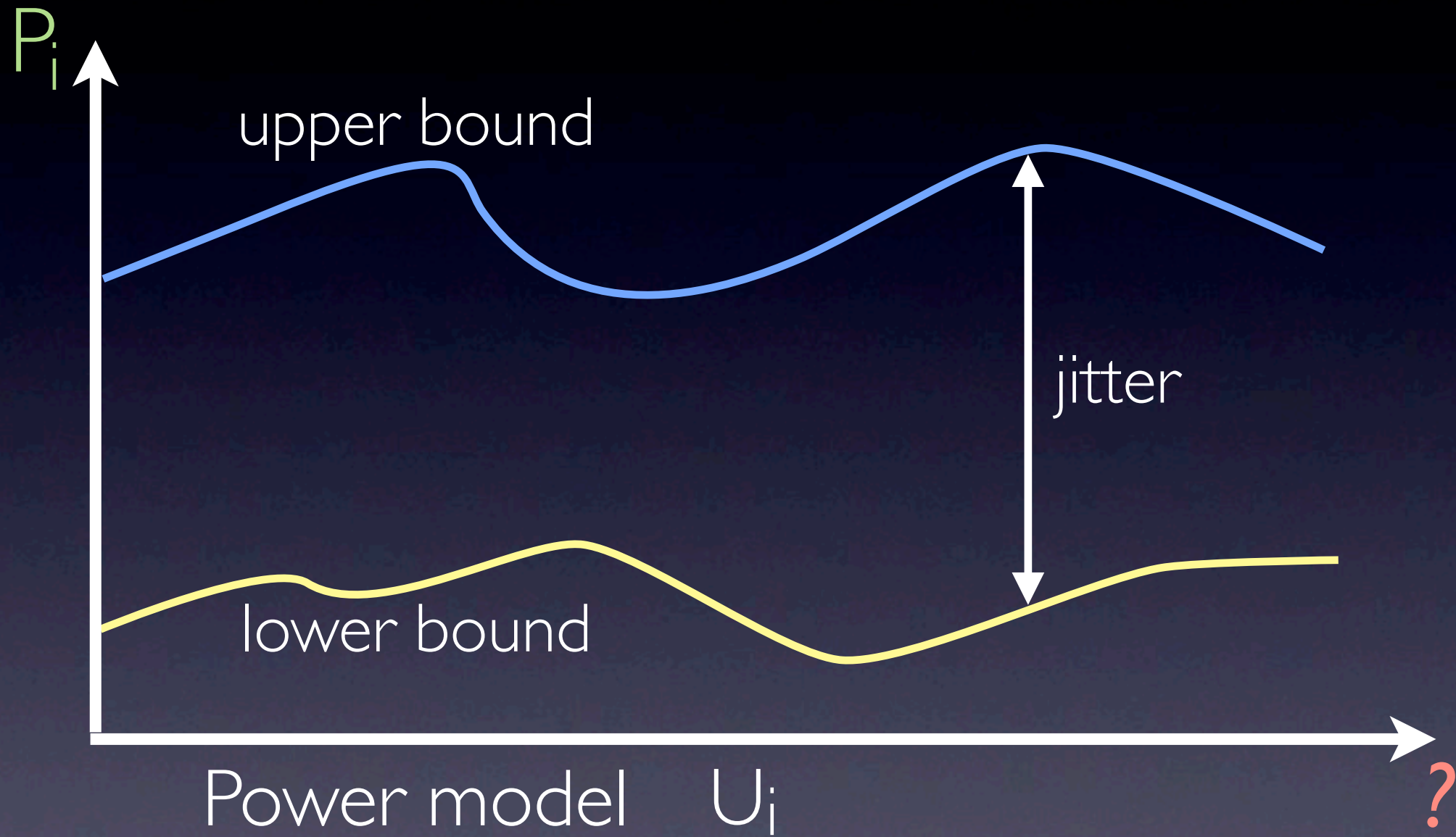


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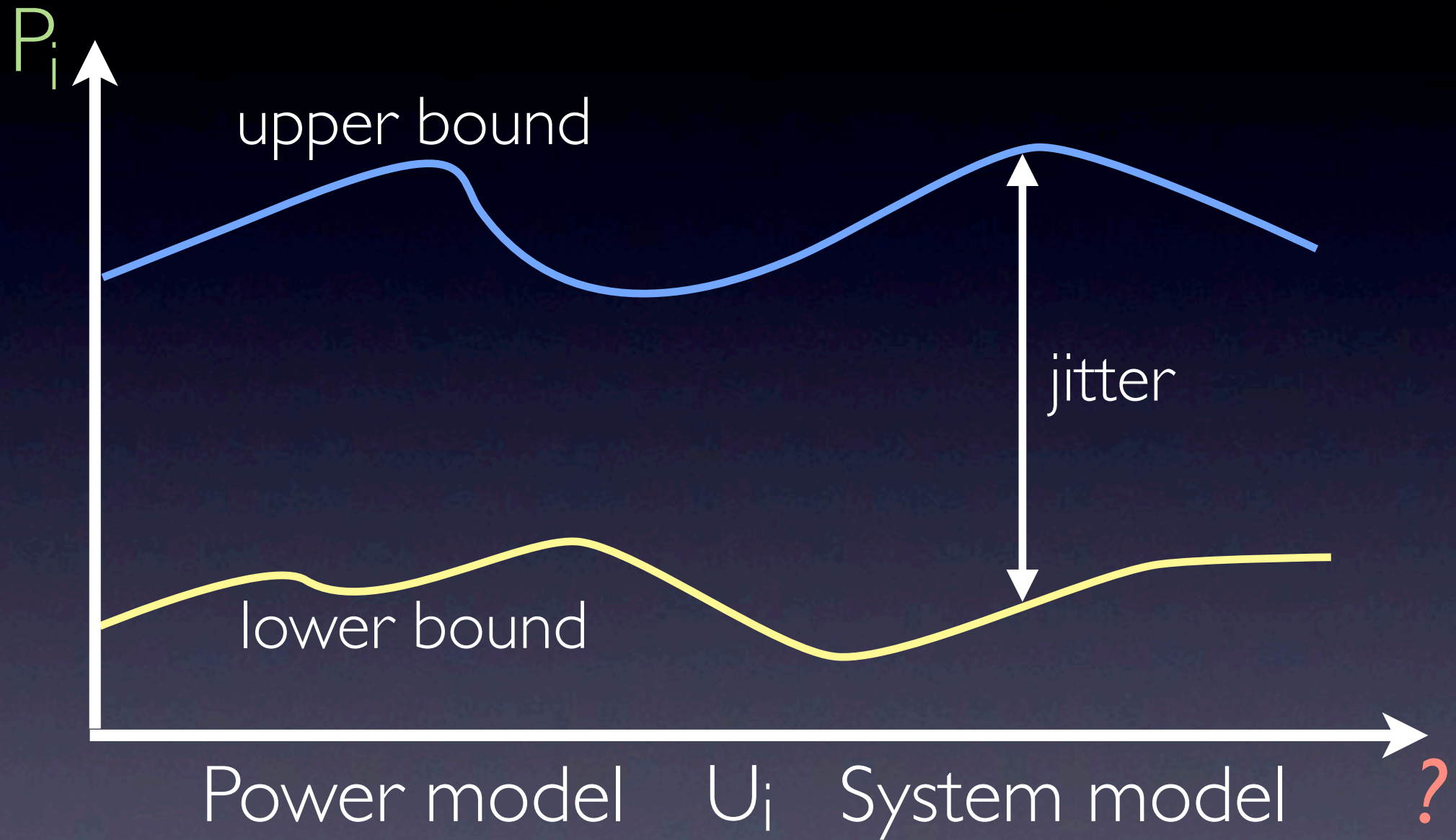


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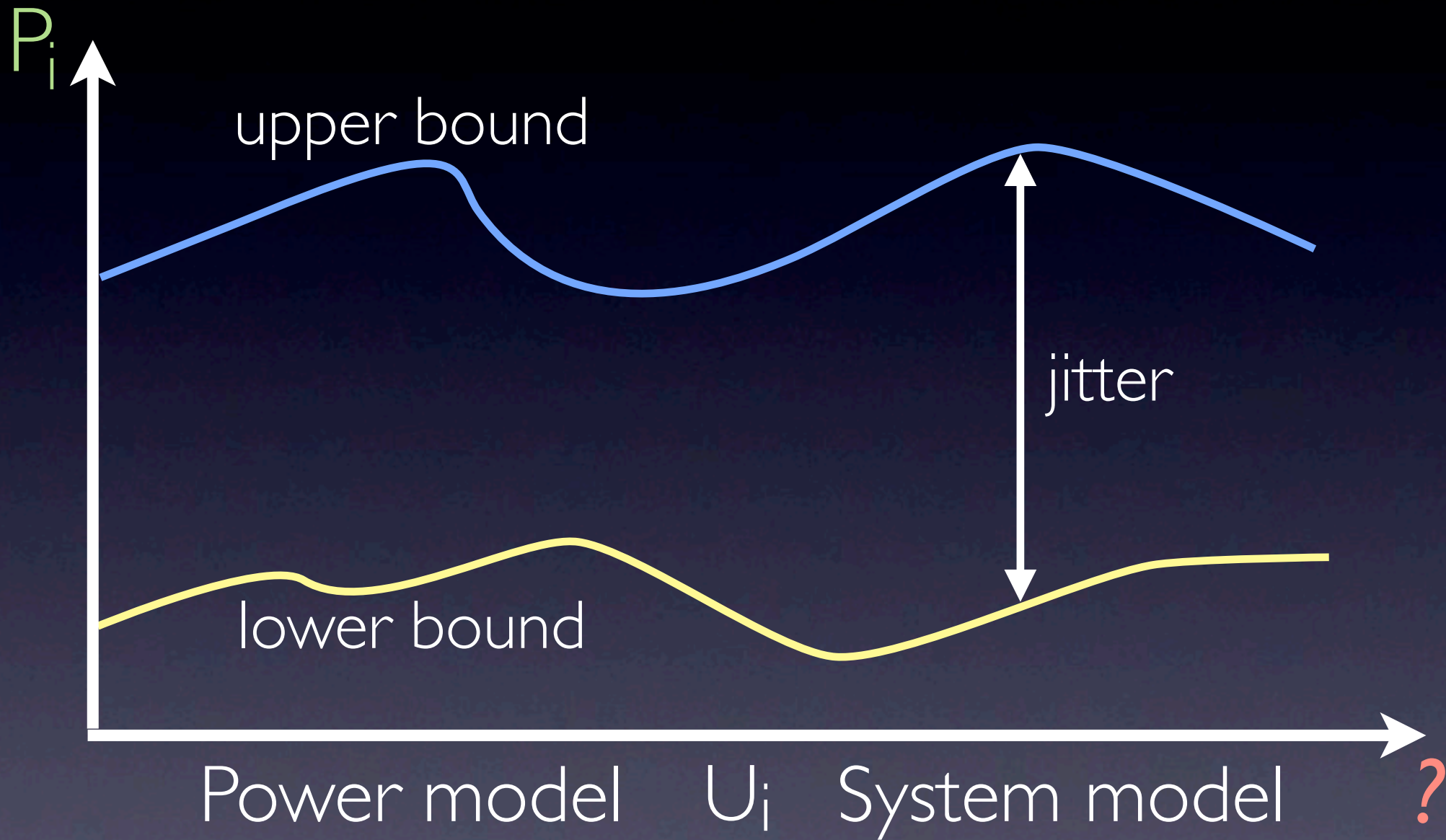


Our approach





Our approach



Lower and upper bounds on the power consumption of a task as functions of task utilization, frequency scaling, and power model.



Our approach



Our approach

Study the compositionality of power consumption (power isolation)



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Isolate power consumption through over-provisioning



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Relationship between the power consumption and the contribution of a single task to this power consumption + the trade-off between quality and cost of power isolation.



Our approach

Study the compositionality of power consumption (power isolation)

Isolate power consumption through over-provisioning

Relationship between the power consumption and the contribution of a single task to this power consumption + the trade-off between quality and cost of power isolation.

We discuss the variance between lower and upper bounds (quality) and the power consumption overhead (cost) of power isolation.



First, the math...



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CPU energy consumption of a EDF system with utilization $U = \sum_{i=1}^n U_i$
running at frequency κf_{max} , $U \leq \kappa \leq 1$
in the interval $[t_0, t_1)$



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$$t_{idle}c_0 + t_{running}(c_0 + c_1(\kappa f_{max})^\omega)$$



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$$t_{running} = (t_1 - t_0) \sum_{i=1}^n \frac{C_i}{\kappa T_i} = (t_1 - t_0) \frac{U}{\kappa}$$



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$$E(\kappa, U) = (t_1 - t_0)c_1 \frac{U}{\kappa} (\kappa f_{max})^\omega$$



Two frequency levels



Two frequency levels





Two frequency levels





Two frequency levels





Two frequency levels



task 1
(2,4)





Two frequency levels



task 1
(2,4)





Two frequency levels



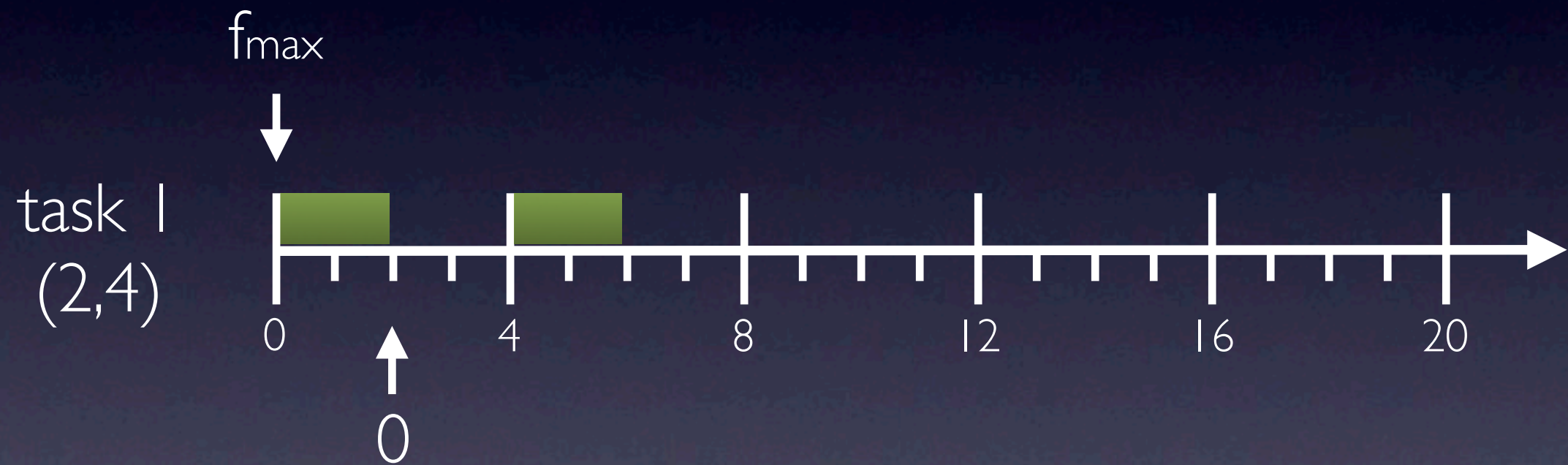
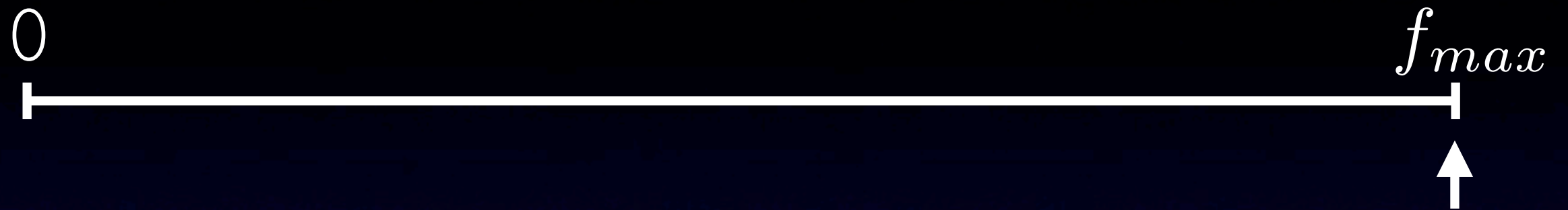


