

Time Safety Check

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Time safety: Motivation

□ RTOS

Traditional *schedulability* test checks for a feasible schedule

- for a given scheduling algorithm
- for given task assumptions (task models)

schedulability  determinism

□ Embedded machine on top of RTOS

- interaction with the environment is completely separated from task execution
- E code is *time safe* if each task *completes before its outputs are read (and new inputs are provided)* - platform dependent property
- if E code is triggered by environment

time safety  determinism

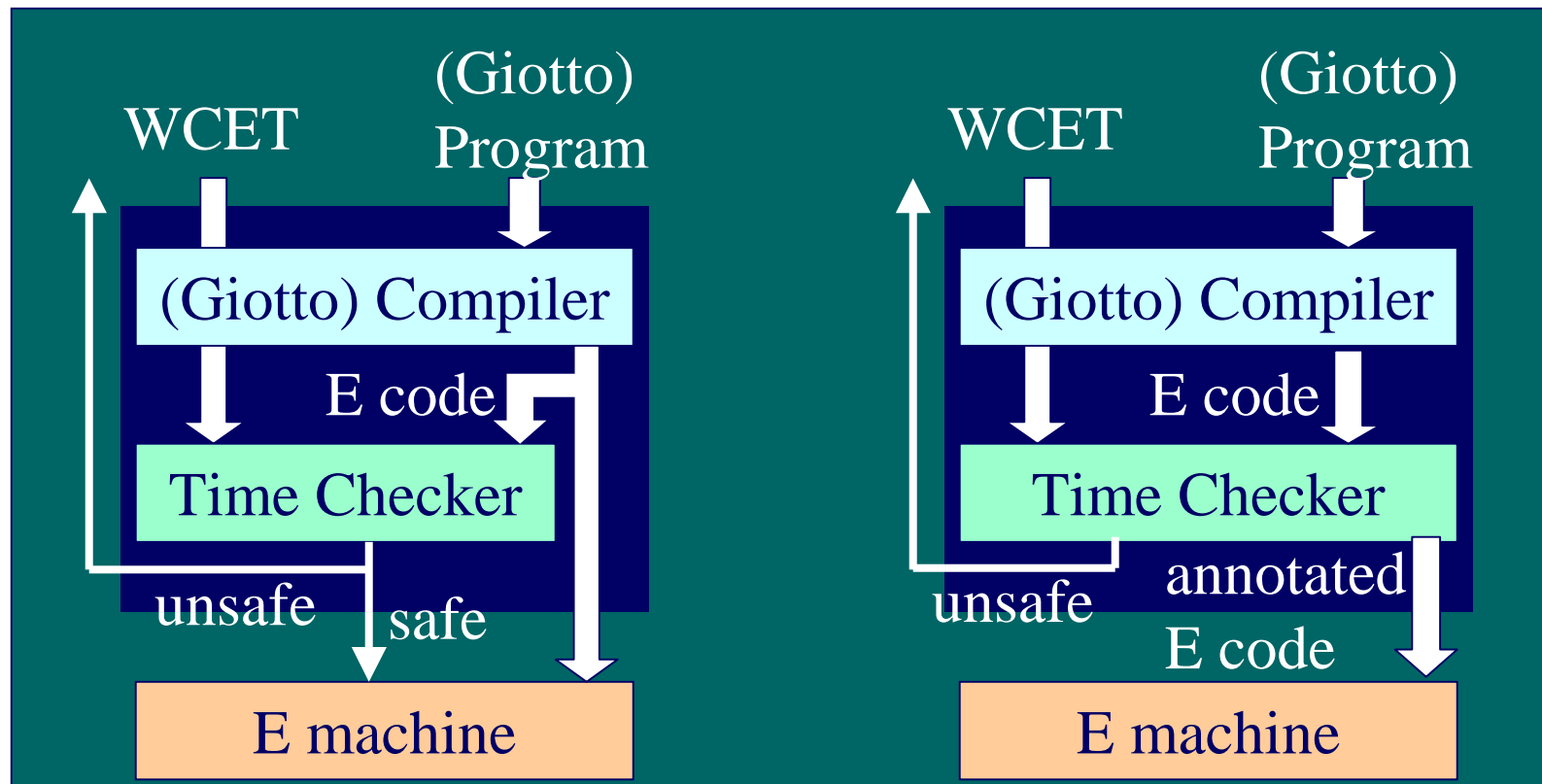
both timing and value predictability ensured

Approach

- ❑ Deadlines implicitly specified in the E code:

Operate on E code directly, without extracting task set model

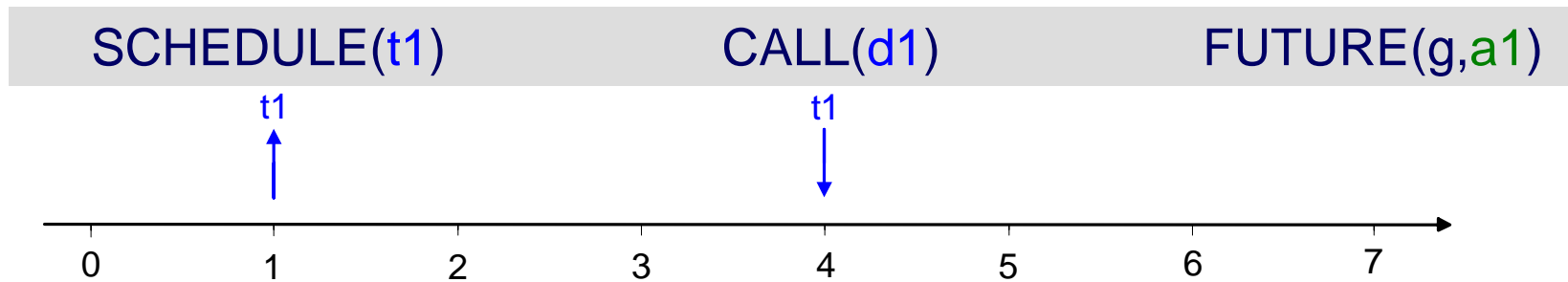
- ❑ more program analysis than schedulability test



Problem statement

□ E code instructions (synchronous computation)

- core instructions:



- control flow instructions:



□ time-triggered E code

$$g(n): \quad \text{clk}' = \text{clk} + n$$

□ platform dependent parameters of the algorithm

- *WCET* for each task
- EDF scheduling scheme

Algorithm

❑ develop the schedule using EDF algorithm to see if all deadlines are met

❑ starting from initial trigger simulate execution of E code:

at each step of the algorithm scan the E code with label *a* for

- CALL and SCHEDULE **completed(*a*)**
- SCHEDULE **scheduled(*a*)**
- FUTURE **future(*a*)**

❑ each step can be considered as state transition:

what's the state? **(task_config, trigger_config)**

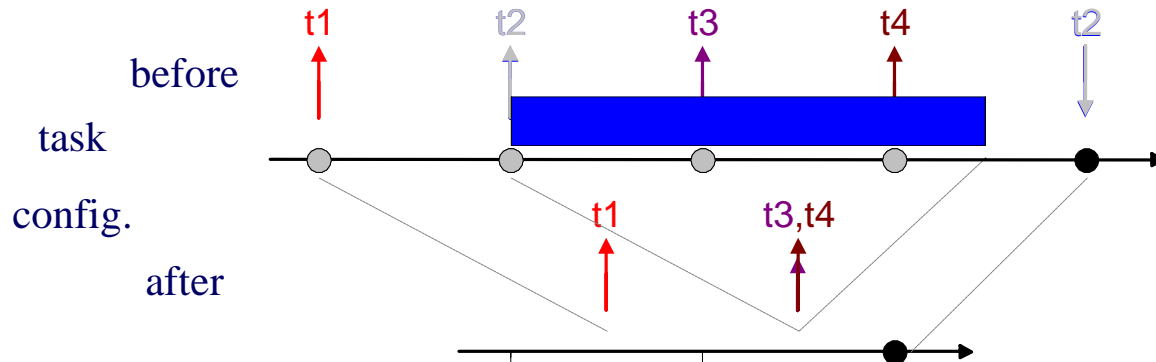
simple numeric test for time safety of a configuration