Two frequency levels



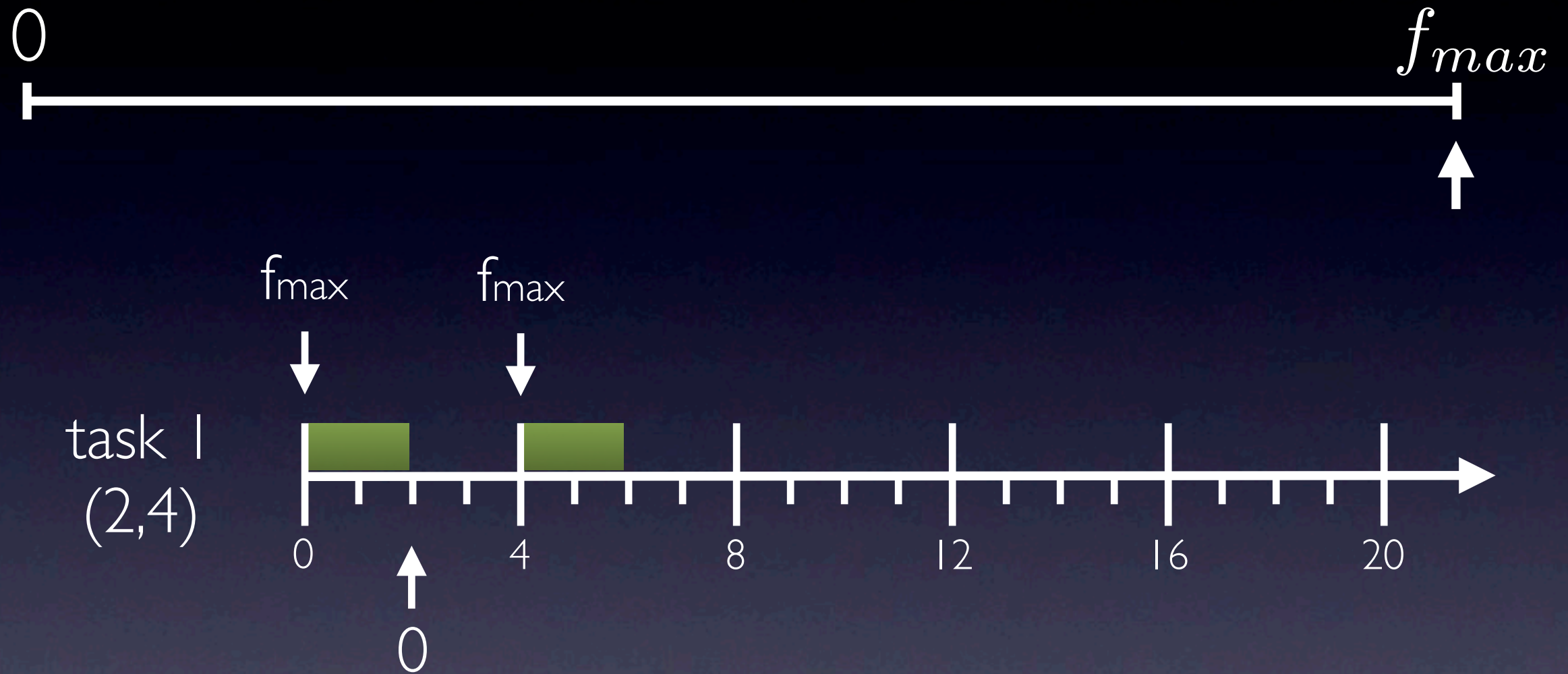


Two frequency levels



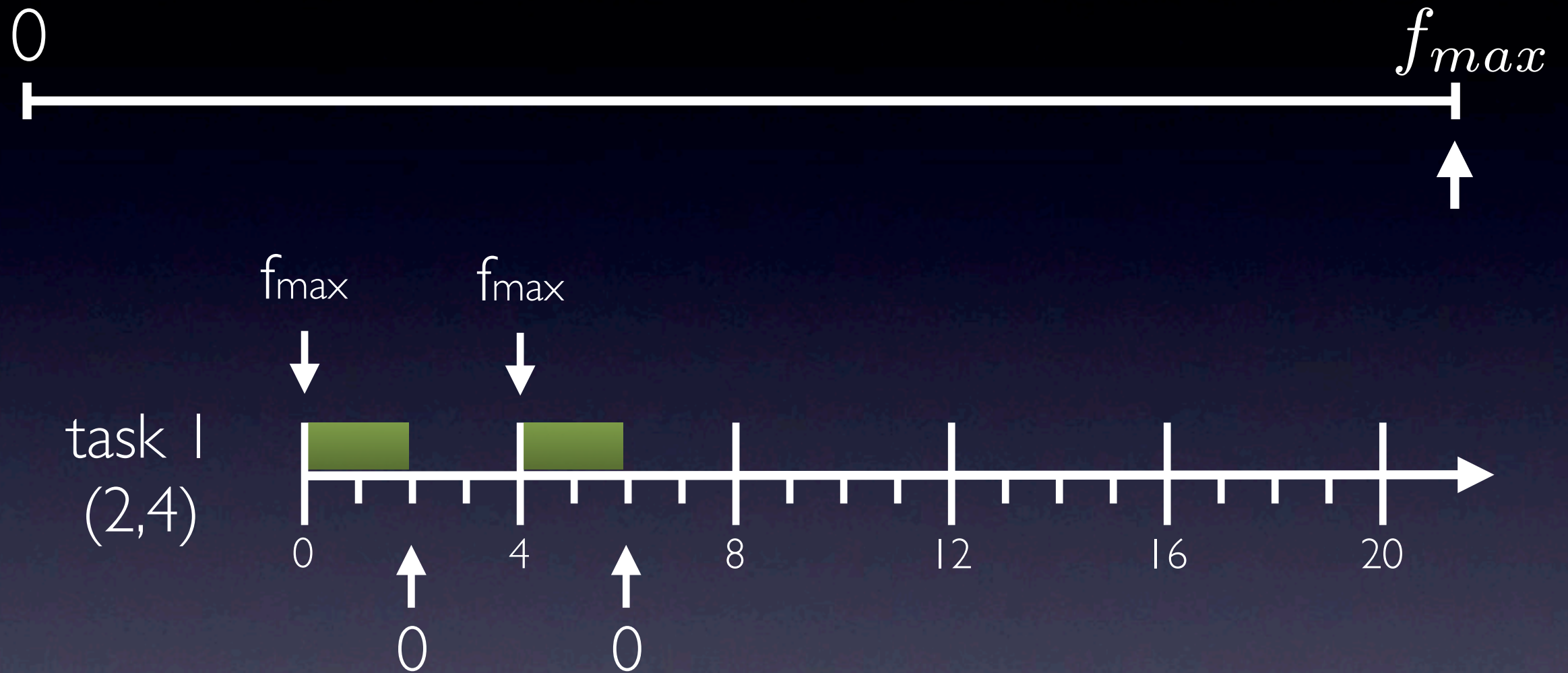


Two frequency levels



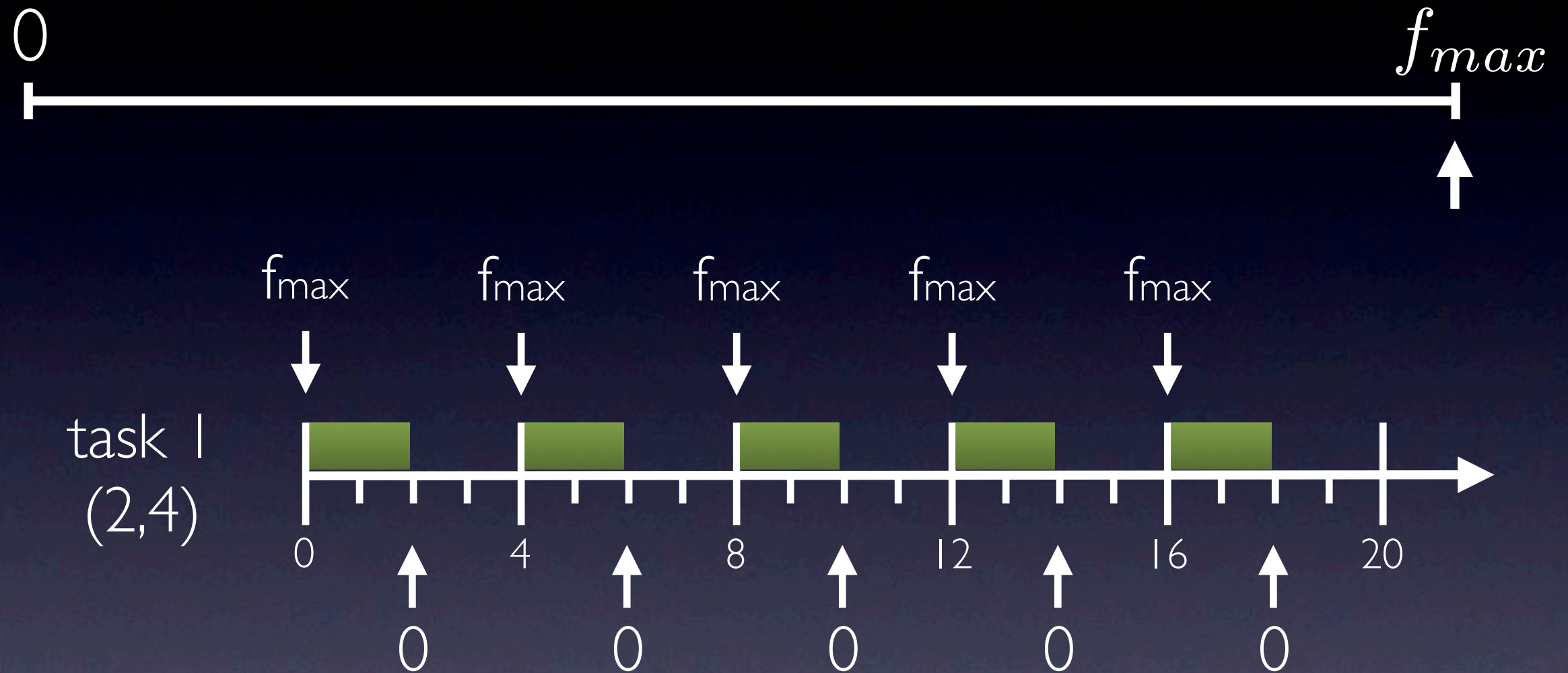


Two frequency levels





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Two frequency levels



$$E(1, U) = (t_1 - t_0) c_1 U f_{max}^\omega$$



Two frequency levels



$$E(1, U) = (t_1 - t_0) c_1 U f_{max}^{\omega} \sum_{i=1}^n \frac{C_i}{T_i}$$



Two frequency levels



$$E(1, U) = (t_1 - t_0)c_1 U f_{max}^\omega \sum_{i=1}^n \frac{C_i}{T_i}$$

$$bE_i^u = bE_i^l = E(1, U_i) = (t_1 - t_0)c_1 U_i f_{max}^\omega$$



Two frequency levels



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$$E\left(1, \sum_{i=1}^n U_i\right) = \sum_{i=1}^n E(1, U_i)$$



Two frequency levels



$$E(1, U) = (t_1 - t_0) c_1 U f_{max}^\omega \sum_{i=1}^n \frac{C_i}{T_i}$$

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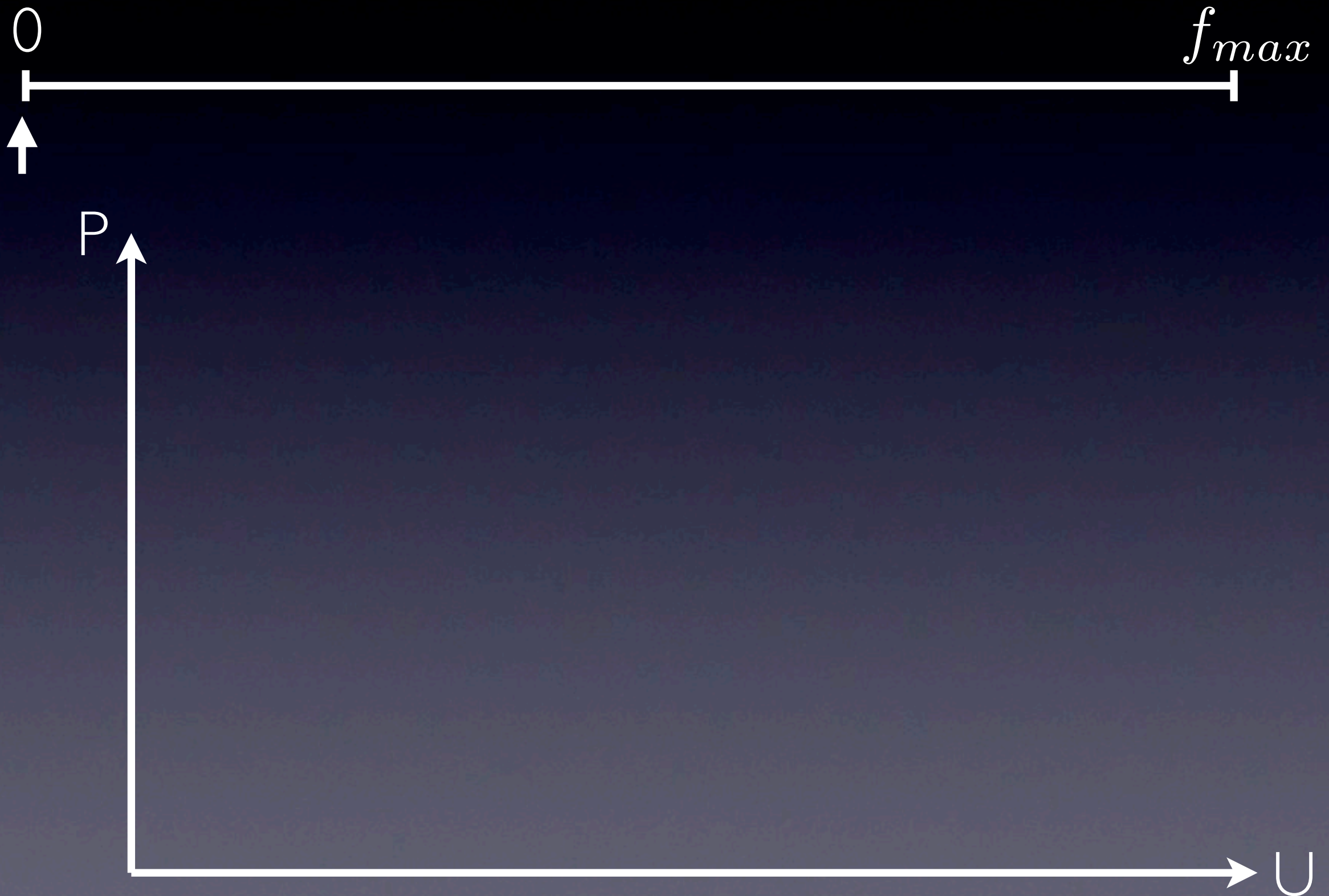
$$E\left(1, \sum_{i=1}^n U_i\right) = \sum_{i=1}^n E(1, U_i) *$$



Continuous frequency levels

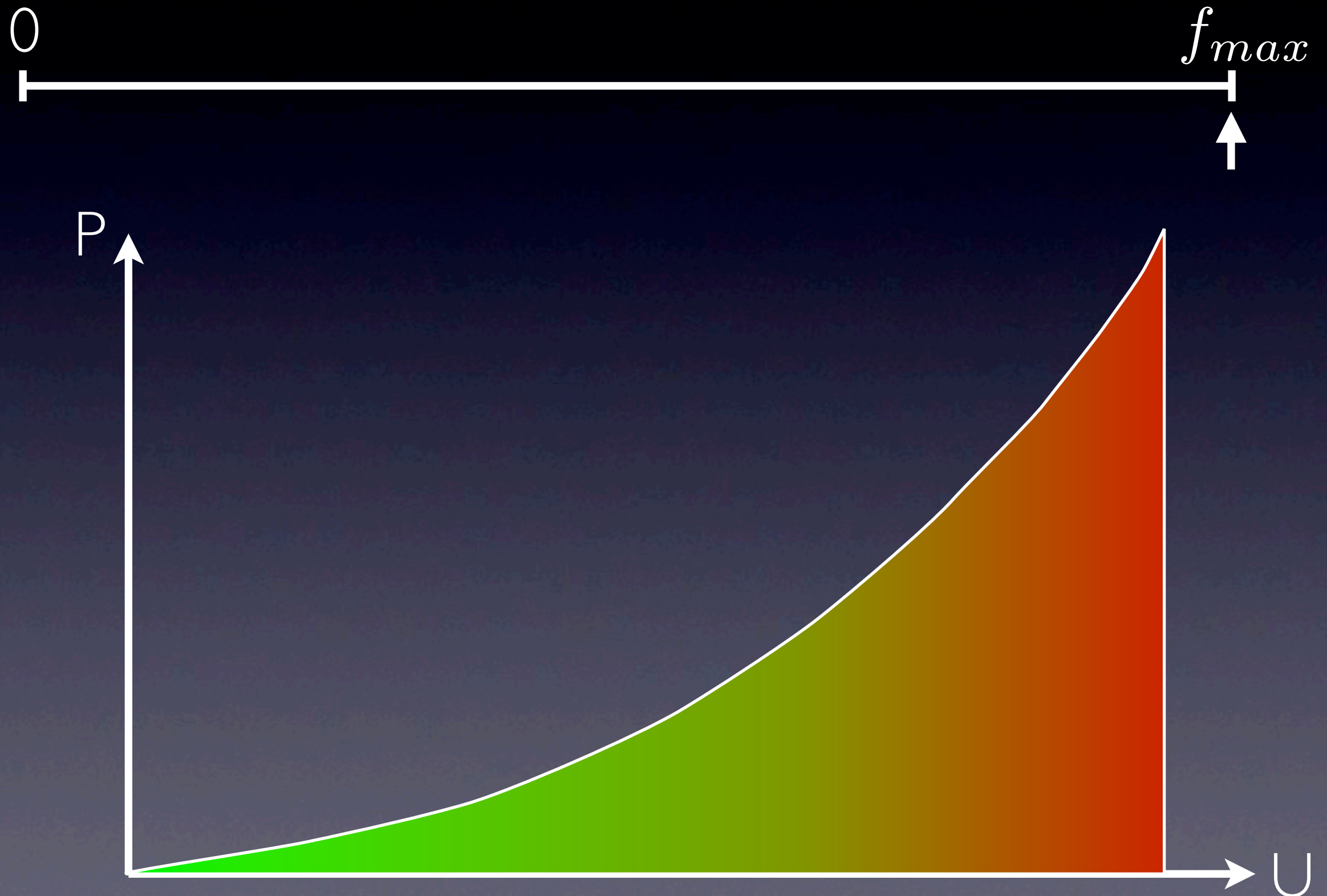


Continuous frequency levels



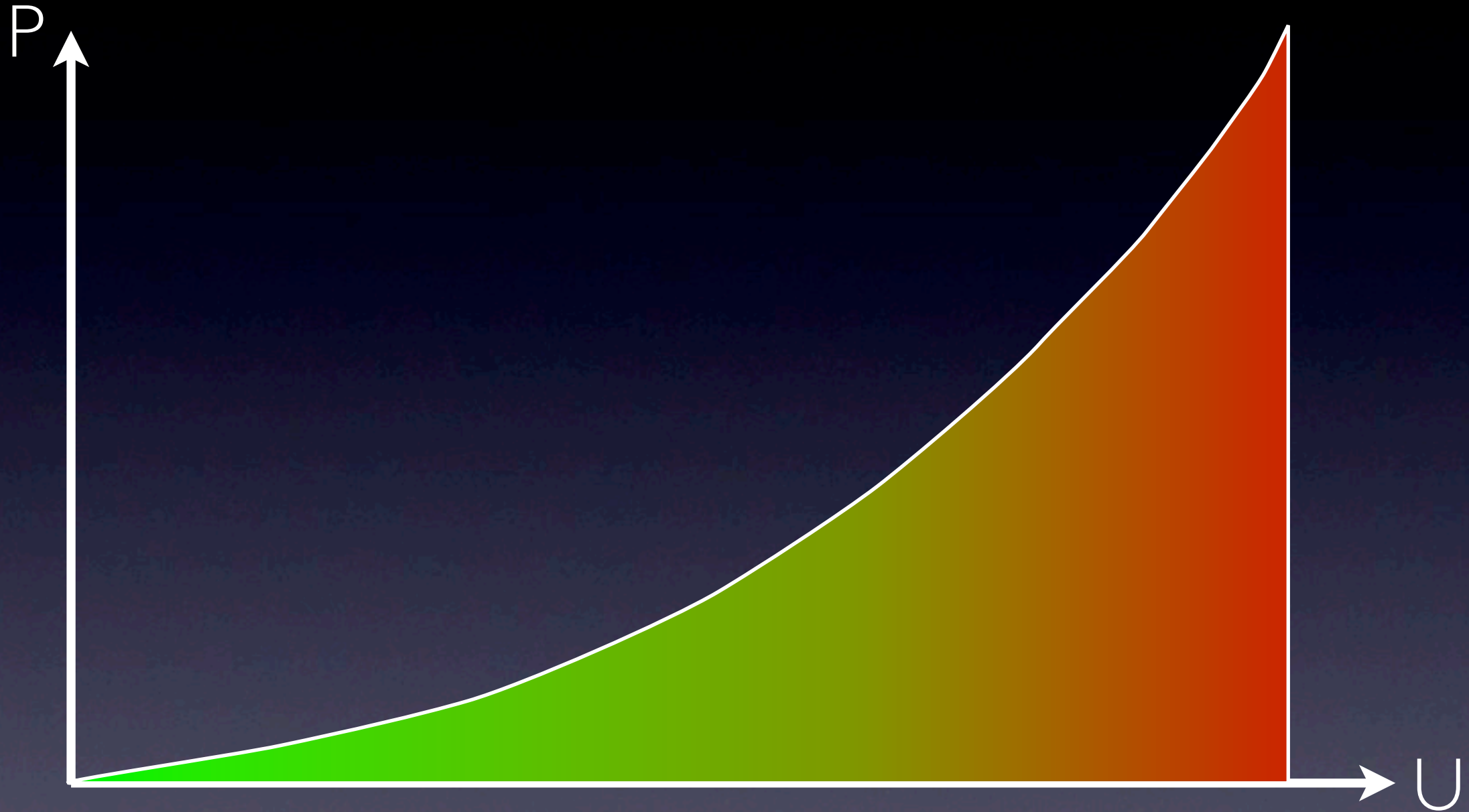


Continuous frequency levels



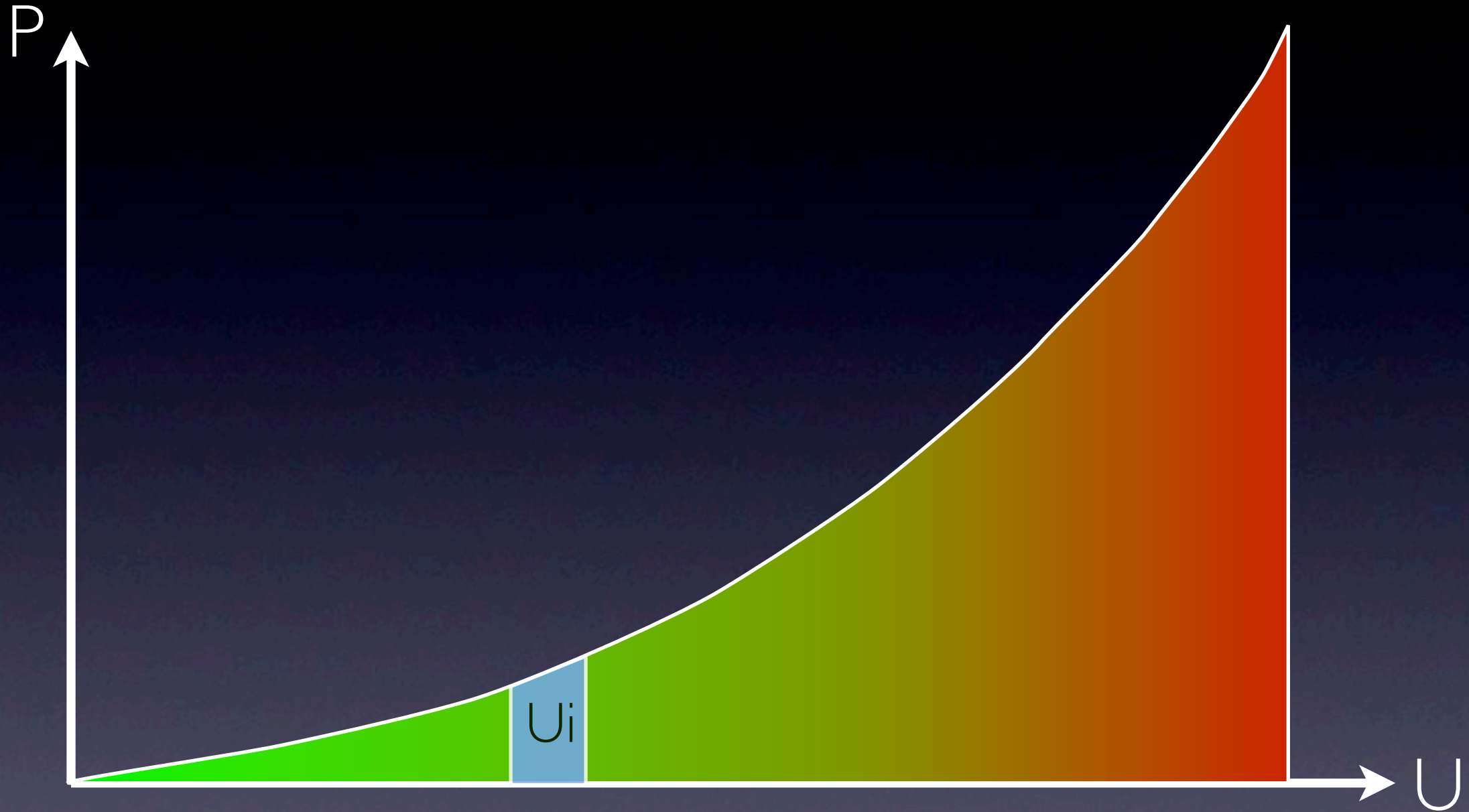


Continuous frequency levels



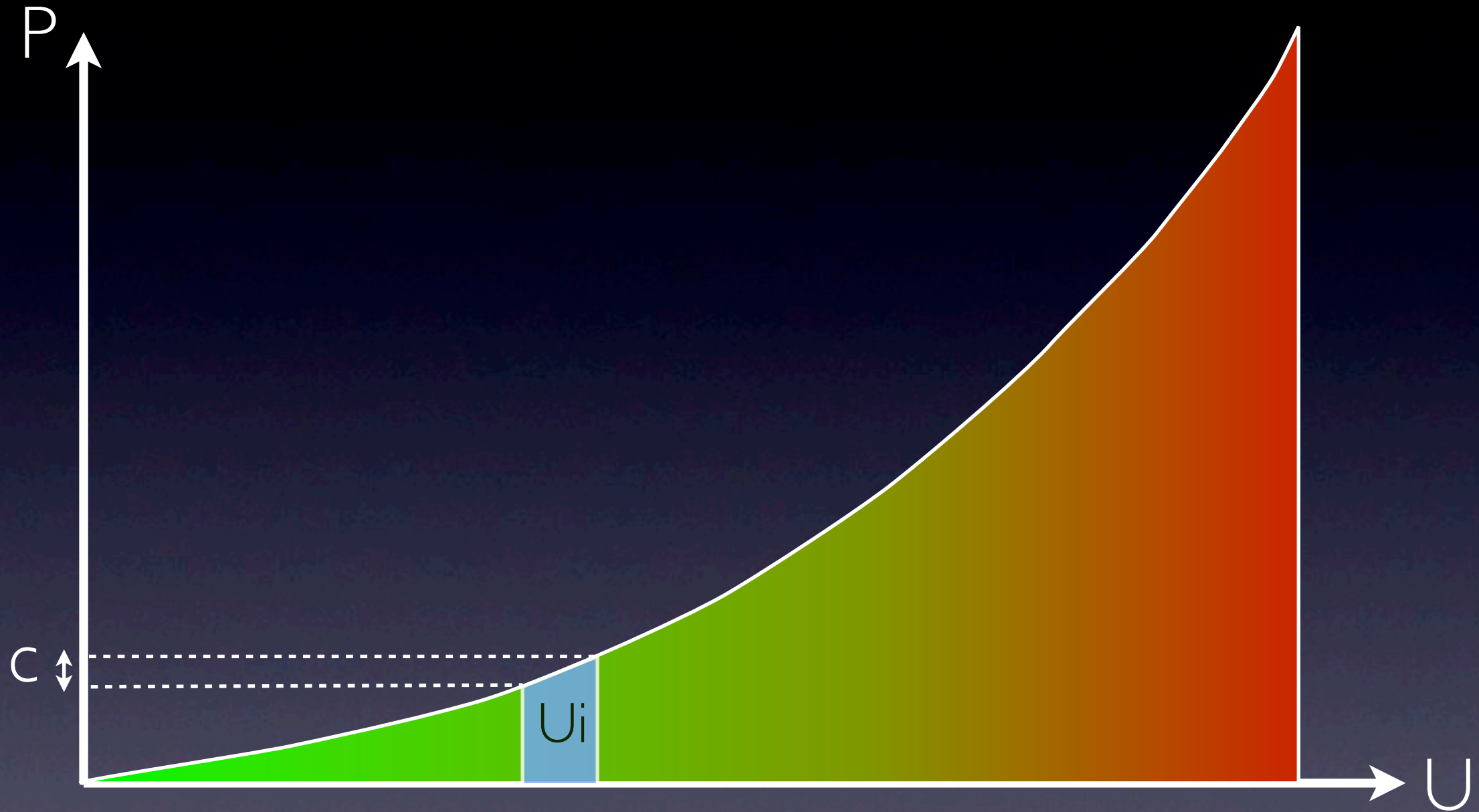


Continuous frequency levels



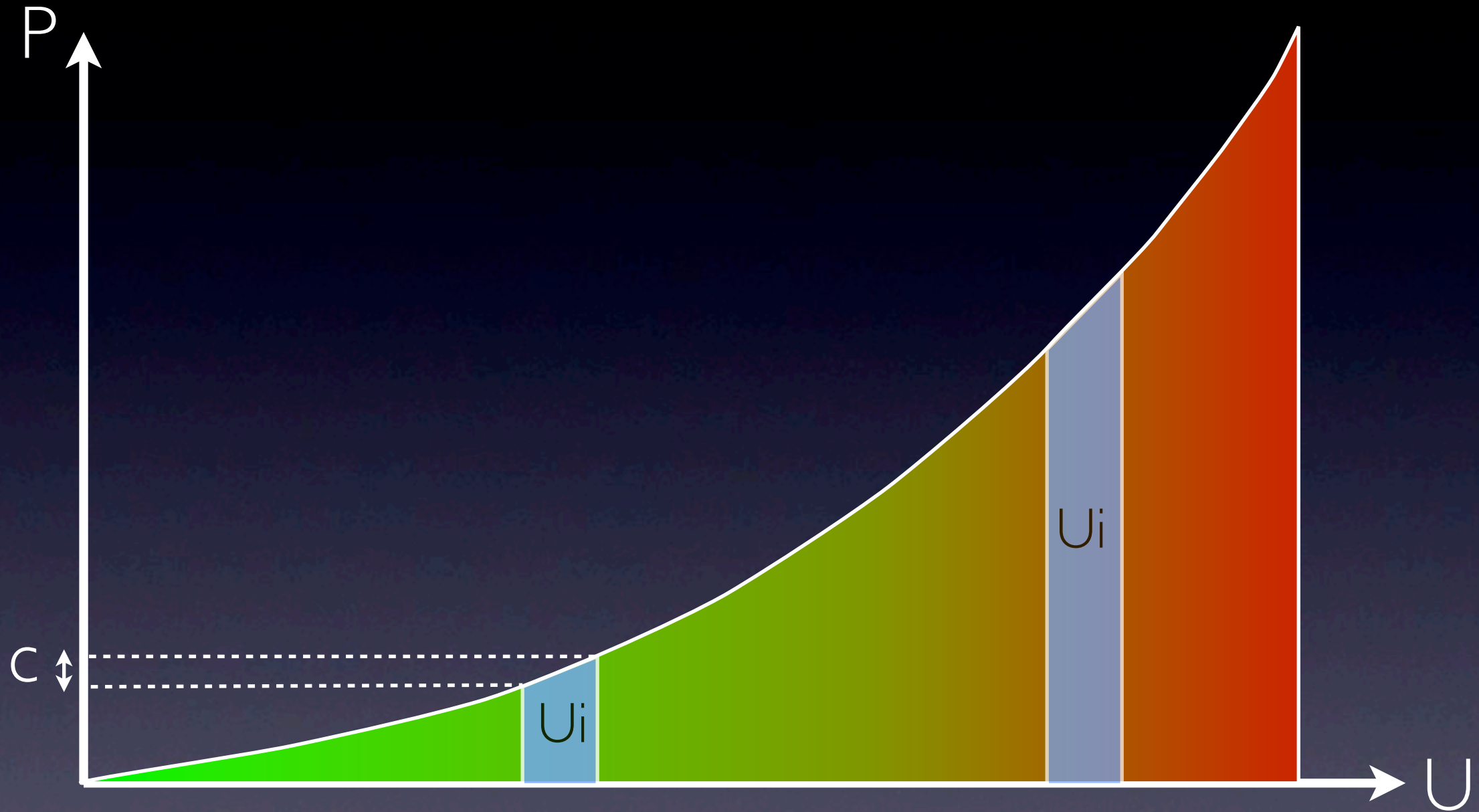


Continuous frequency levels



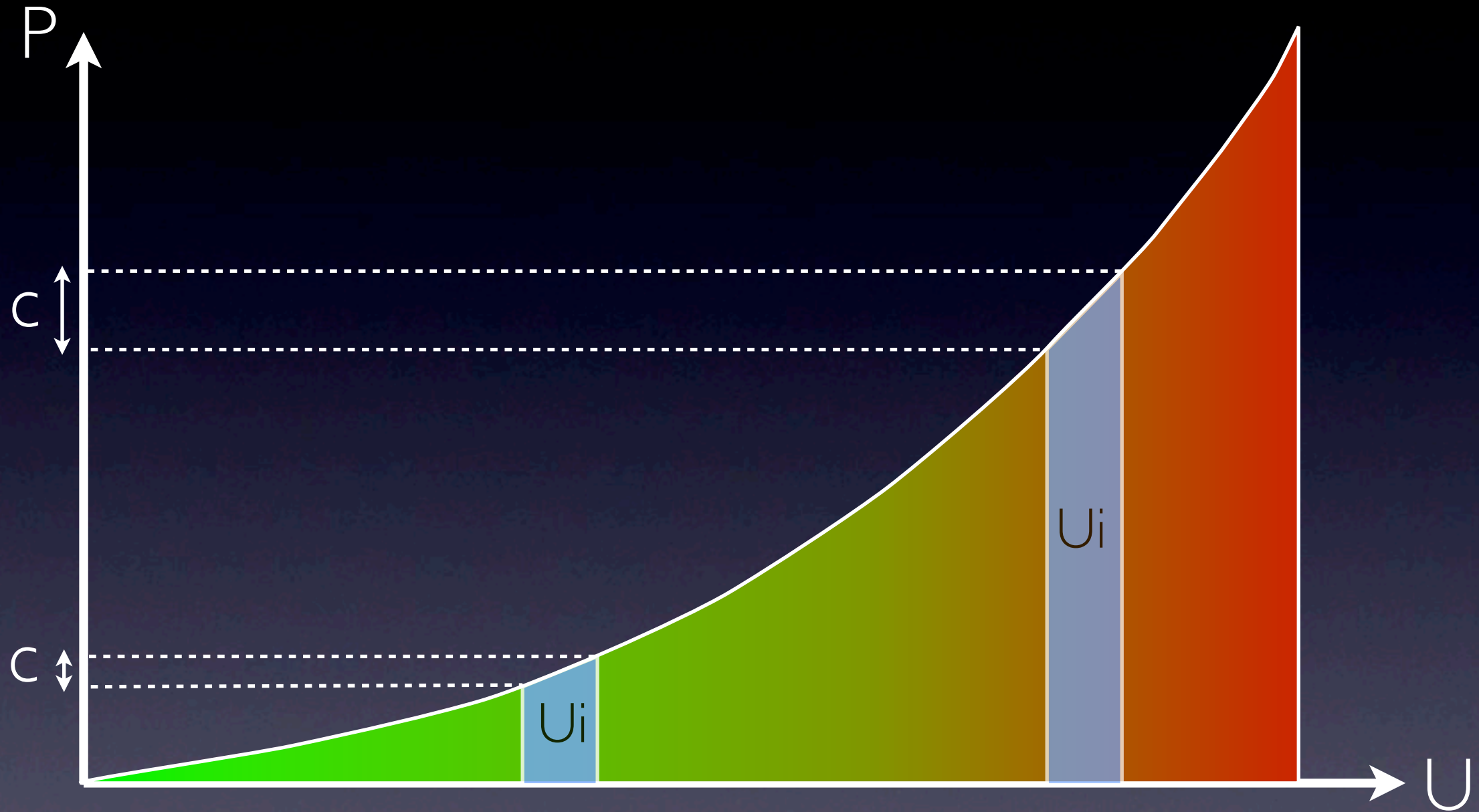


Continuous frequency levels



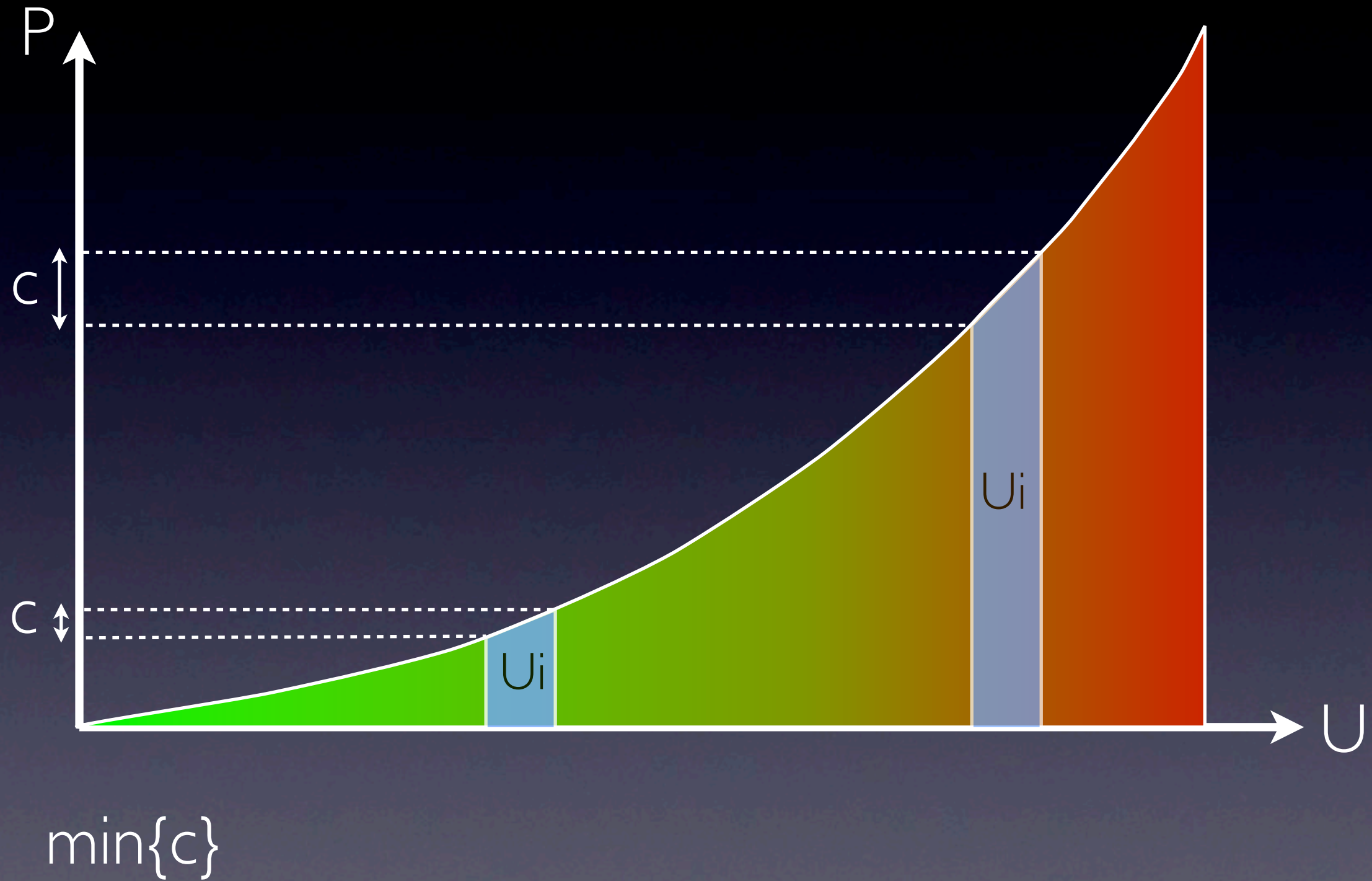


Continuous frequency levels



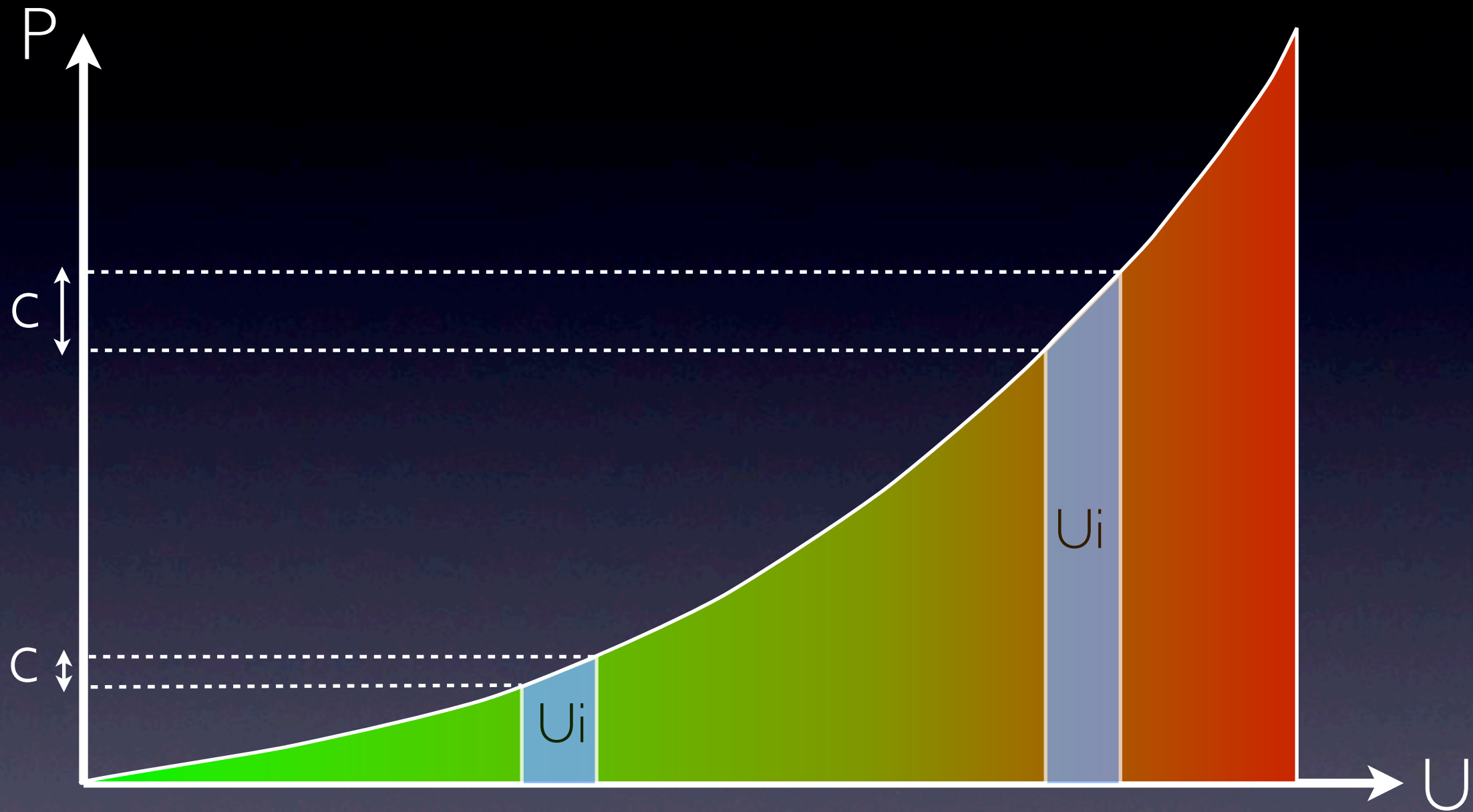


Continuous frequency levels





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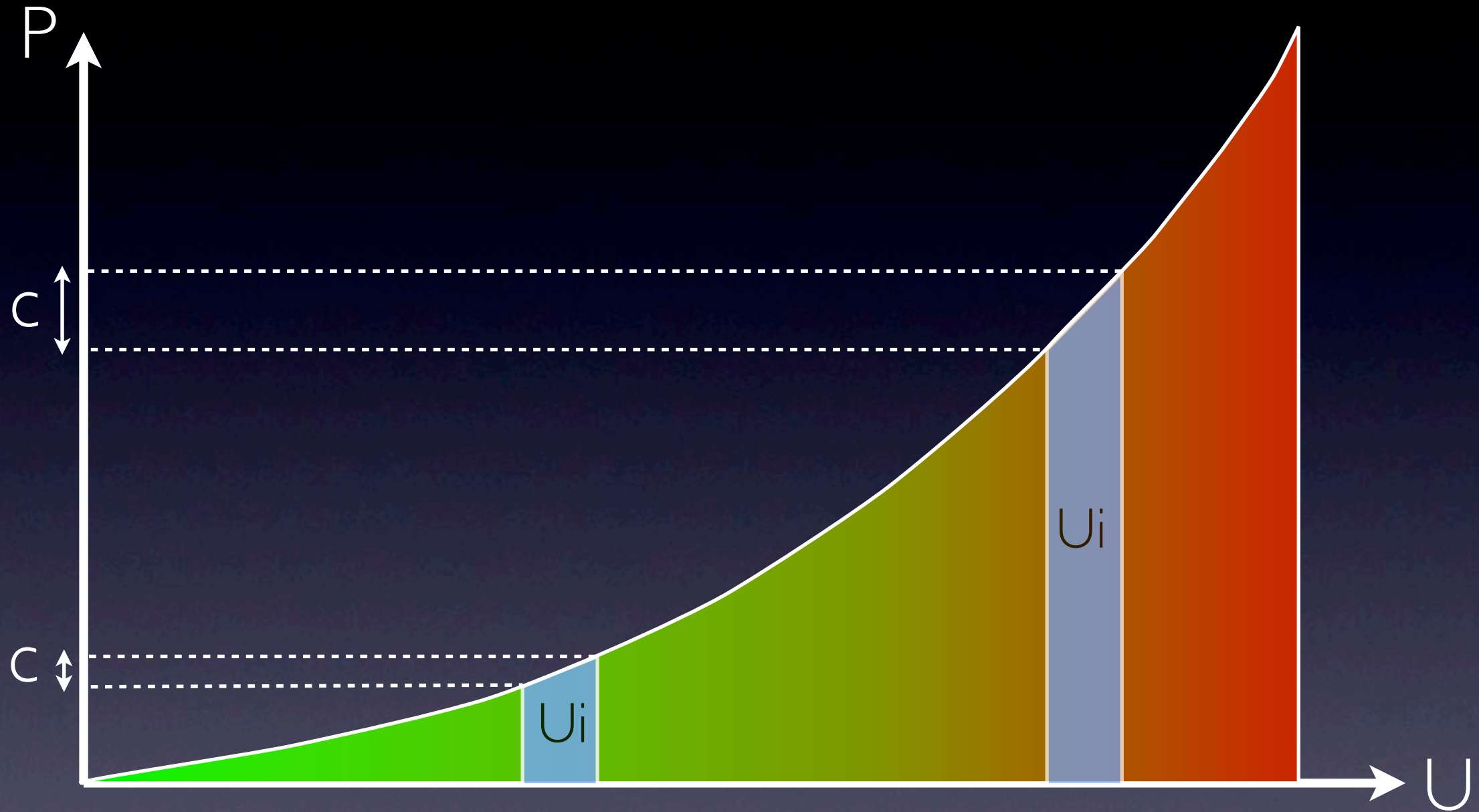
$\min\{c\}$

$\max\{c\}$

task i is the only running task



Continuous frequency levels



$\min\{c\}$

task i is the only running task

$\max\{c\}$

f is switched from $I-U_i$ to I



Continuous frequency levels



Continuous frequency levels

$$E(U, U) = (t_1 - t_0)c_1(f_{max}U)^\omega.$$



Continuous frequency levels

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$$\begin{aligned} bE_i^u &= E(1, 1) - E(1 - U_i, 1 - U_i) \\ &= (t_1 - t_0)c_1f_{max}^\omega(1 - (1 - U_i)^\omega) \end{aligned}$$