❑ simulate until new state already visited or time violation occurred

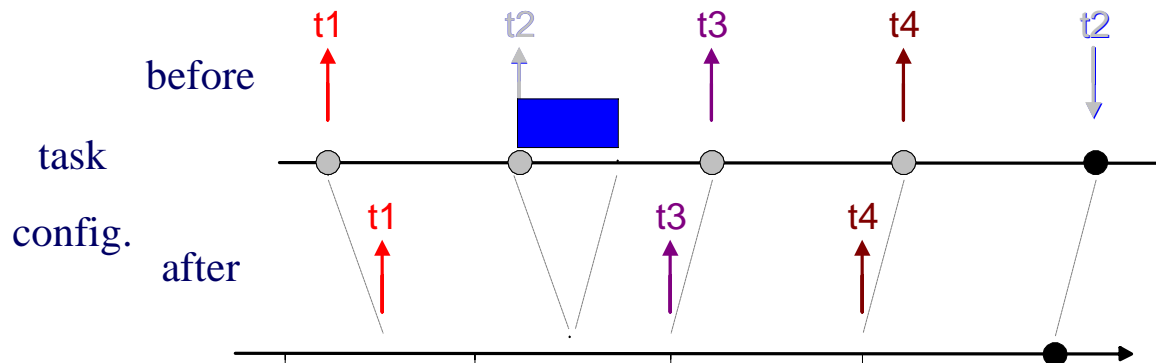
❑ run the algorithm for the each assignment of conditional jumps

Basic state transition

$$WCET(t2) = 2.5$$



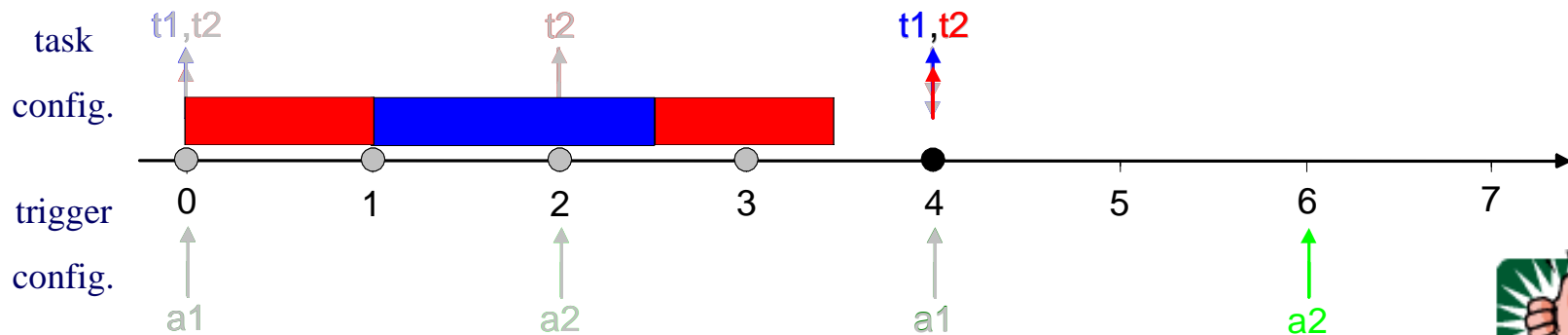
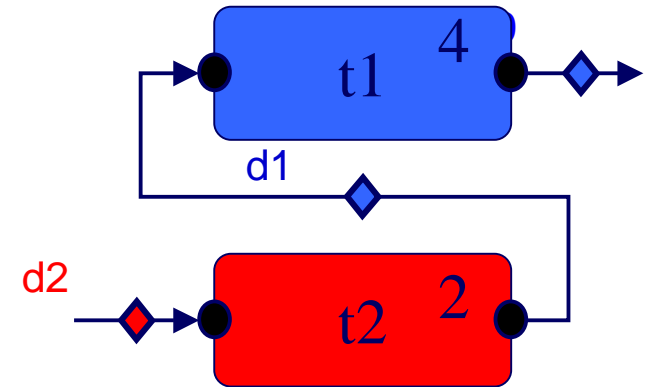
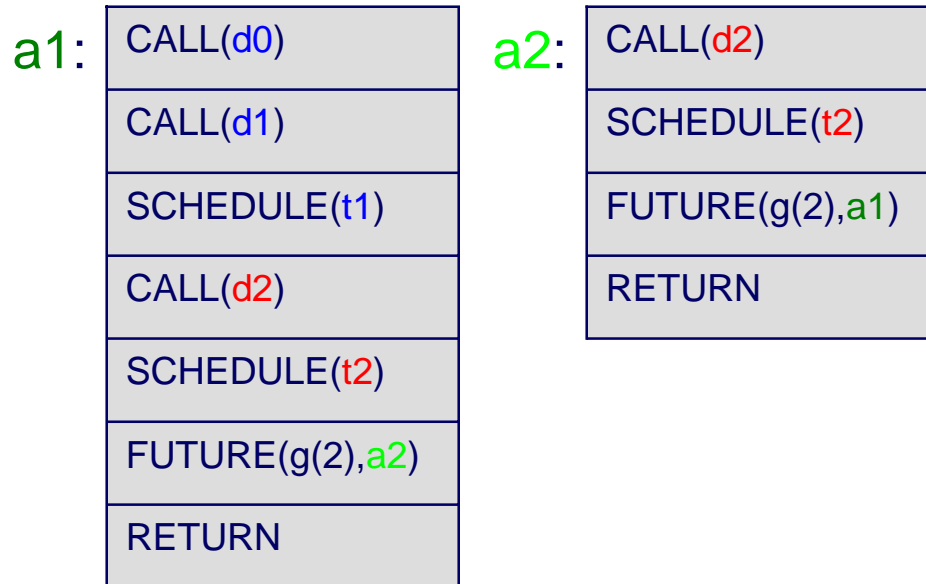
$$WCET(t2) = 0.5$$