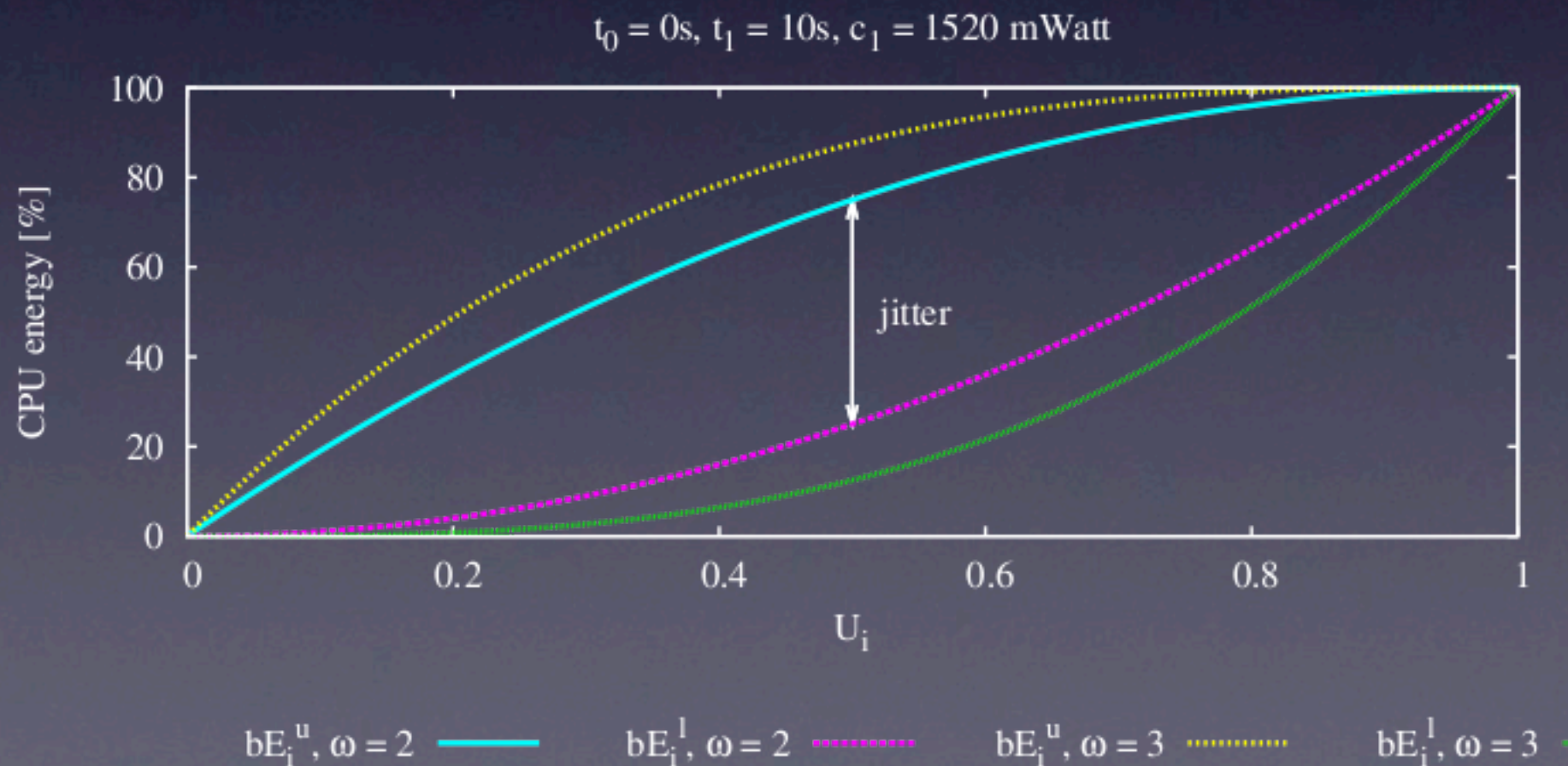


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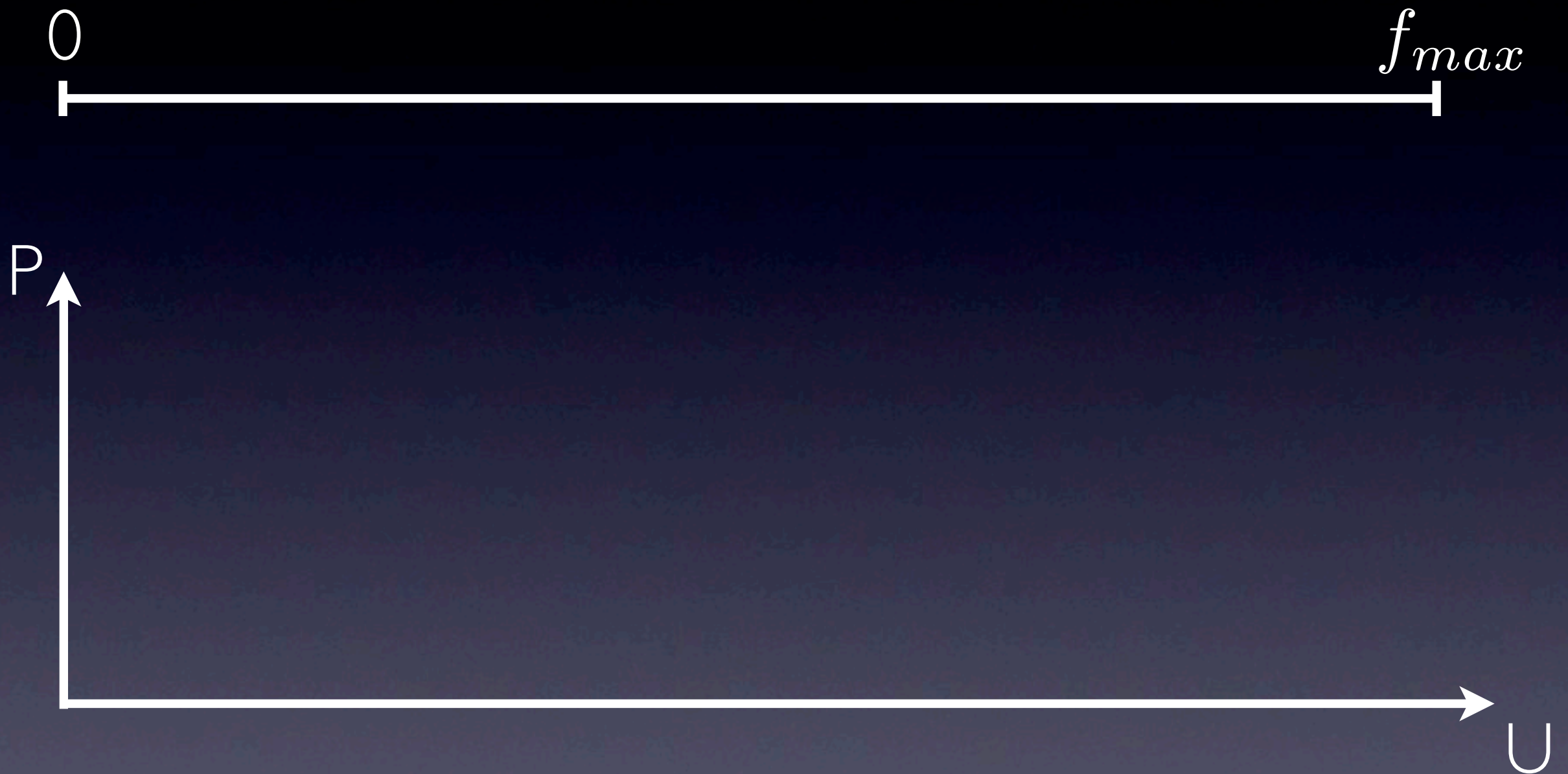




Discrete frequency levels

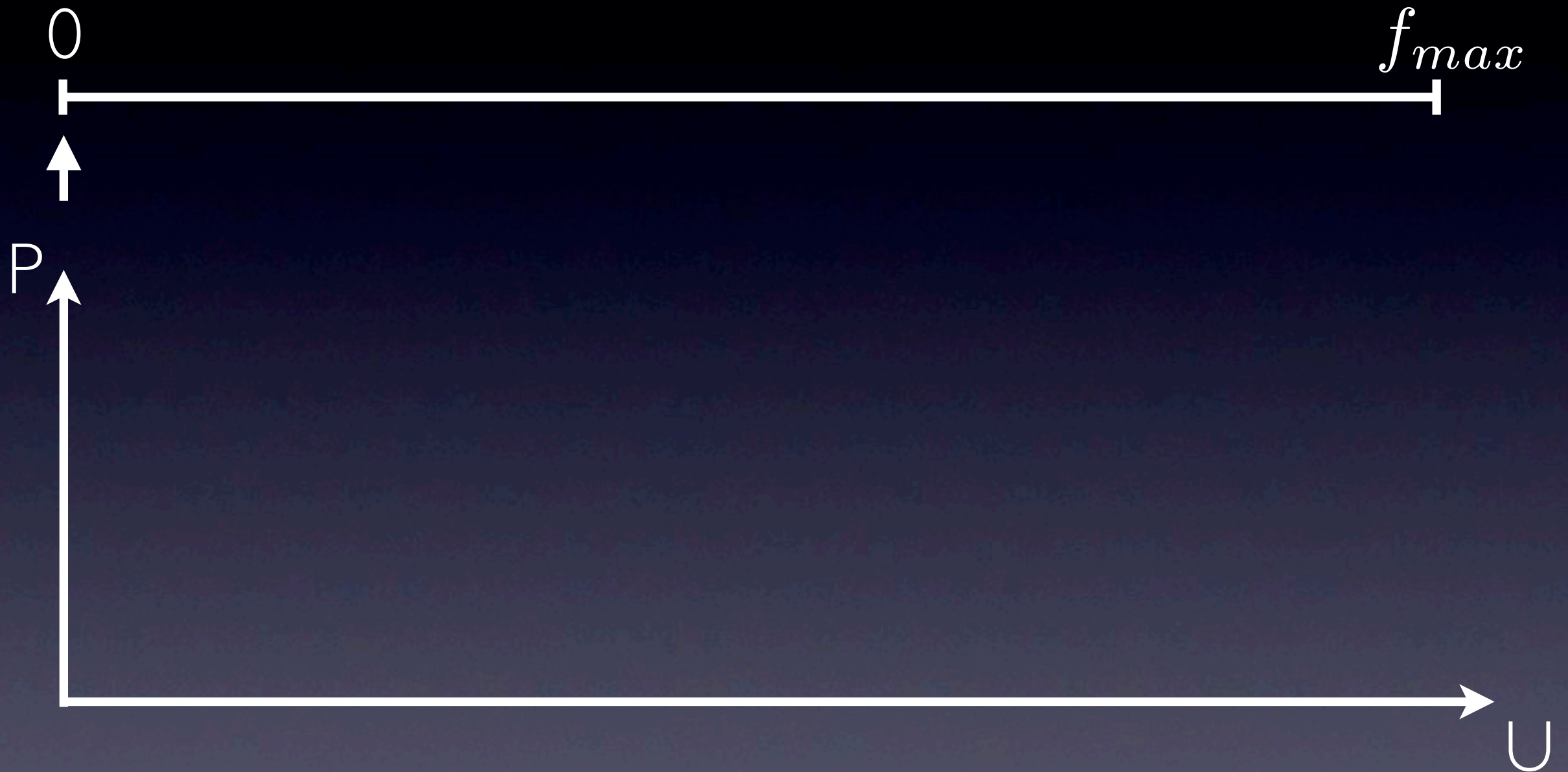


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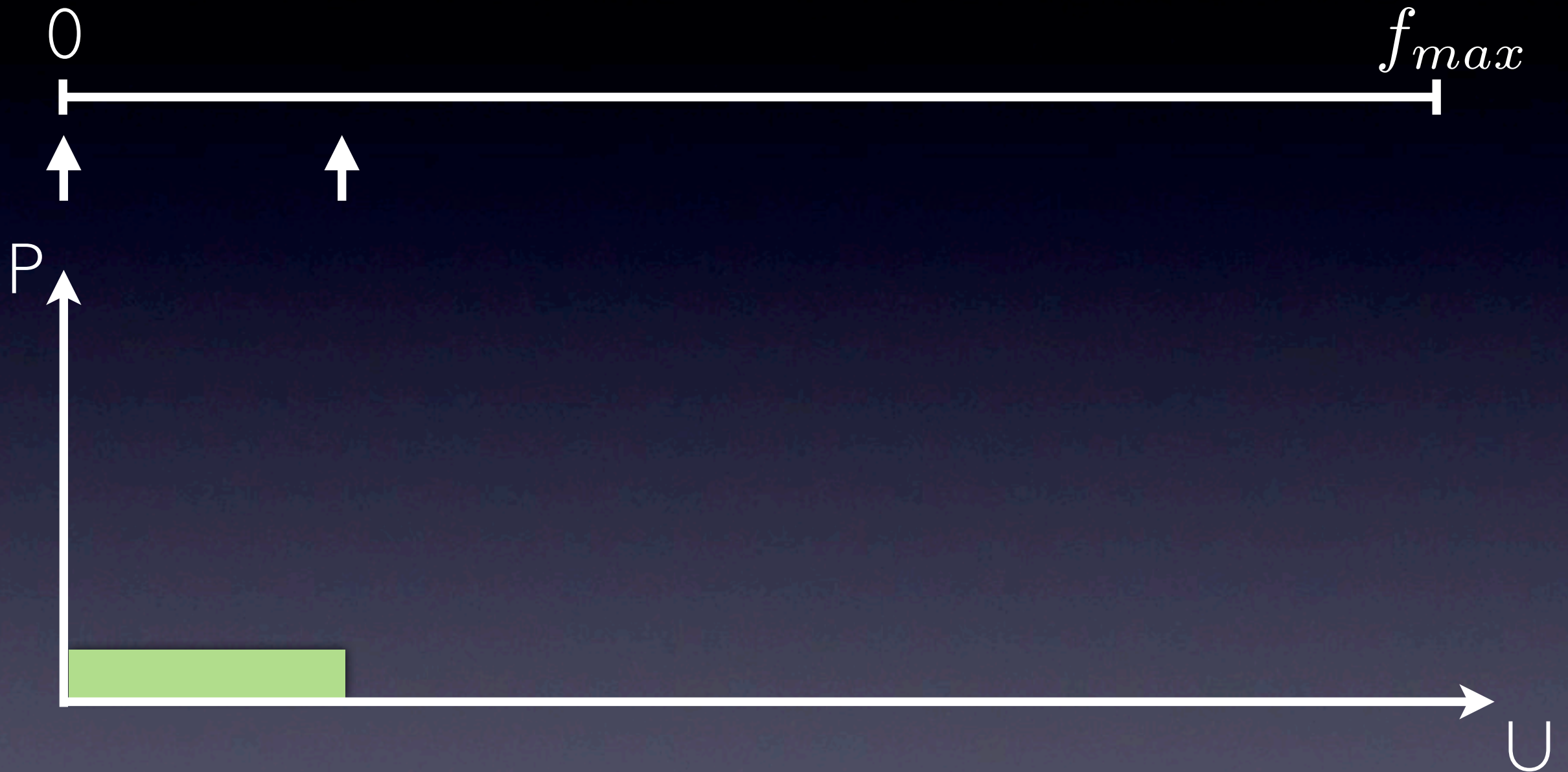


Discrete frequency levels



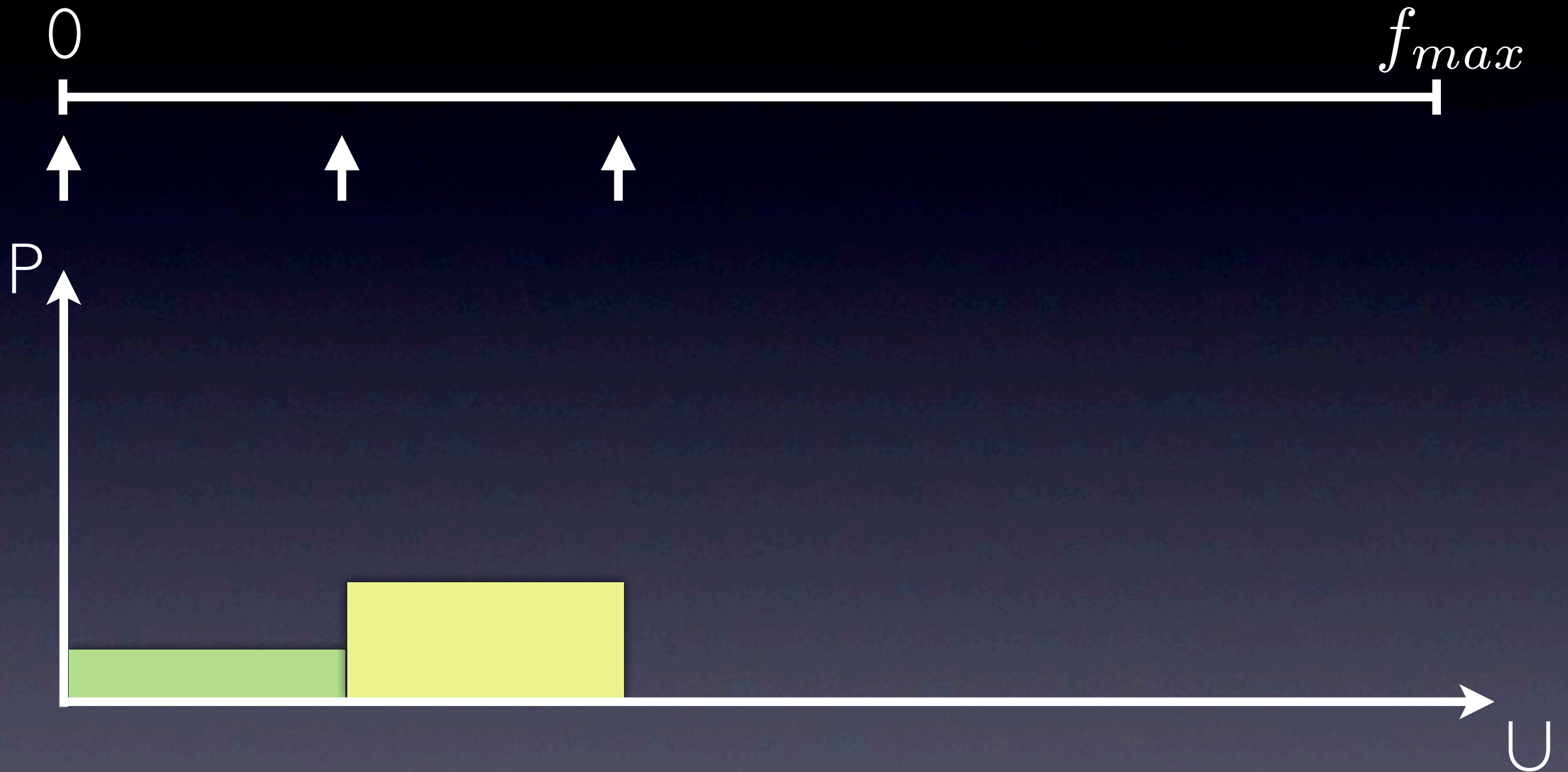


Discrete frequency levels



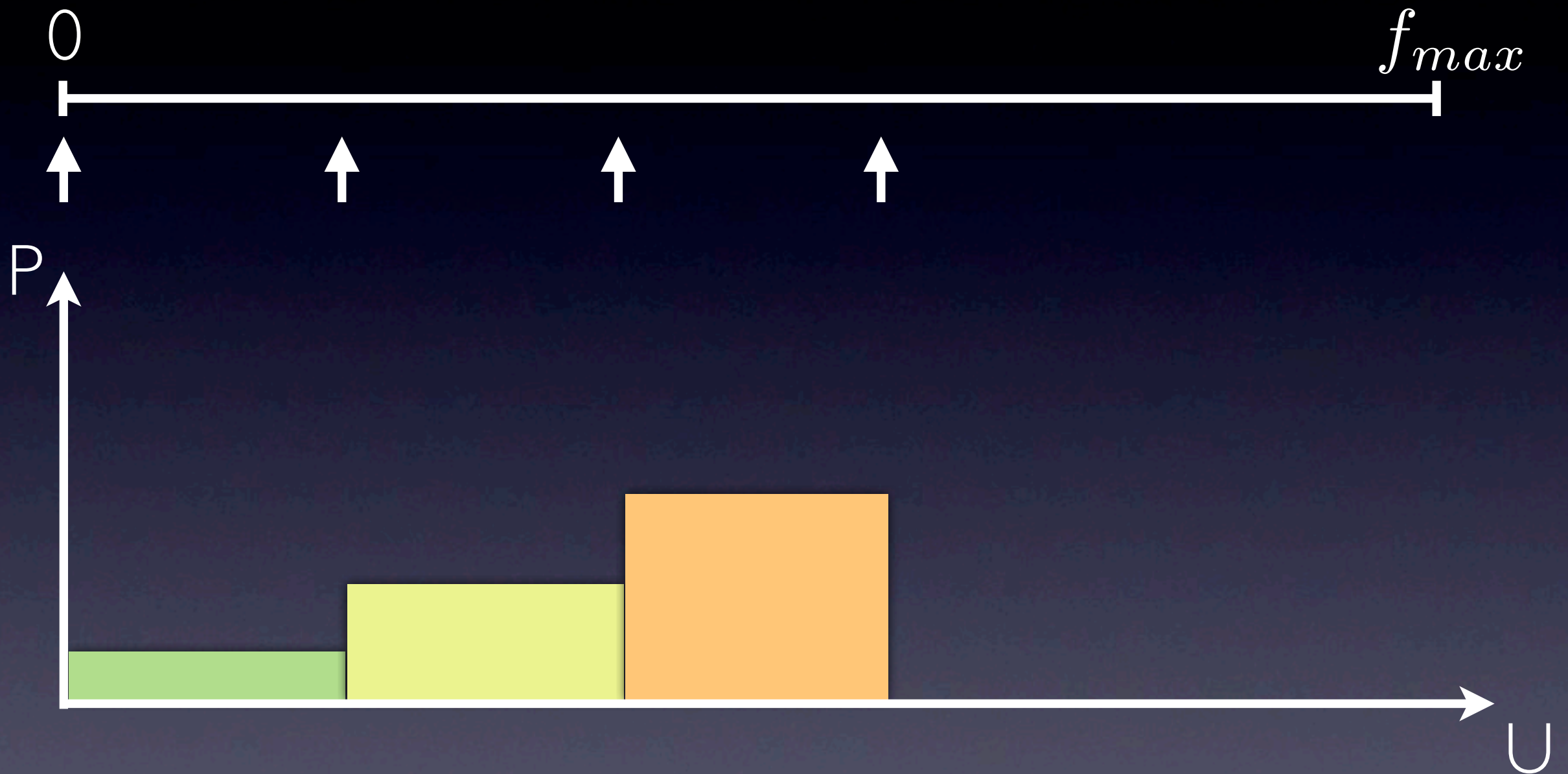


Discrete frequency levels



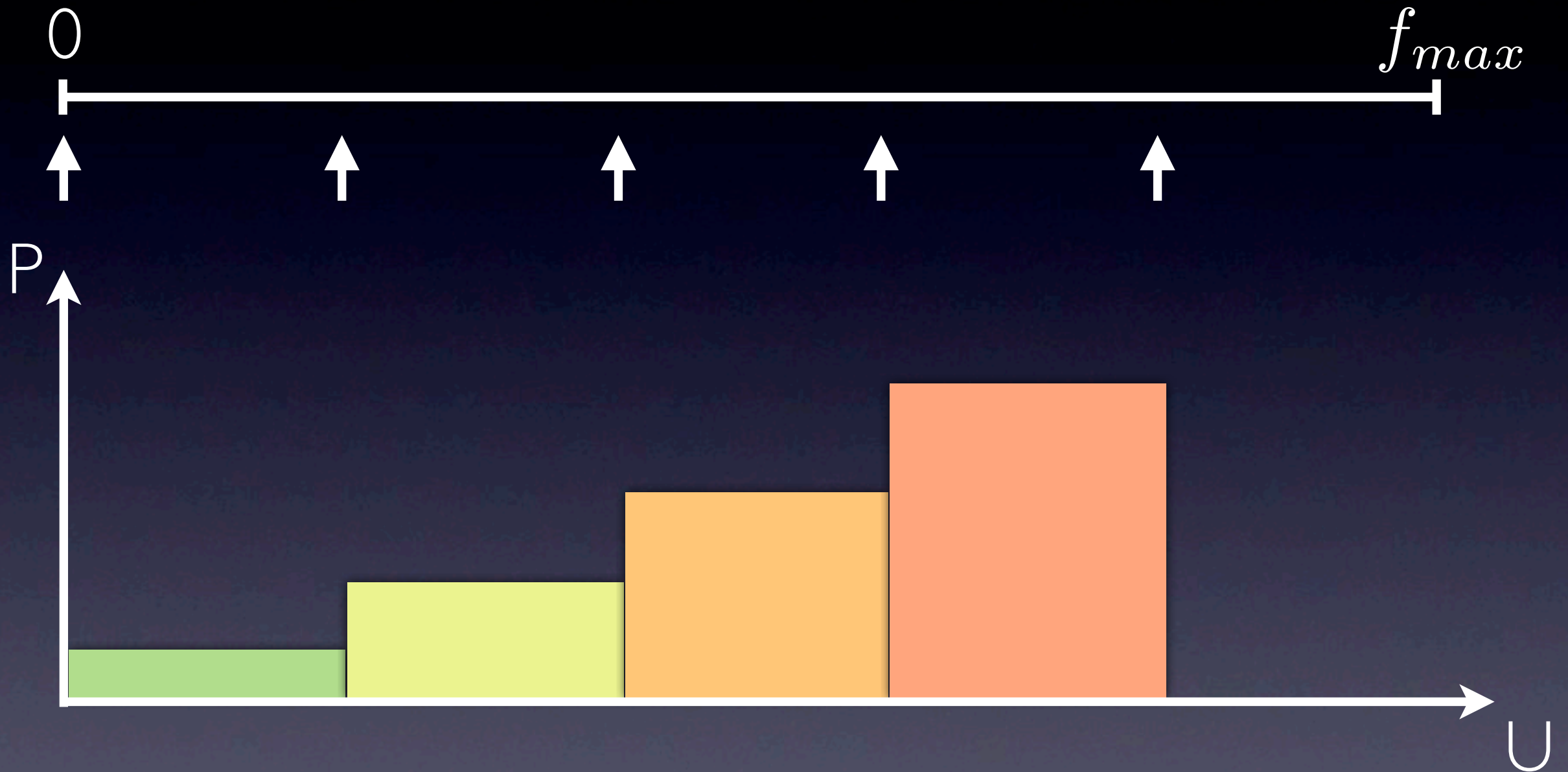


Discrete frequency levels



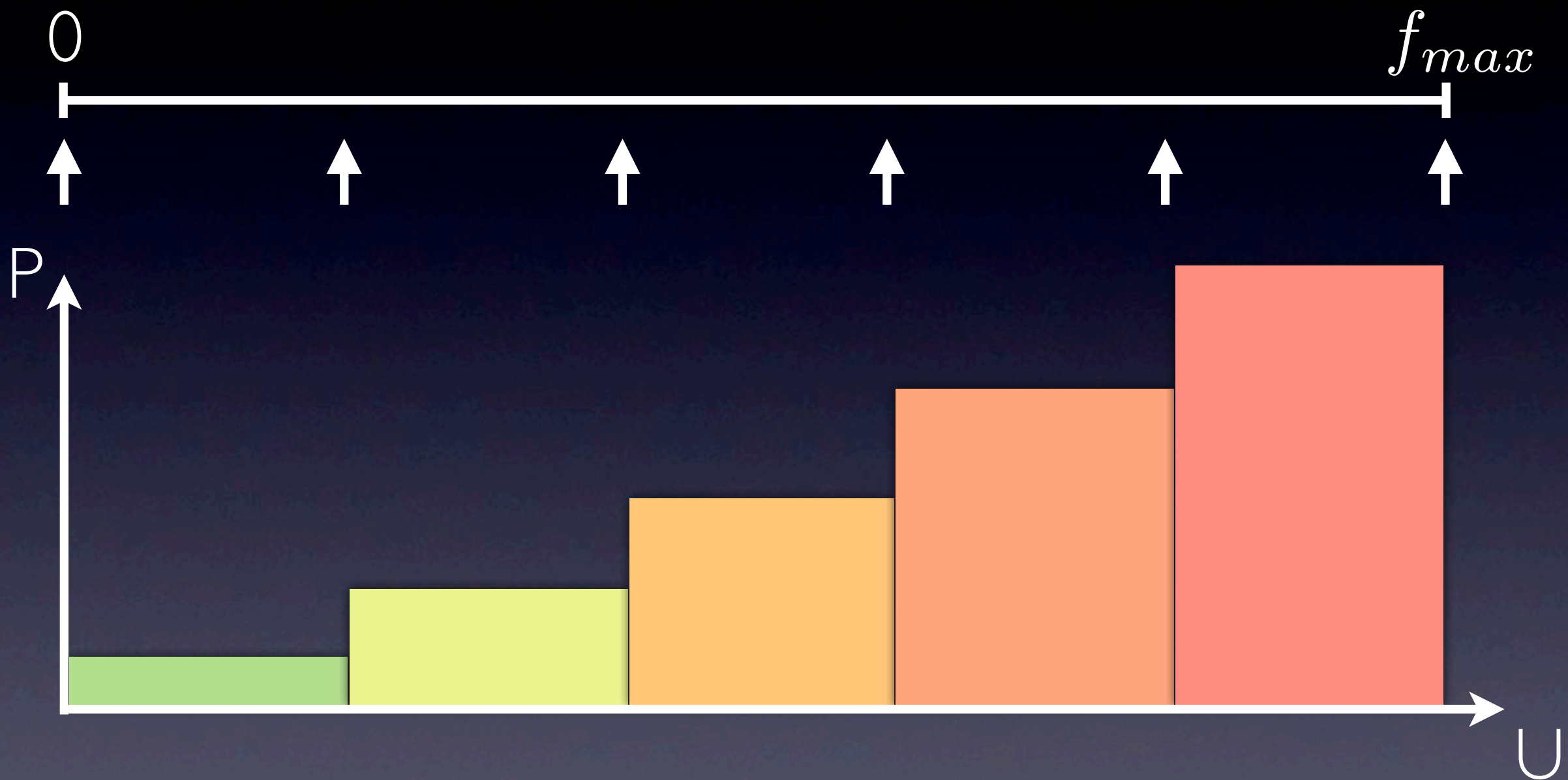


Discrete frequency levels



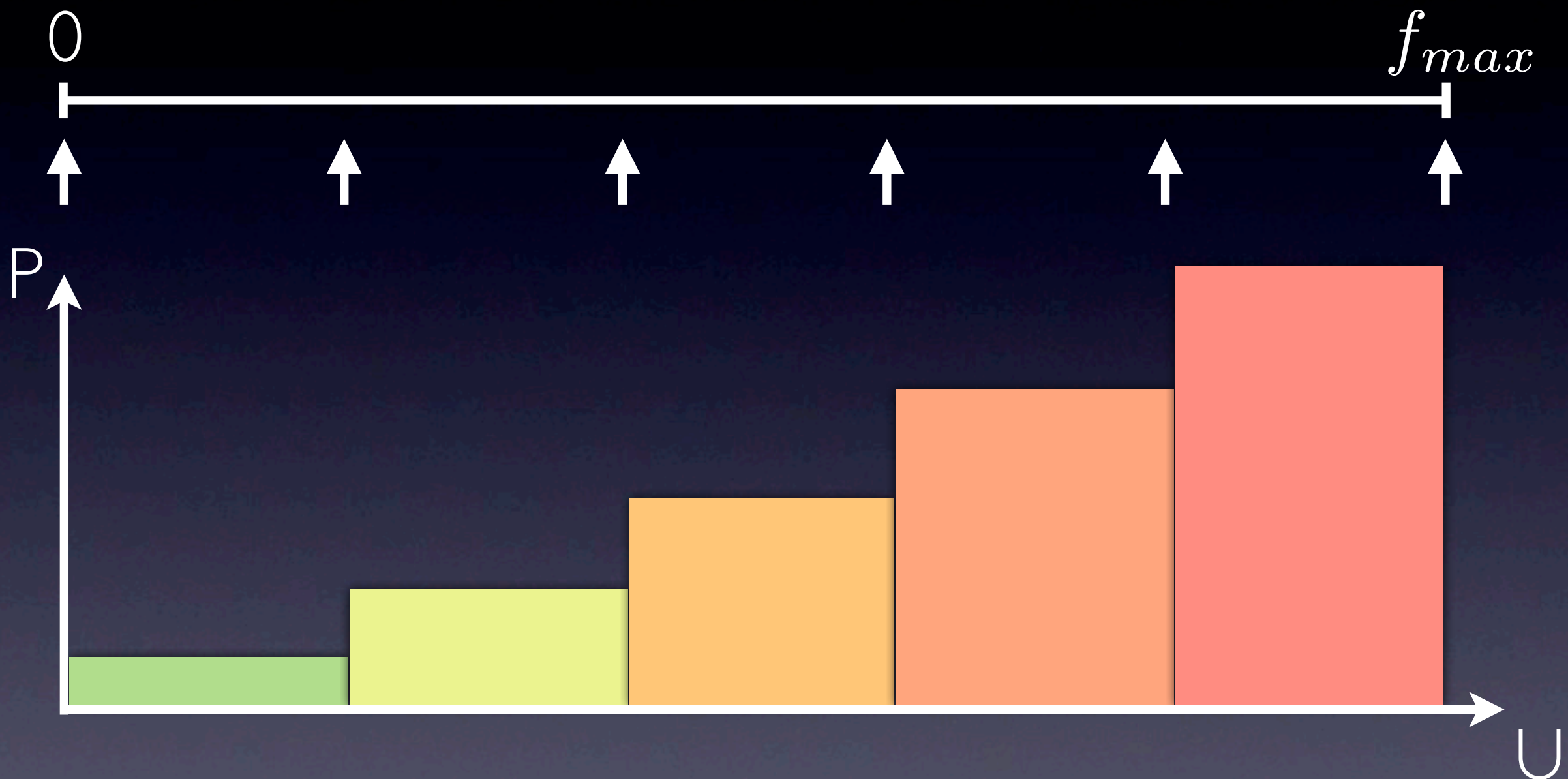


Discrete frequency levels





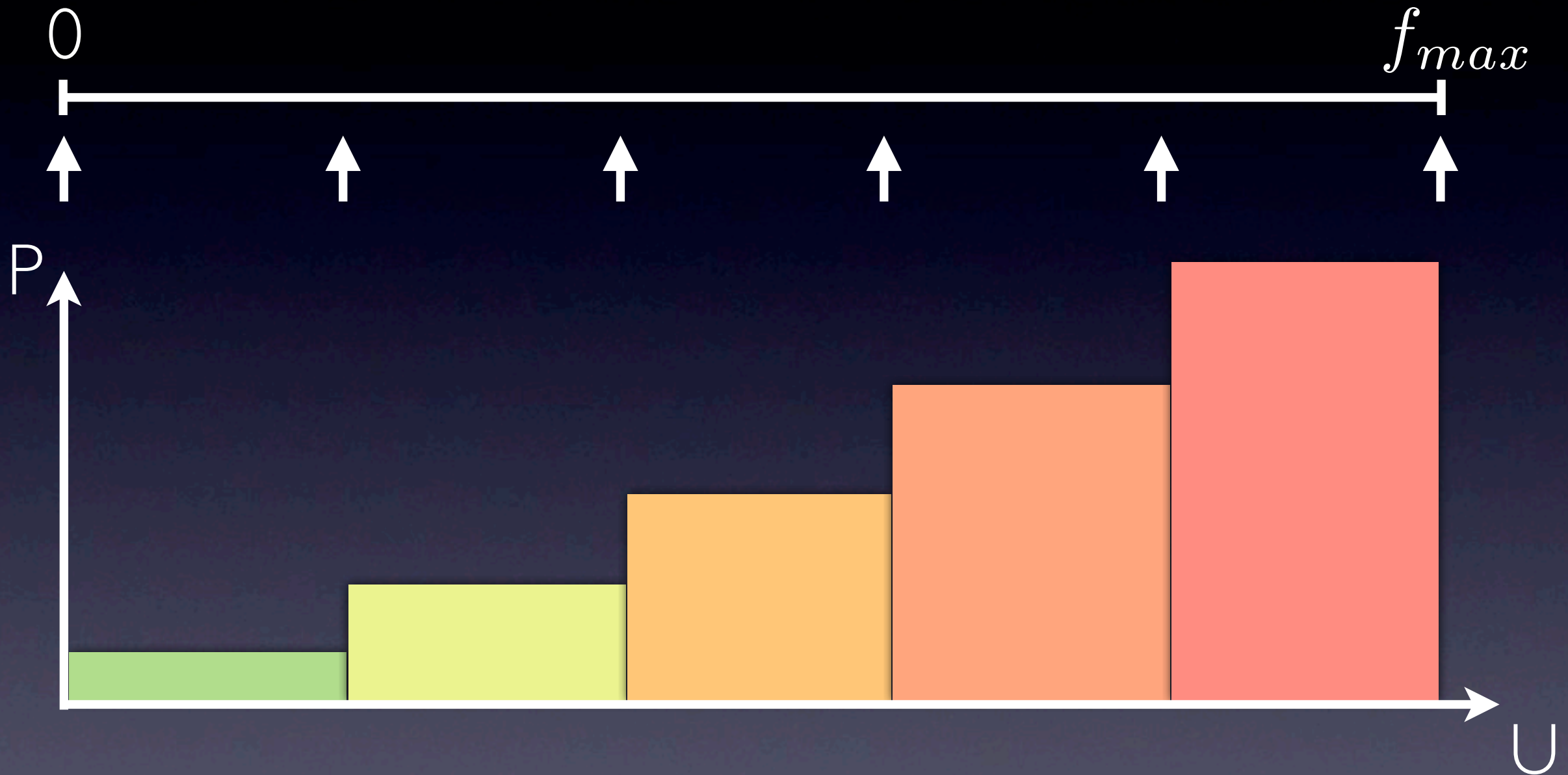
Discrete frequency levels



Minimum contribution of task i to the power consumption



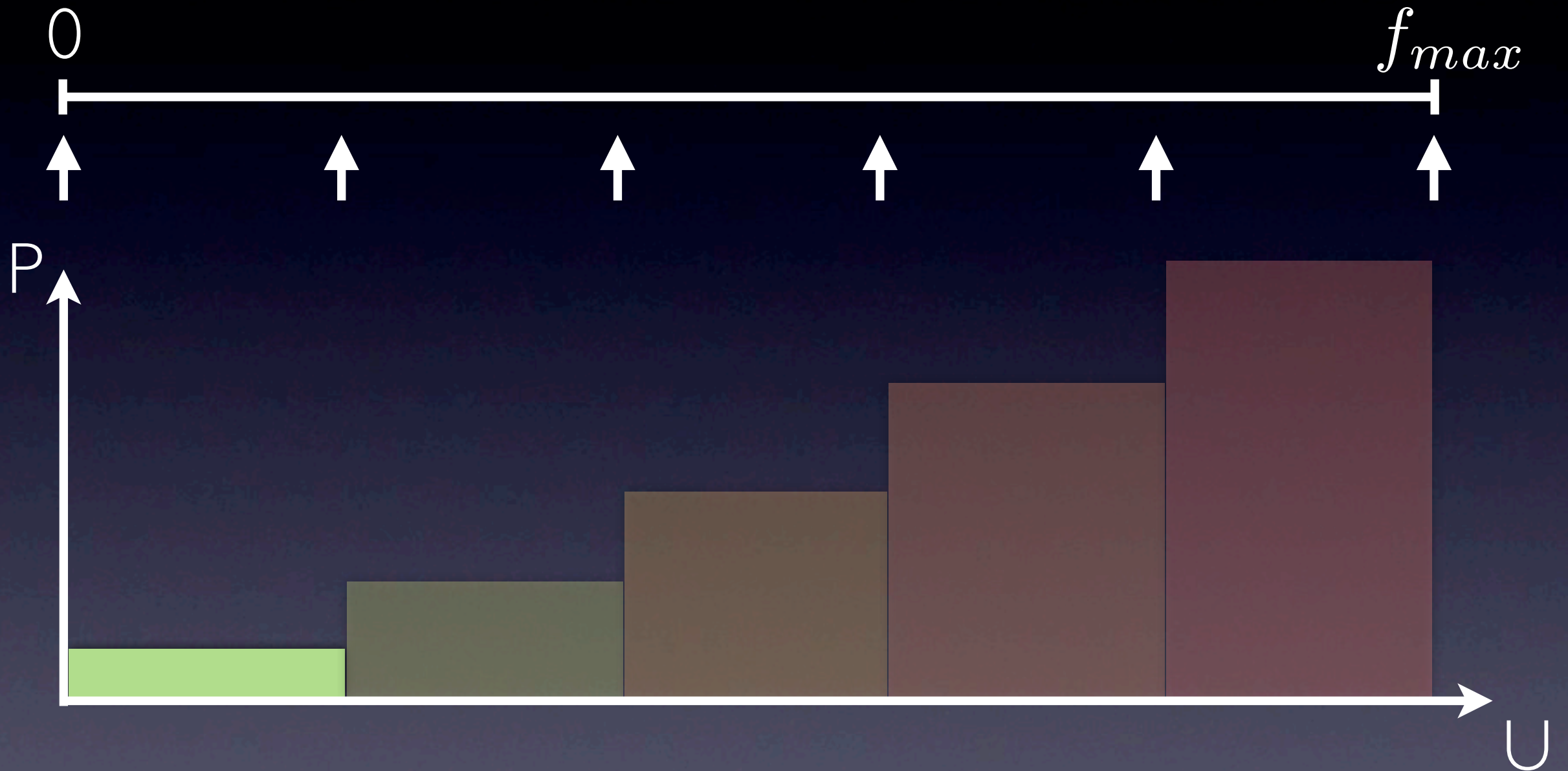
Discrete frequency levels



Minimum contribution of task i to the power consumption
Maximum contribution of task i to the power consumption