Two-task example

$A_0 = \{(a1,0)\}$

$WCET(t1)=1.5, WCET(t2)=1$



Two-task example (2)

$A_0 = \{(a1,0)\}$

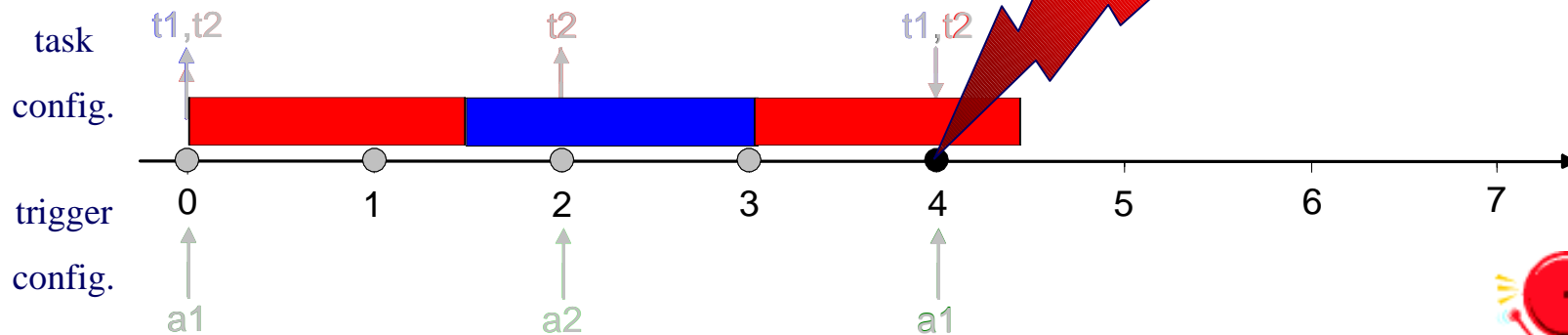
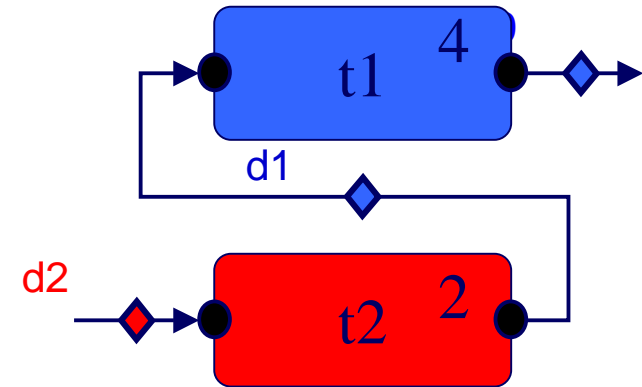
$WCET(t1) = 1.5, WCET(t2) = 1.5$

a1:

CALL(d0)
CALL(d1)
SCHEDULE(t1)
CALL(d2)
SCHEDULE(t2)
FUTURE(g(2),a2)
RETURN

a2:

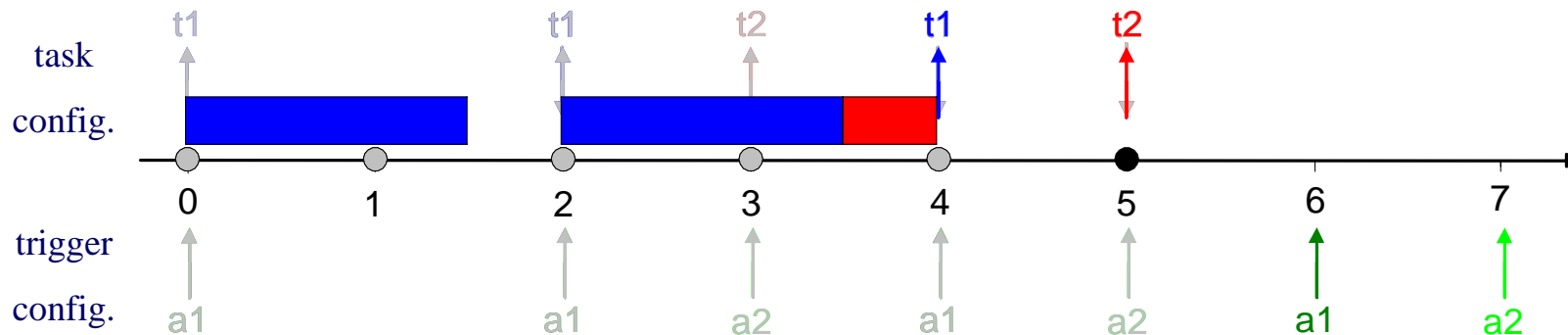
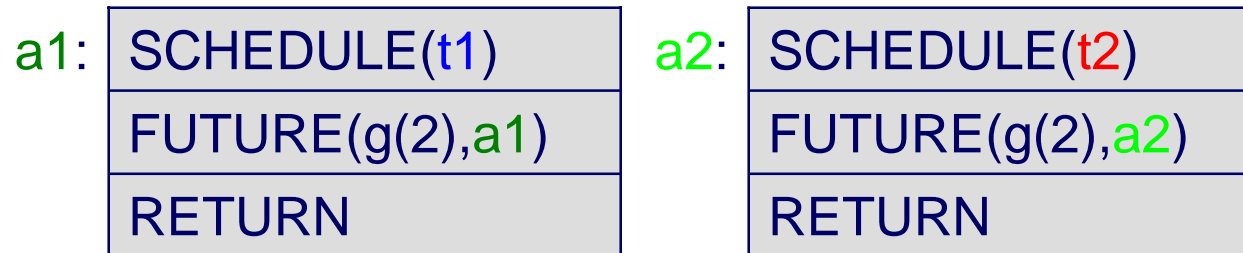
CALL(d2)
SCHEDULE(t2)
FUTURE(g(2),a1)
RETURN