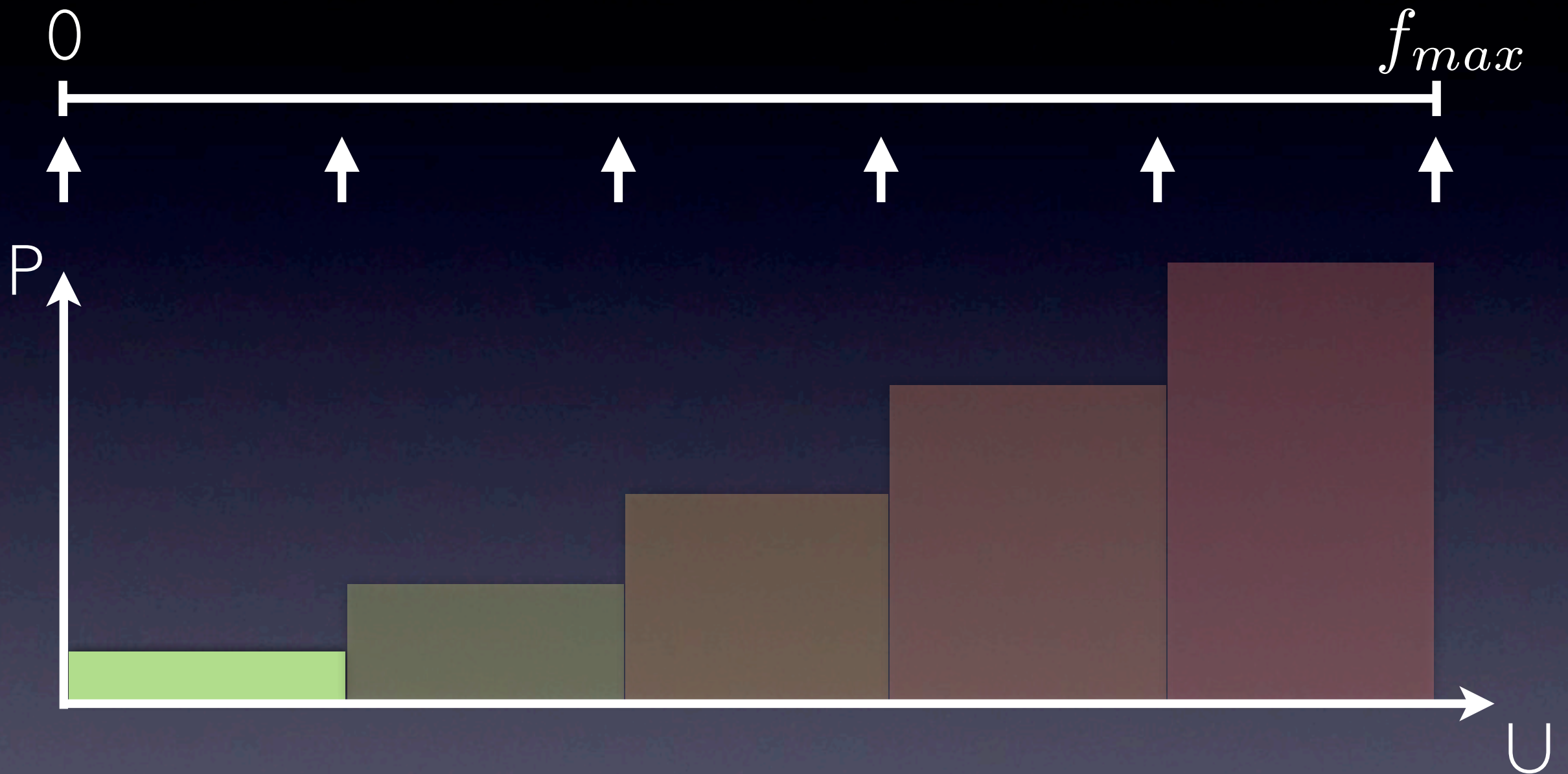


Minimum Contribution





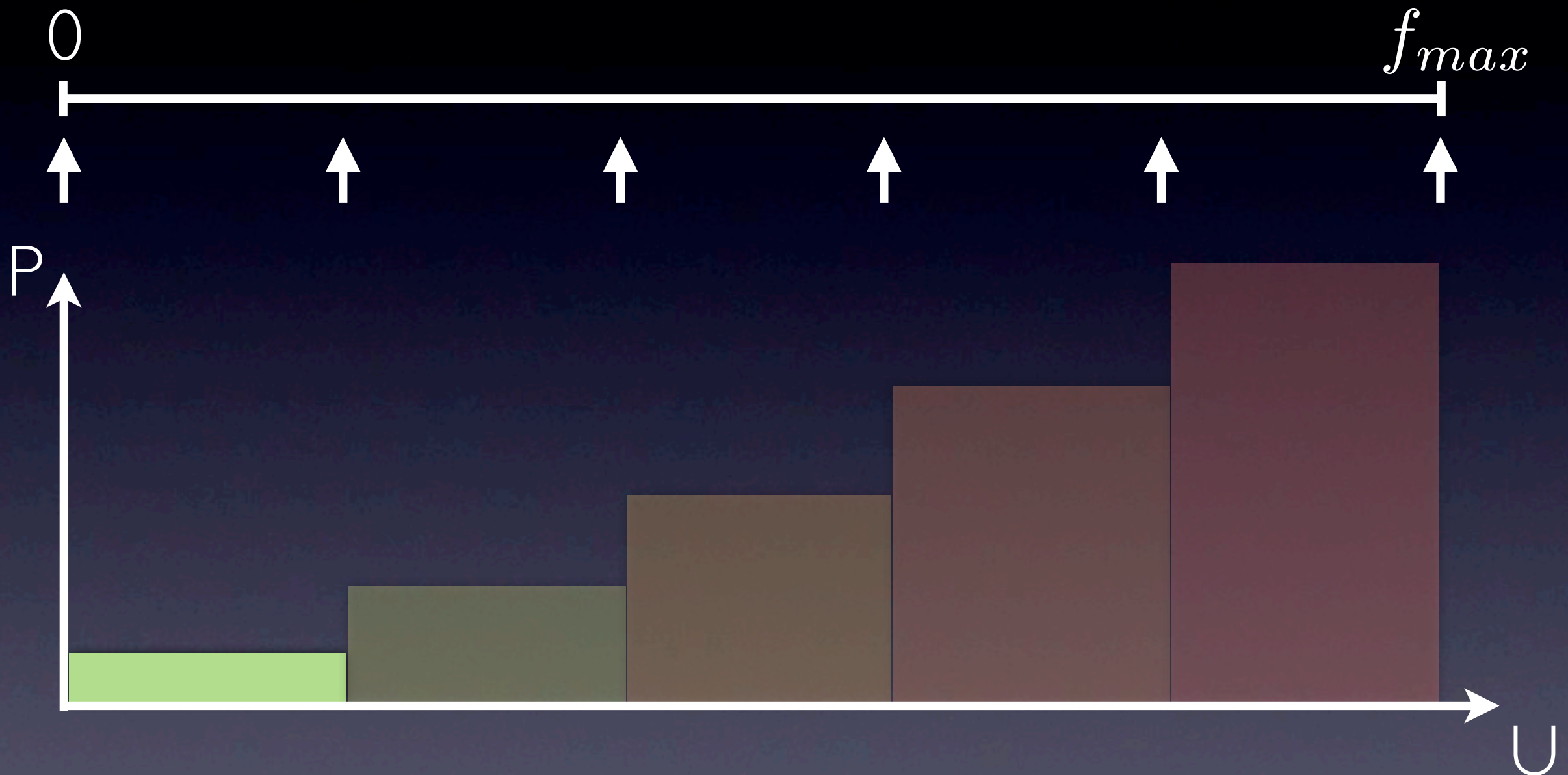
Minimum Contribution



Task i is the only task in the system



Minimum Contribution

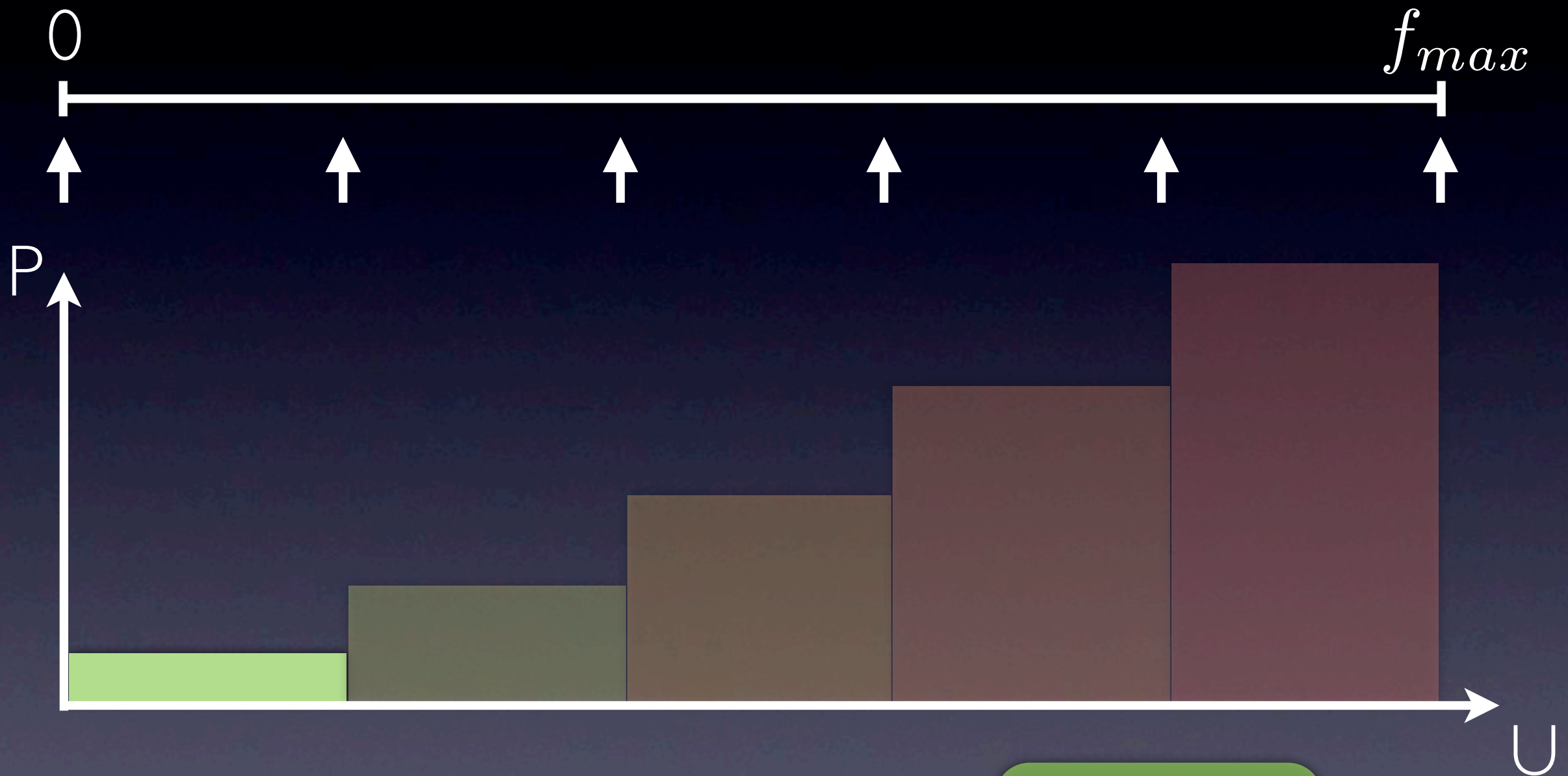


Task i is the only task in the system

$$bE_i^l = (t_1 - t_0)c_1 \frac{U_i}{\kappa_l} (\kappa_l f_{max})^\omega$$



Minimum Contribution

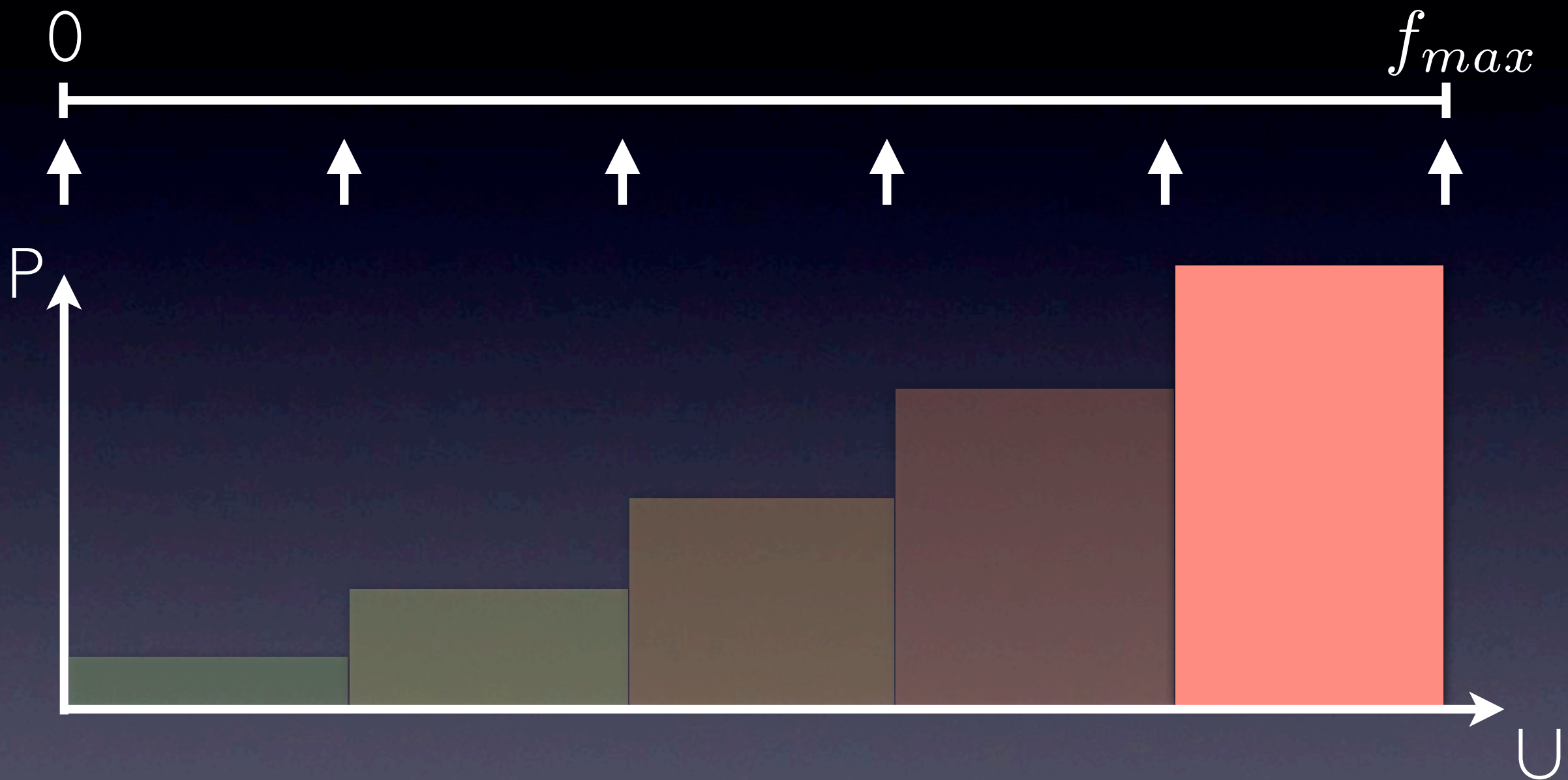


Task i is the only task in the system $\kappa_{l-1} < U_i \leq \kappa_l$

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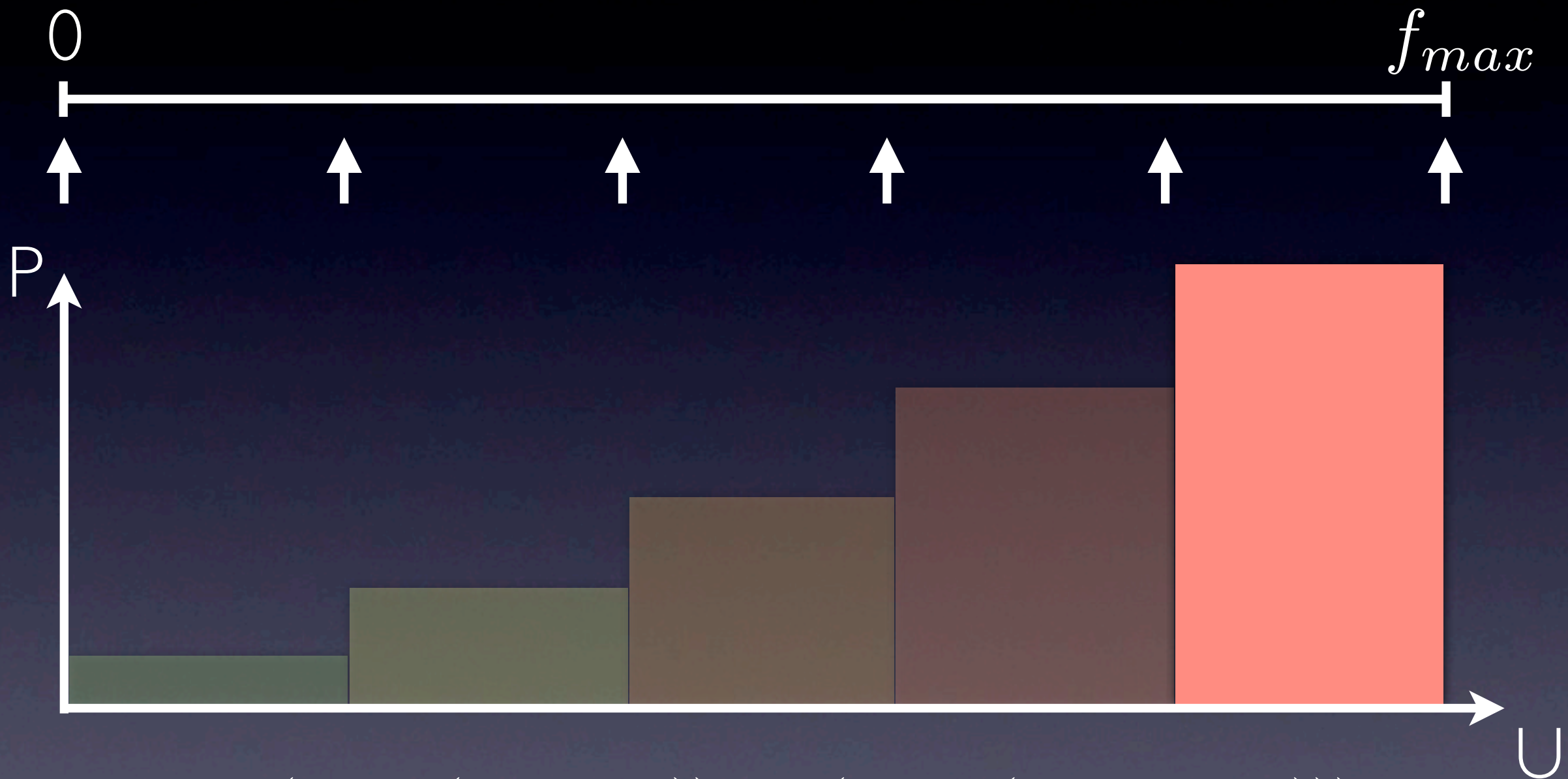


Maximum Contribution





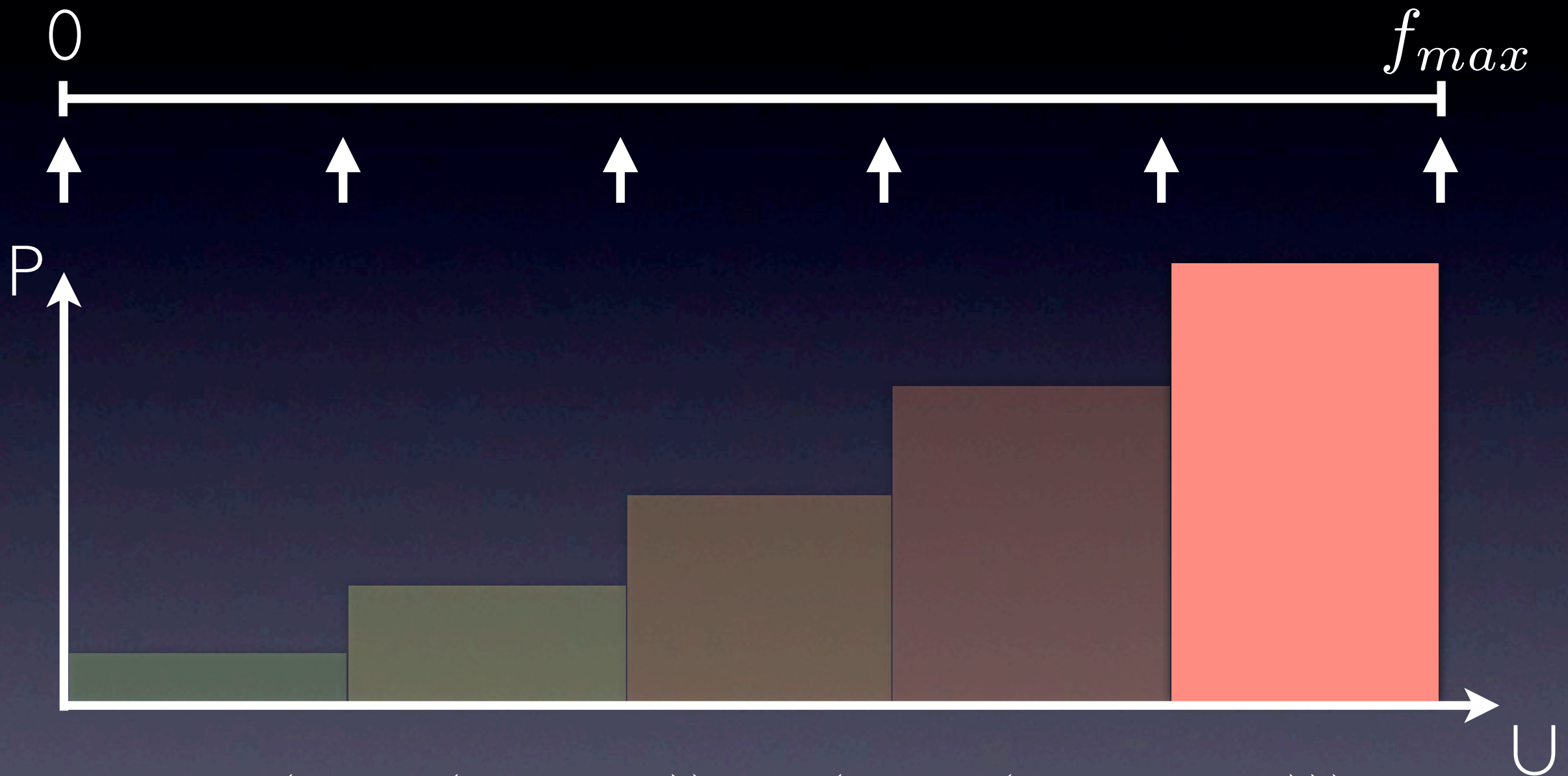
Maximum Contribution



$$E(1, \min(\kappa + U_i, 1)) - E(\kappa, \min(\kappa_{u-1}, \kappa_{m-2}))$$



Maximum Contribution

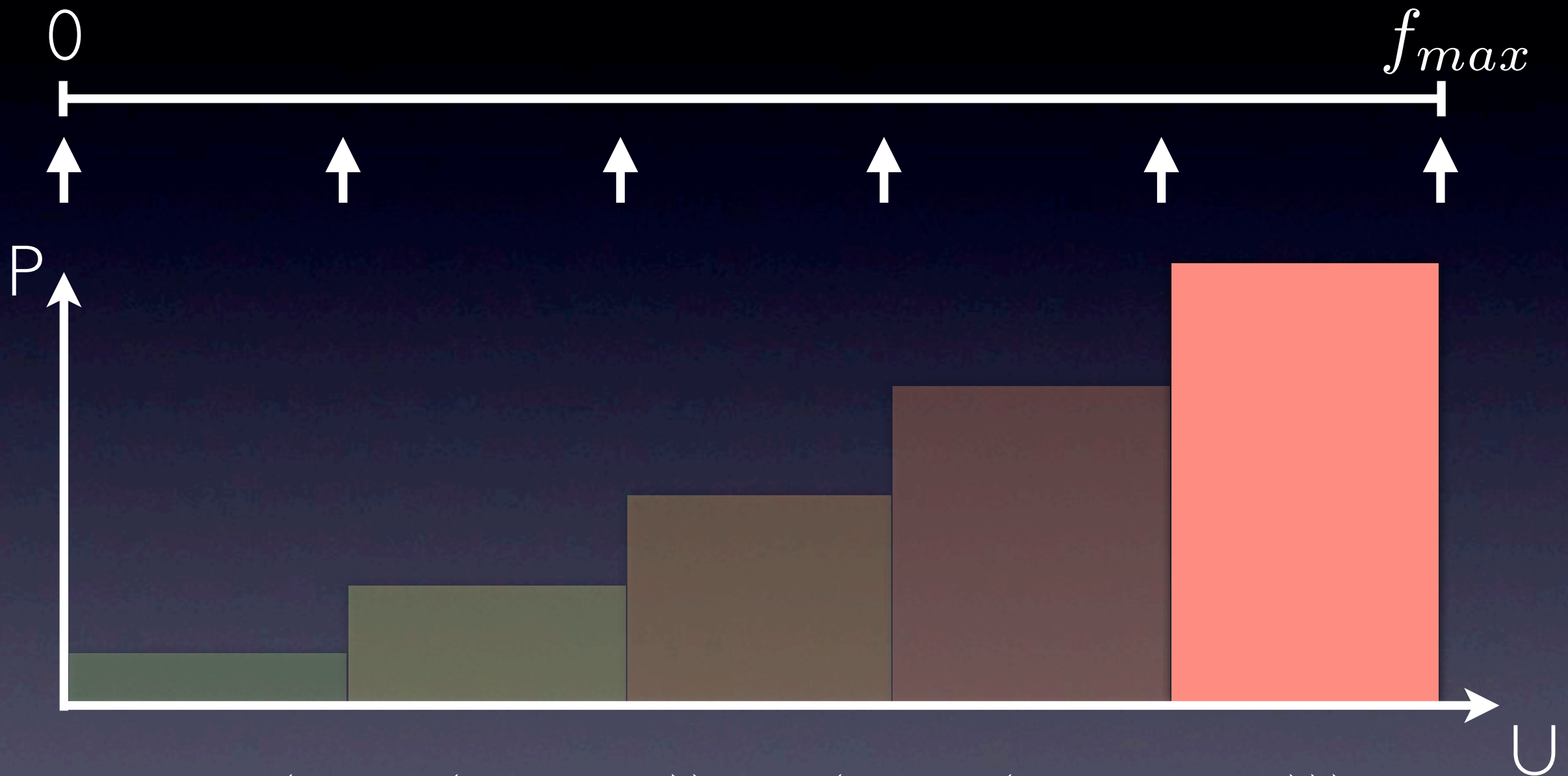


$$E(1, \min(\kappa + U_i, 1)) - E(\kappa, \min(\kappa_{u-1}, \kappa_{m-2}))$$

$$\kappa = \min(\kappa_u, \kappa_{m-1})$$



Maximum Contribution



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$$\kappa = \min(\kappa_u, \kappa_{m-1})$$

$$\kappa_{u-1} < 1 - U_i \leq \kappa_u$$



Discrete Frequencies - Bounds

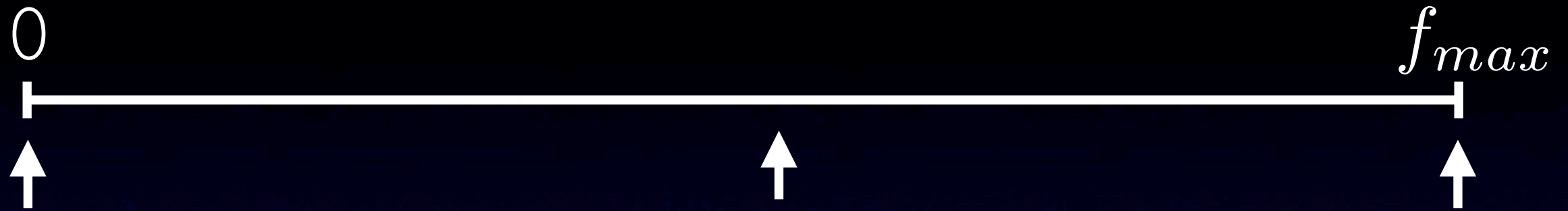


$$bE_i^u = (t_1 - t_0)c_1 f_{max}^\omega (\min(\kappa + U_i, 1) - \kappa^\omega \max(1 - \frac{U_i}{\kappa}, \min(\kappa_{u-1}, \kappa_{m-2})))$$

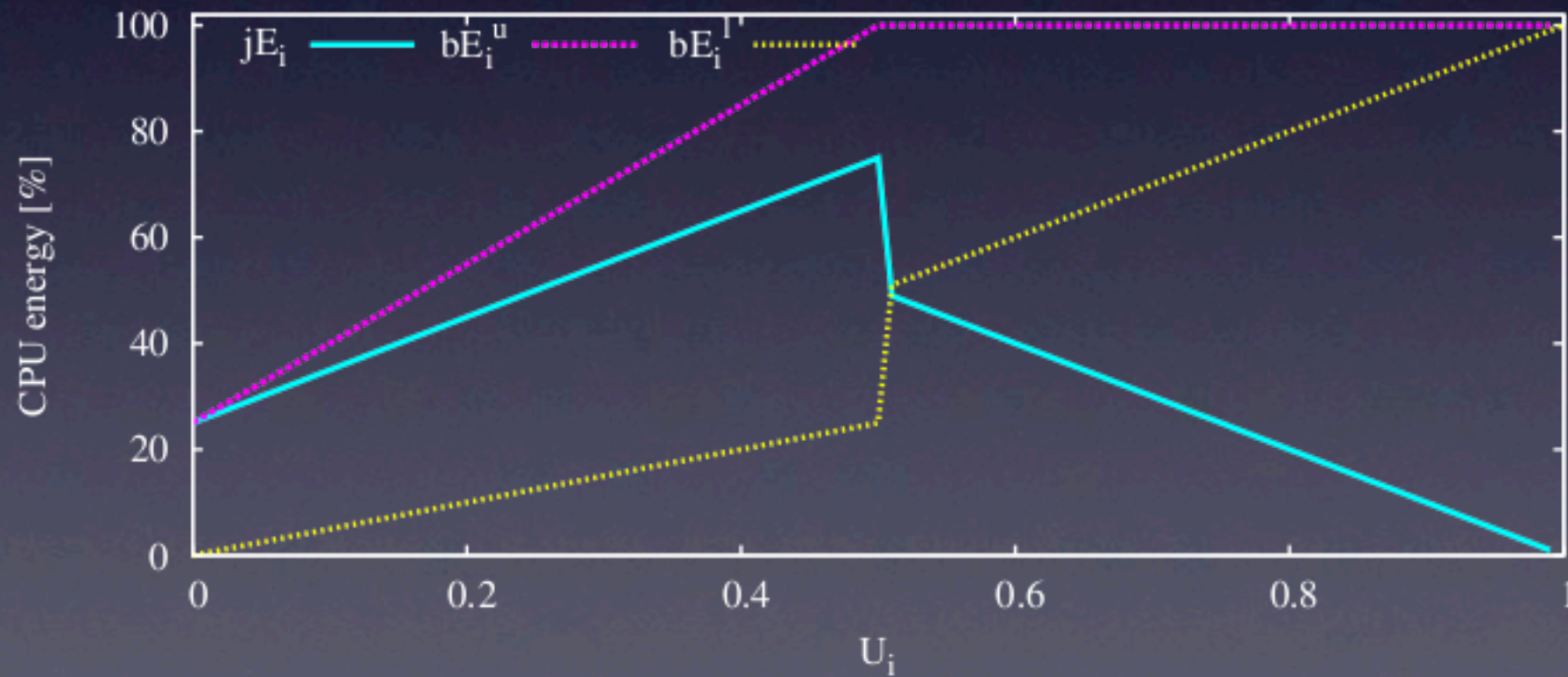
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3 discrete frequencies - bounds