Phase-shifted task set

$$Ao = \{(a1,0),(a2,3)\}$$

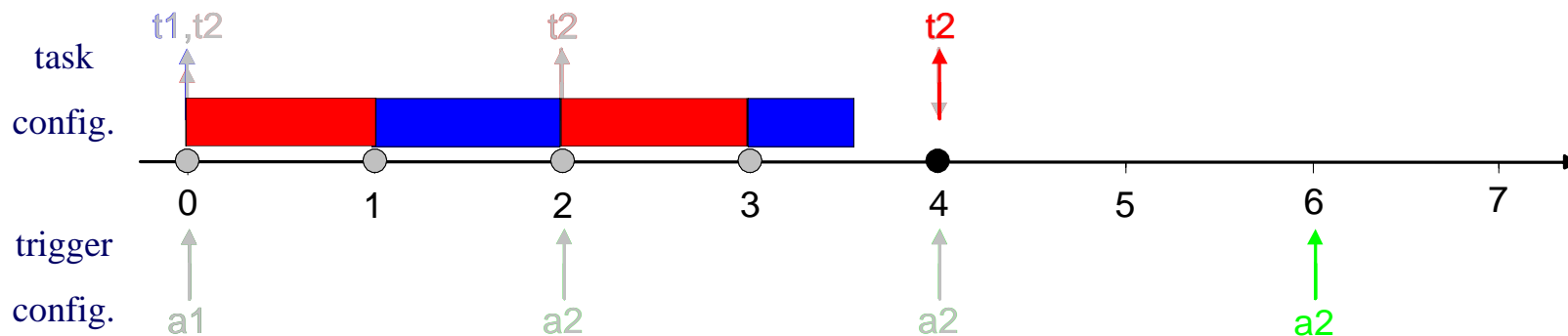
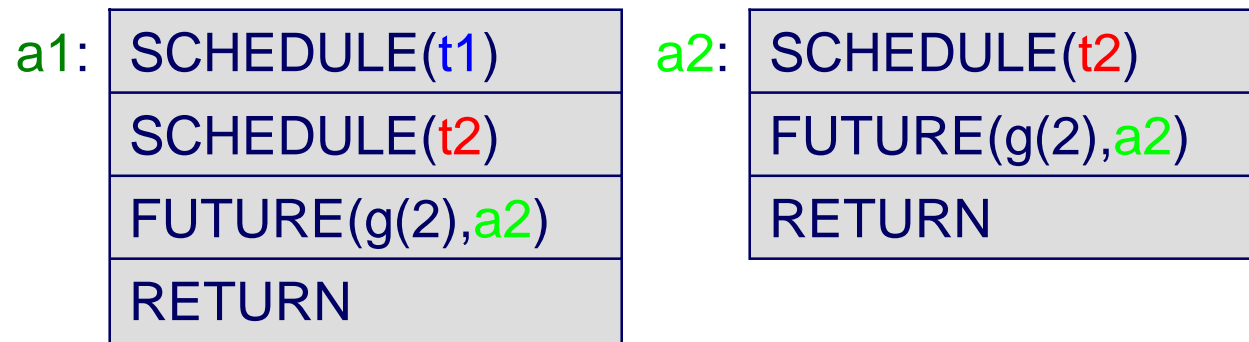
$$WCET(t1) = 1.5, WCET(t2) = 0.5$$