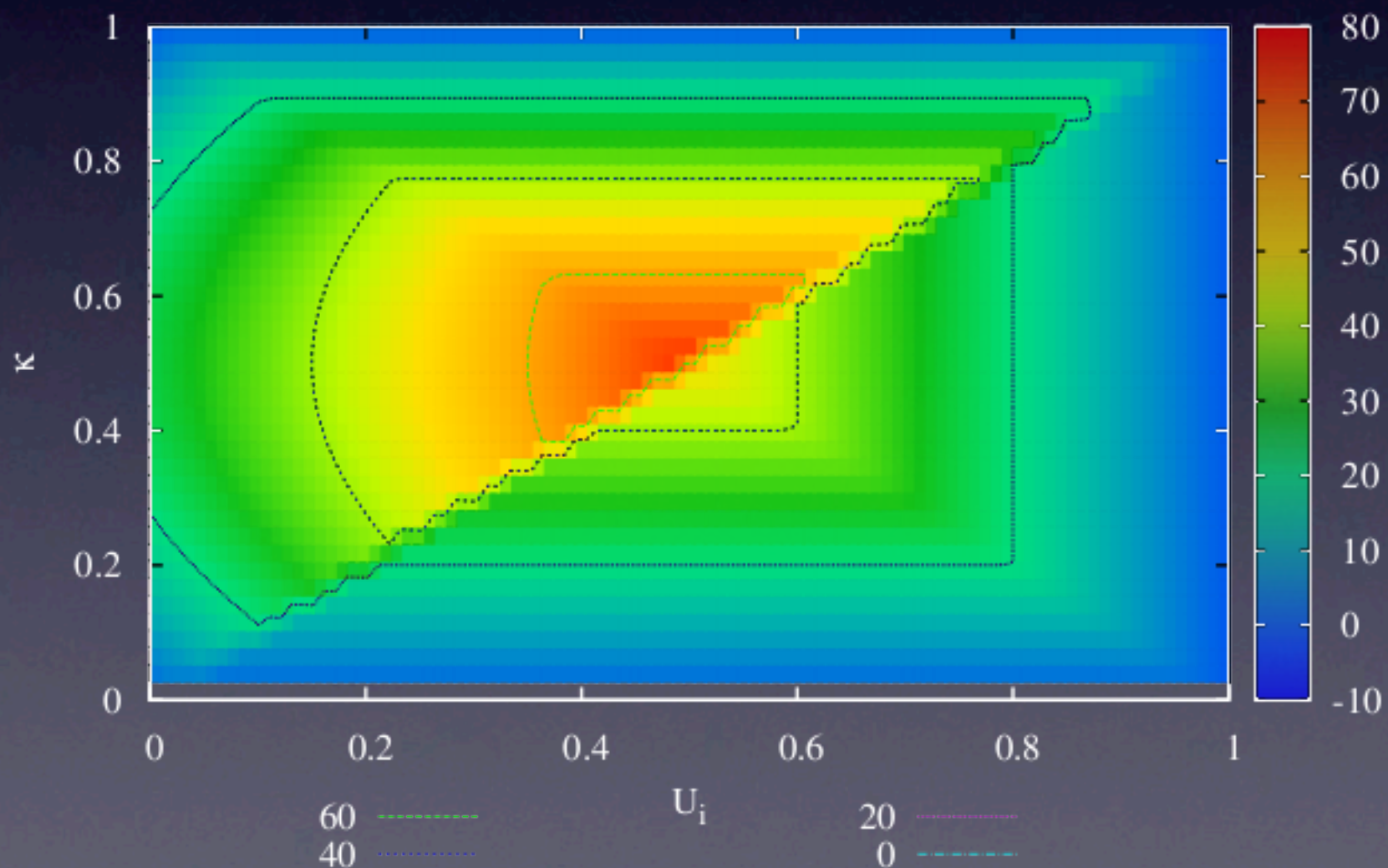
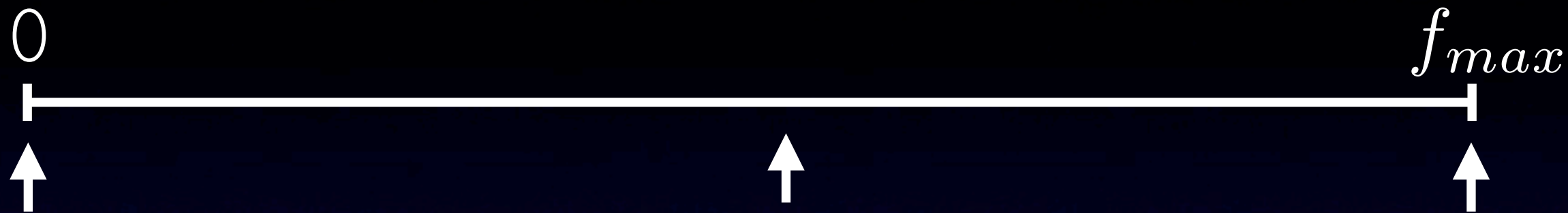


$t_0 = 0s, t_1 = 10s, c_1 = 1520 \text{ mWatt}, \omega = 2, \kappa = 0.0, 0.5, 1.0$





3 discrete frequencies - jitter

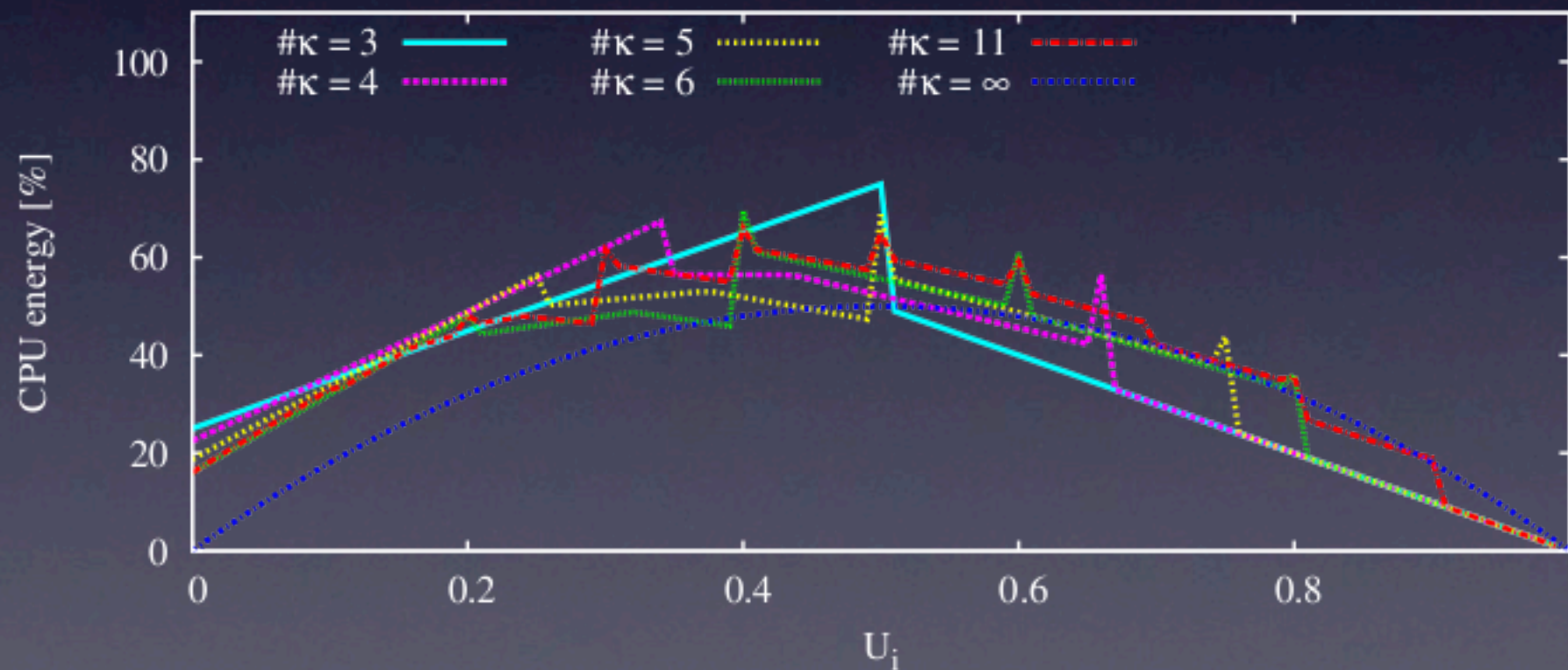




Discrete Frequencies - Jitter



$t_0 = 0s, t_1 = 10s, c_1 = 1520 \text{ mWatt}, \omega = 2$





Cost of power isolation



Cost of power isolation

Difference between the optimal and actual power consumption



Cost of power isolation

Difference between the optimal and actual power consumption

Optimal is achieved with infinite frequency levels



Cost of power isolation

Difference between the optimal and actual power consumption

Optimal is achieved with infinite frequency levels

The cost of power isolation depends on

- the sum of task utilizations
- the utilization of the considered task
- the number of available frequency levels
- the distribution of the frequency levels in the interval $[0, f_{\max}]$



Cost of power isolation

Difference between the optimal and actual power consumption

Optimal is achieved with infinite frequency levels

The cost of power isolation depends on

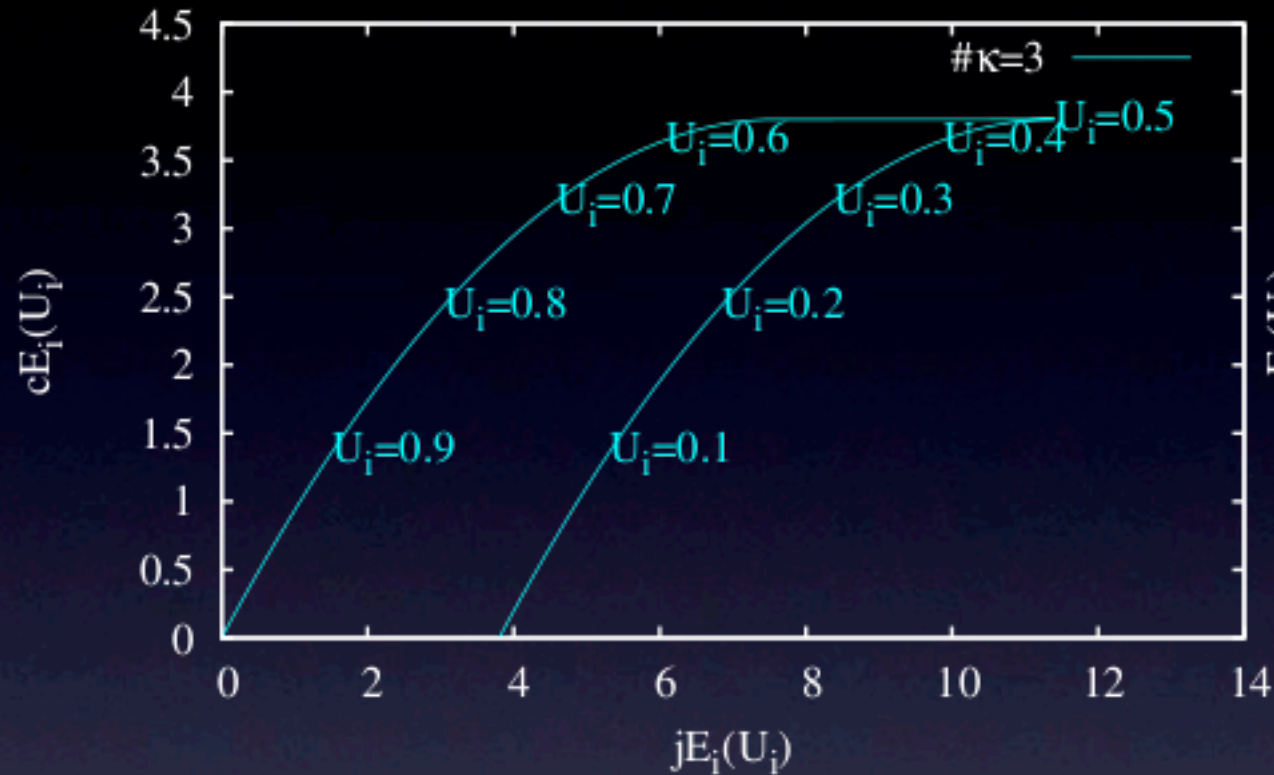
- the sum of task utilizations
- the utilization of the considered task
- the number of available frequency levels
- the distribution of the frequency levels in the interval $[0, f_{max}]$

$$cE_i = (t_1 - t_0)c_1 f_{max}^\omega U_i (1 - U_i^{\omega-1})$$

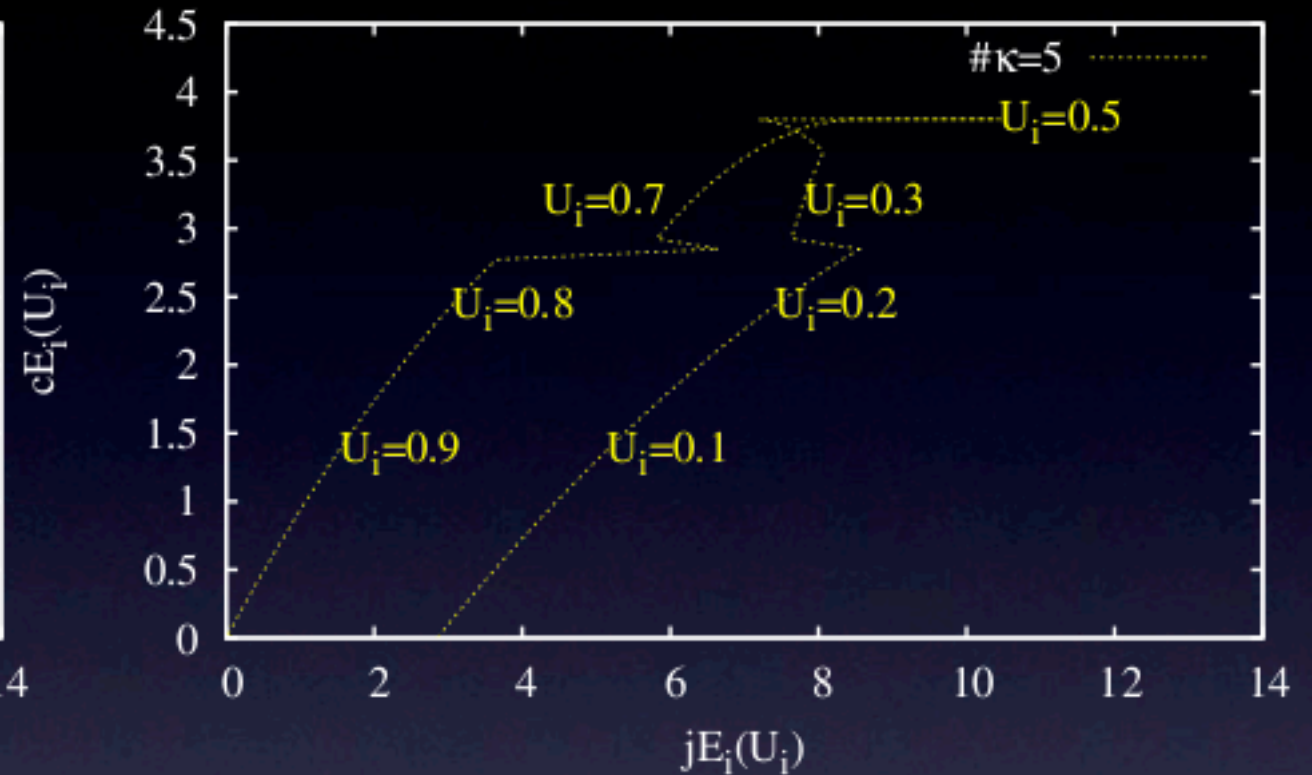


Cost of power isolation

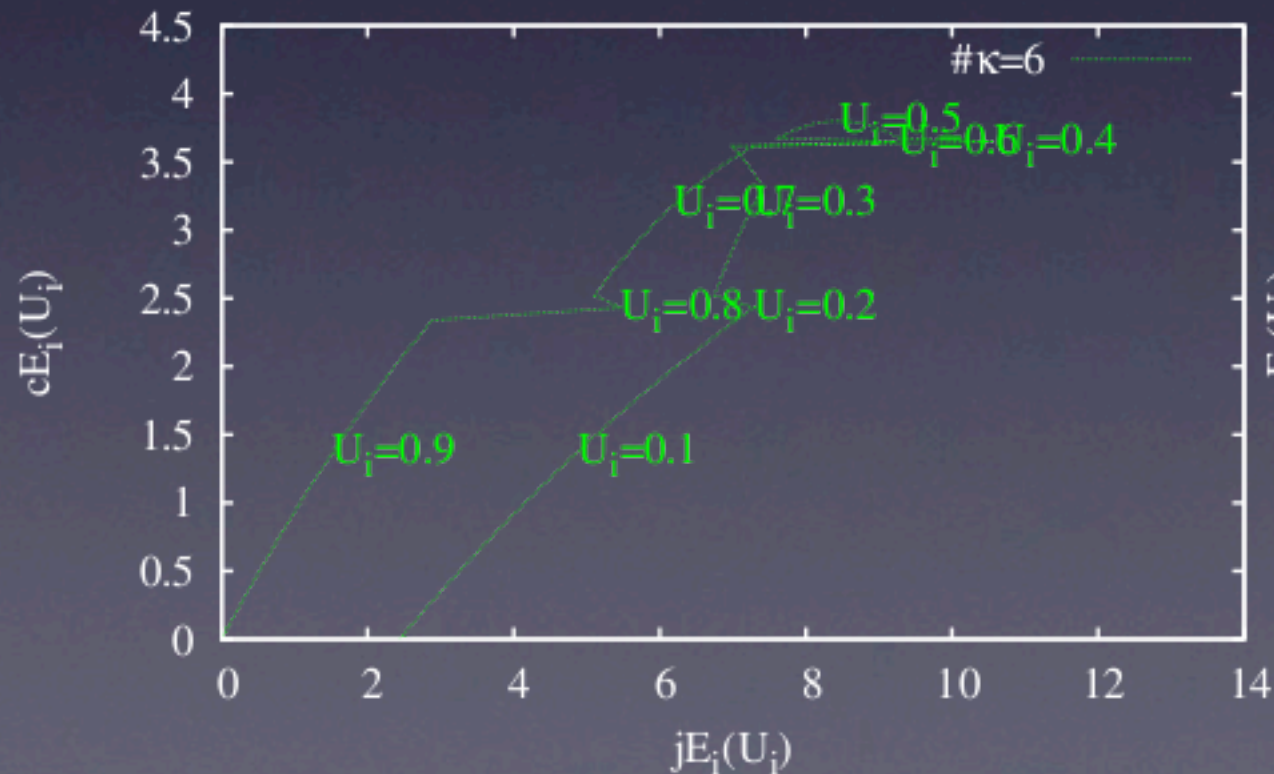
$t_0 = 0s, t_1 = 10s, c_1 = 1520 \text{ mWatt}, \omega = 2$



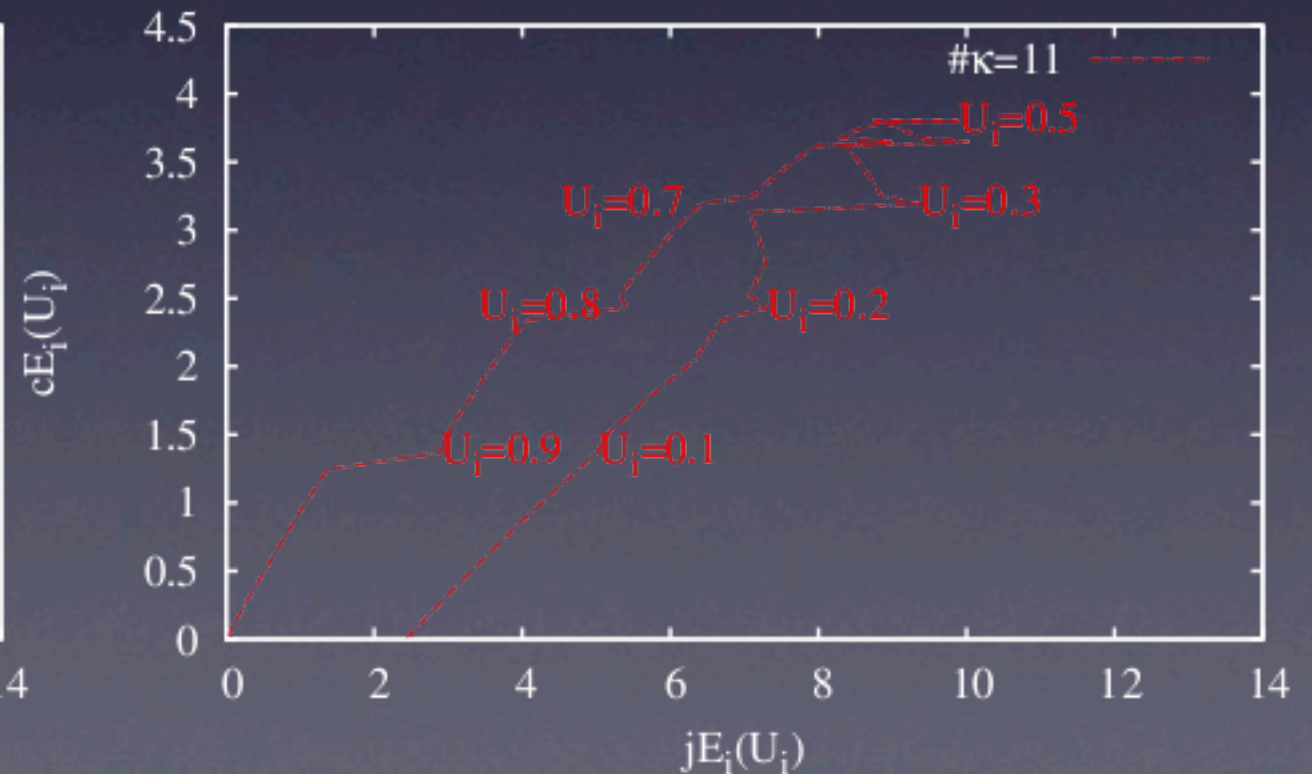
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$t_0 = 0s, t_1 = 10s, c_1 = 1520 \text{ mWatt}, \omega = 2$



$t_0 = 0s, t_1 = 10s, c_1 = 1520 \text{ mWatt}, \omega = 2$





Conclusion



Conclusion

Lower and upper bounds on the individual power consumption



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Lower and upper bounds on the individual power consumption

Quality of power isolation



Conclusion

Lower and upper bounds on the individual power consumption

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Cost of power isolation



Conclusion

Lower and upper bounds on the individual power consumption

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Full temporal [Craciunas12], spatial [Craciunas08], and power isolation of tasks



Conclusion

Lower and upper bounds on the individual power consumption

Quality of power isolation

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Full temporal [Craciunas12], spatial [Craciunas08], and power isolation of tasks

The key insight is that there appears to be a fundamental trade-off between quality and cost of time, space, and power isolation



Thank you

[Abeni04] L. Abeni and G. C. Buttazzo, “Resource reservation in dynamic realtime systems,” *Real-Time Syst.*, vol. 27, no. 2, pp. 123–167, 2004.

[Craciunas08] S. S. Craciunas, C. M. Kirsch, H. Payer, A. Sokolova, R. Staudinger, and H. Stadler, “A compacting real-time memory management system,” *USENIX*, 2008.

[Craciunas12] S. S. Craciunas, C. M. Kirsch, H. Payer, H. Rock, and A. Sokolova, “Temporal isolation in real-time systems: The VBS approach,” *Journal on Software Tools for Technology Transfer*, Springer, 2012.

[Liu and Layland73] C. L. Liu and J. W. Layland, “Scheduling algorithms for multiprogramming in a hard-real-time environment,” *Journal of the ACM*, vol. 20, pp. 46–61, 1973.

[Pillai01] P. Pillai and K. G. Shin, “Real-time dynamic voltage scaling for low power embedded operating systems,” in *Proc. SOSP*. ACM, 2001.

[Mosse05] R. Xu, D. Mosse, and R. Melhem, “Minimizing expected energy in real-time embedded systems,” in *Proc. EMSOFT*. ACM, 2005.

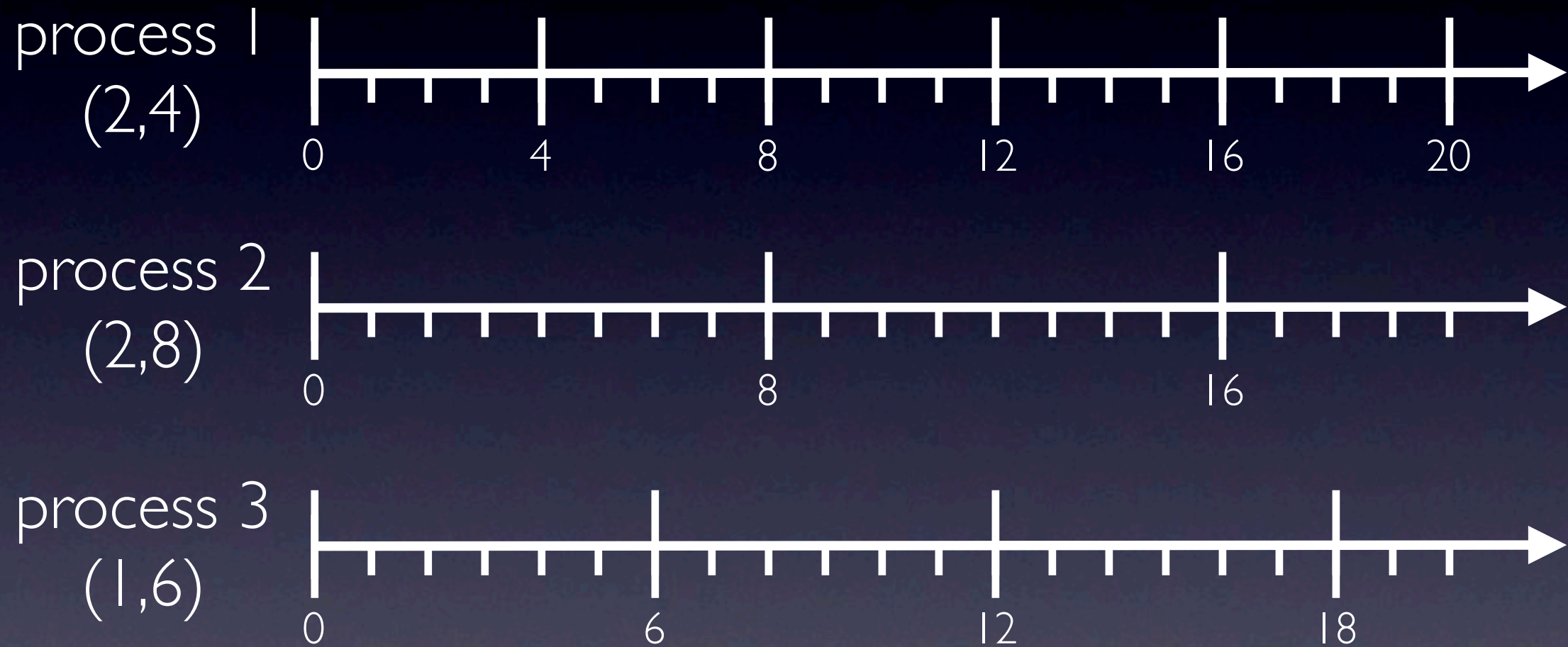
[Chen08] J.-J. Chen and L. Thiele, “Expected system energy consumption minimization in leakage-aware DVS systems,” in *Proc. ISLPED*. ACM, 2008.

[Pathak11] A. Pathak, Y. C. Hu, M. Zhang, V. Bahl, and Y.-M. Wang, “Fine-grained power modeling for smartphones using system call tracing,” in *Proc. Eurosys*. ACM, 2011.

[Cao08] Q. Cao, D. Fesehaye, N. Pham, Y. Sarwar, and T. Abdelzaher, “Virtual battery: An energy reserve abstraction for embedded sensor networks,” in *Proc. RTSS*. IEEE, 2008.



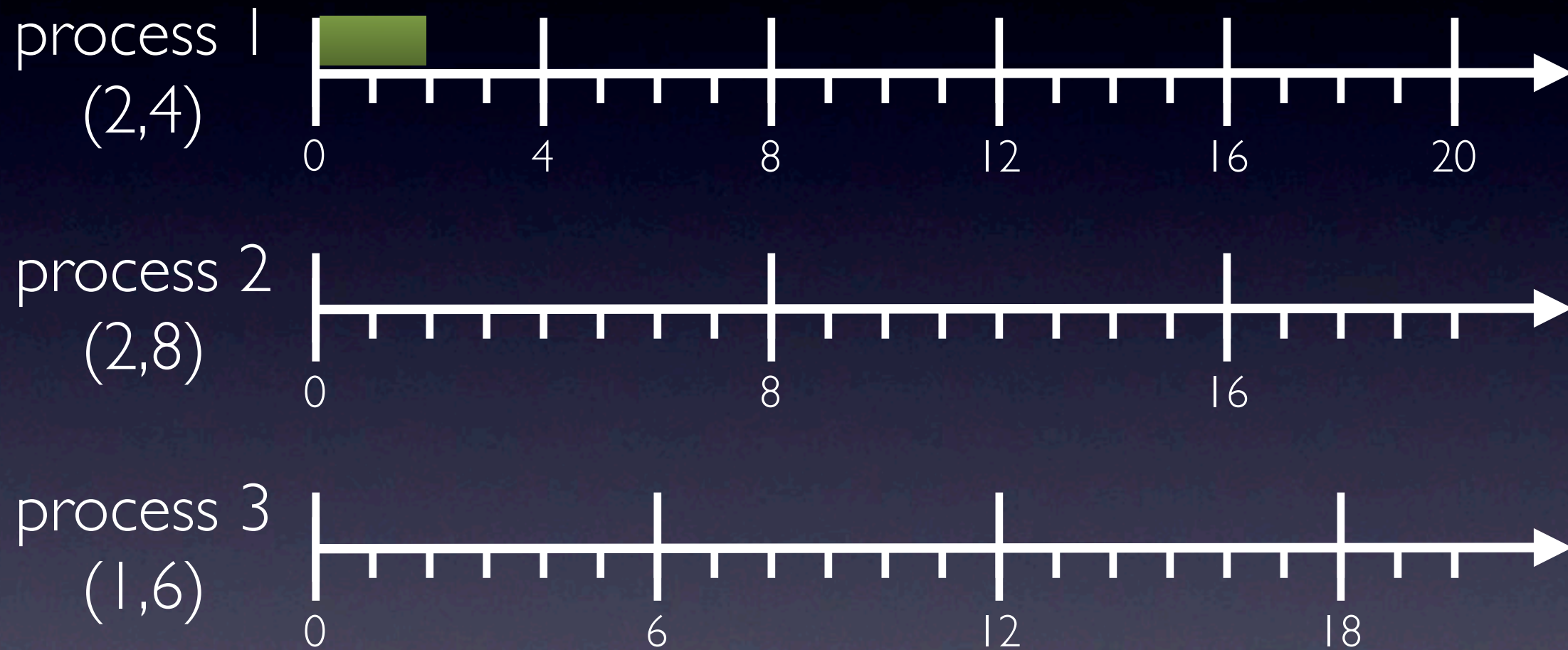
EDF



[Liu and Layland73]



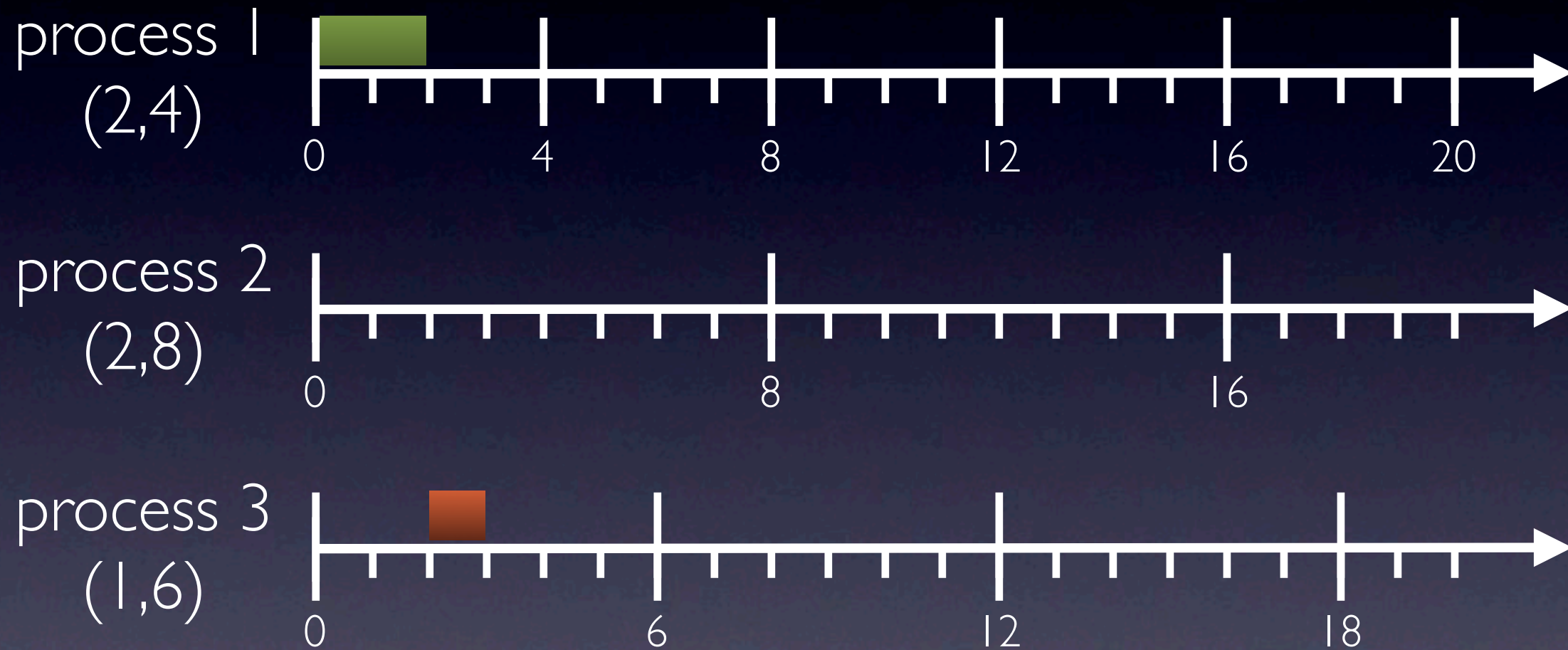
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[Liu and Layland73]



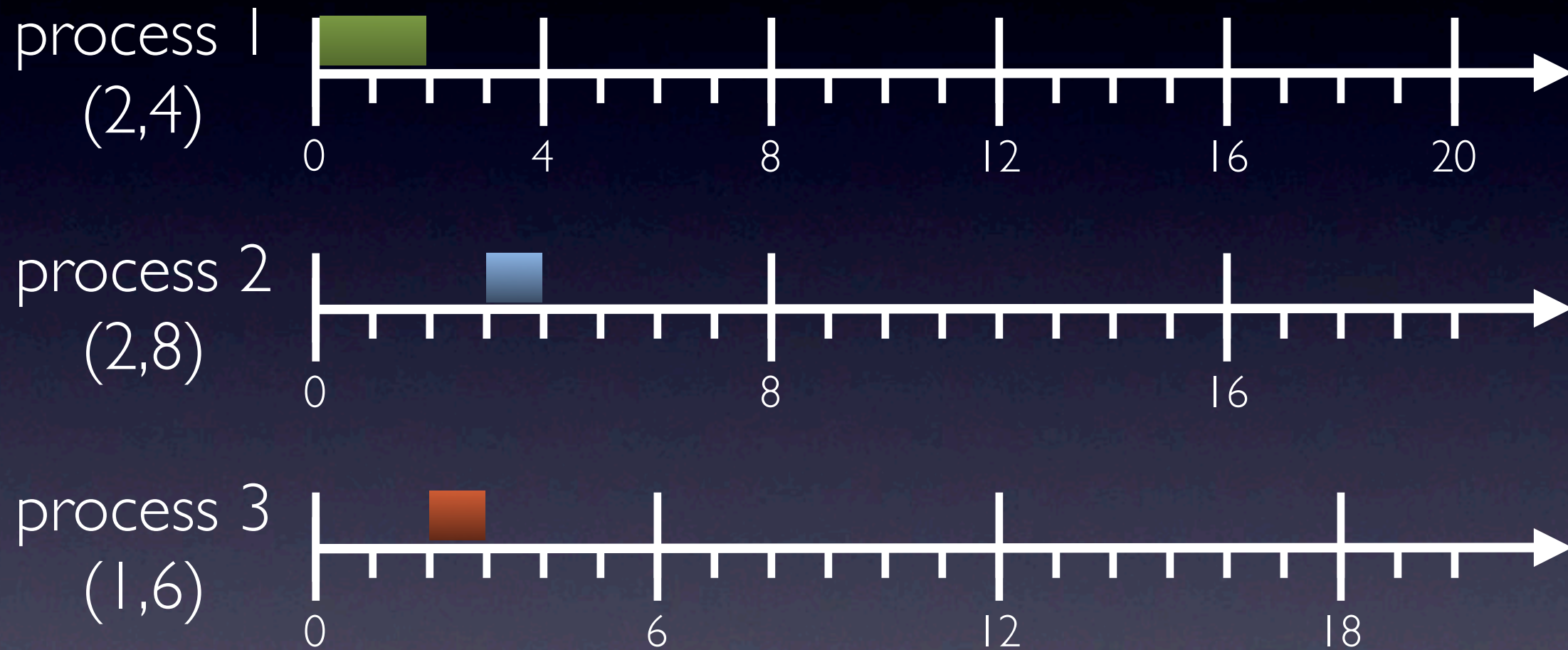
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[Liu and Layland73]



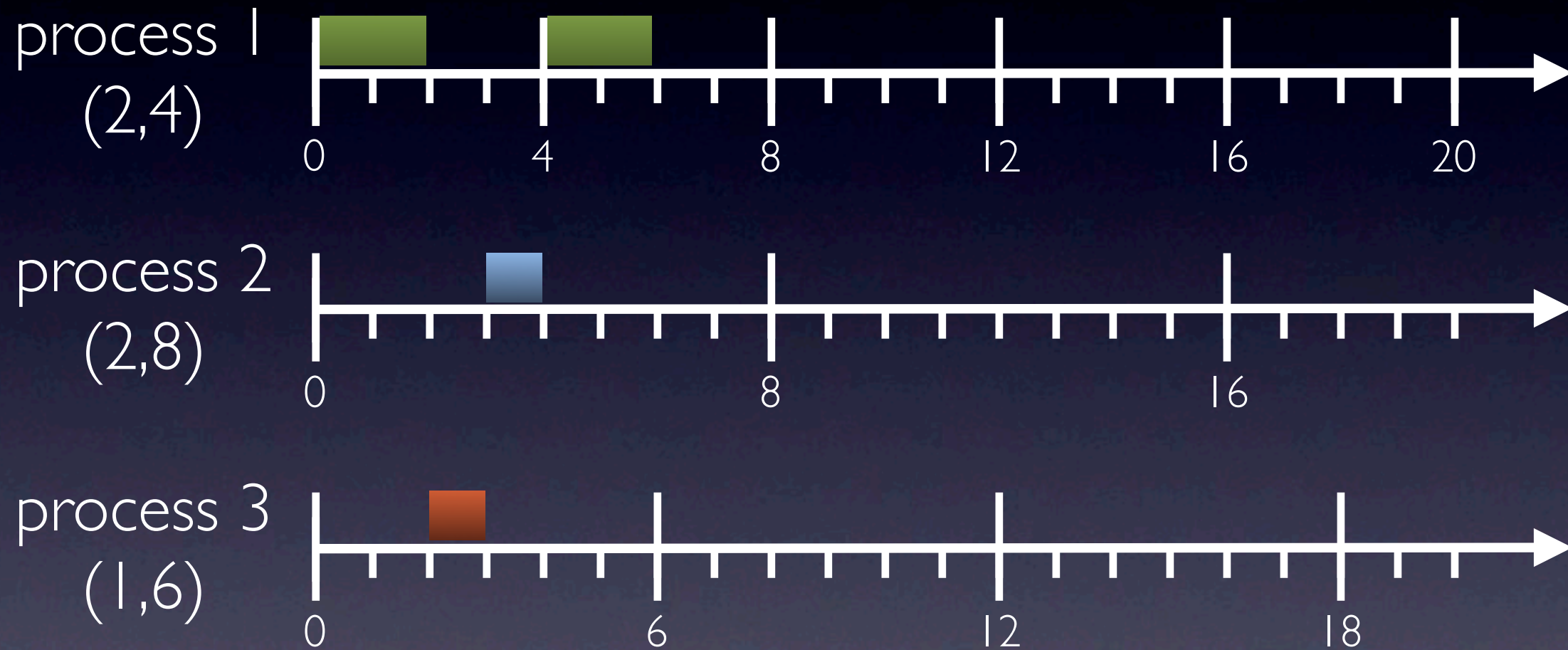
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[Liu and Layland73]



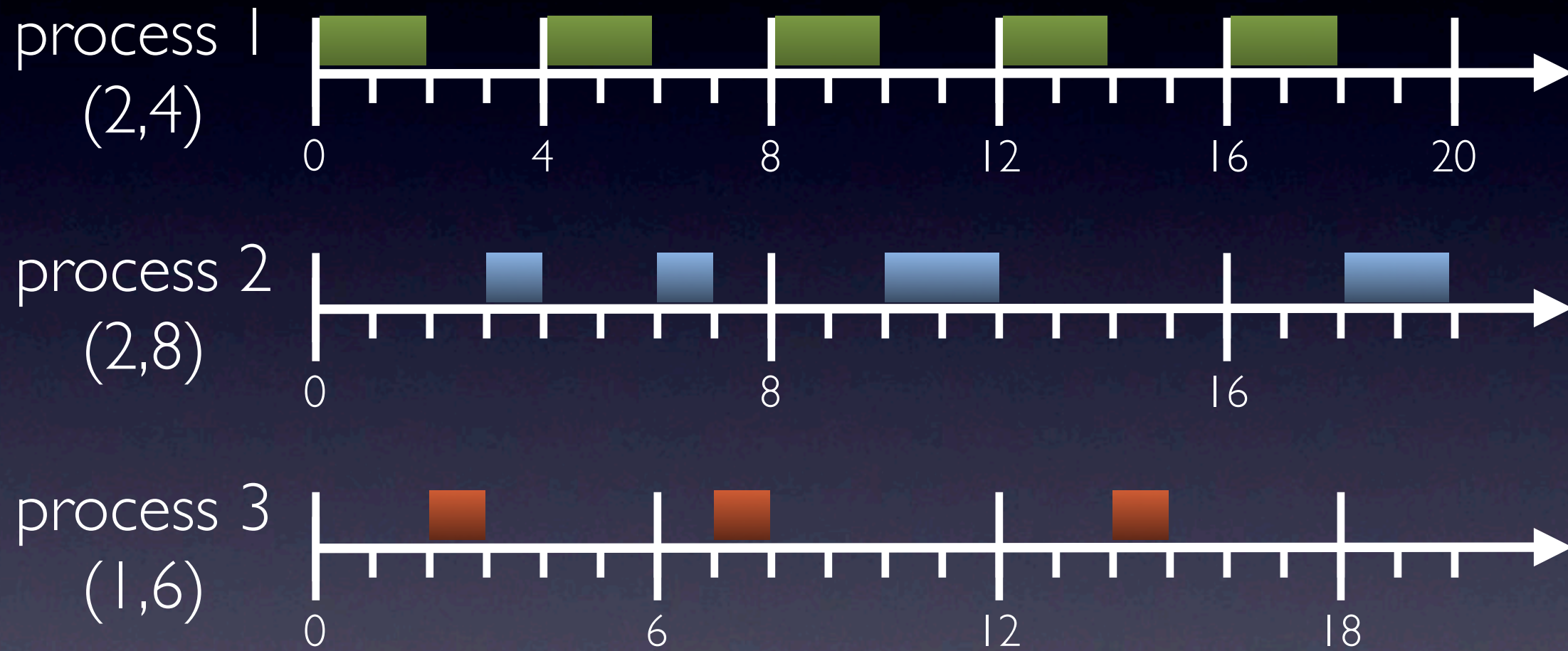
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