Non-EDF schedule

$$A_0 = \{(a_1, 0)\}$$

$$WCET(t_1) = 1.5, WCET(t_2) = 1$$



IF instruction example

$Ao = \{(a1,0),(a2,0)\}$

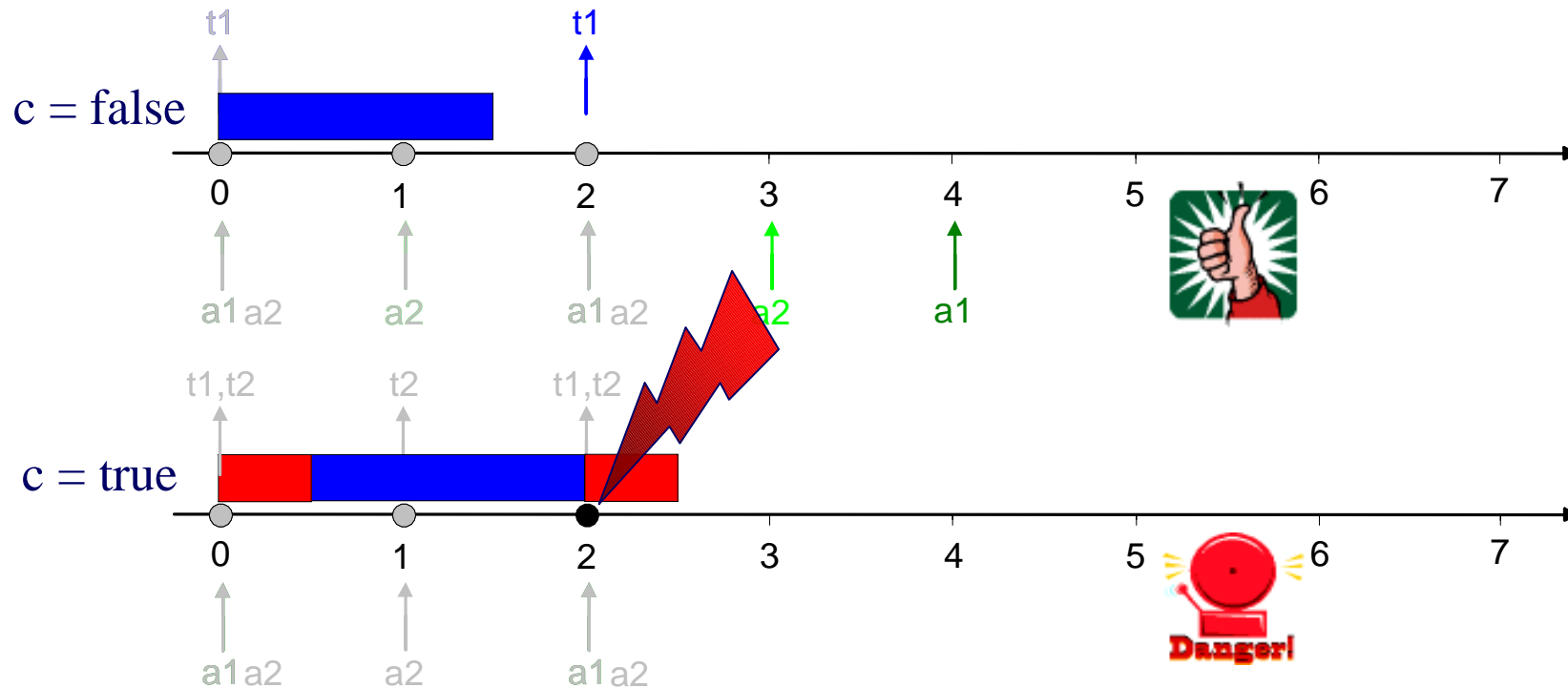
$WCET(t1)=1.5, WCET(t2)=0.5$

a1:

SCHEDULE(t1)
FUTURE(g(2),a1)
RETURN

a2:

IF(c,a2',a2'')
a2': SCHEDULE(t2)
a2'': FUTURE(g(1),a2)
RETURN



Pseudo code

Algorithm 1 `time_safety_check(A, T)`

```
if  $(A, T) \in \mathcal{H}$  then
   $\mathcal{H} \leftarrow \mathcal{H} \cup \{(A, T)\}$ 
   $C \leftarrow \text{enum\_cond\_assignment}(\text{number of if instructions})$ 
  while  $C \neq \emptyset$  do
     $C \leftarrow C \cup \{C\}$ 
    if  $\text{is\_safe}(A, T, C) = \text{false}$  then
      time safety violation!
    end if
     $T_n \leftarrow \text{execute\_tasks}(A, T, C)$ 
     $T_n \leftarrow \text{schedule\_tasks}(A, T_n, C)$ 
     $A_n \leftarrow \text{future}(A, C)$ 
     $\text{time\_safety\_check}(A_n, T_n)$ 
  end while
end if
```

Algorithm 2 `is_safe(A, T, C)`

```
 $T_c \leftarrow \text{completed}(A, C)$ 
 $T_r \leftarrow T, \omega = 0$ 
while  $T_r \neq \emptyset$  do
   $T_r \leftarrow \langle (T, \tau) \rangle \circ T_r$ 
   $\omega \leftarrow \omega + \sum_{t \in \text{run}_\tau} \text{wcet}(t) - \tau$ 
   $\omega \leftarrow \max(0, \omega)$ 
end while
return  $\omega = 0$ 
```

Algorithm 3 `execute_tasks(A, T, C)`

```
 $T_c \leftarrow \text{completed}(A, C)$ 
 $T \leftarrow \text{execute\_completed\_tasks}(T_c, T)$ 
 $T \leftarrow \text{merge\_tasks}(T)$ 
 $T \leftarrow \text{execute\_tasks\_early}(T)$ 
return  $T$ 
```

Algorithm 4 `execute_completed_tasks(T_c, T)`

```
 $T_i \leftarrow \langle \rangle, T_r \leftarrow T$ 
while  $T_r \neq \langle \rangle$  do
   $T_r \leftarrow \langle (T, \tau) \rangle \circ T_r$ 
   $\tau \leftarrow \tau - \sum_{t \in \text{run}_\tau} \text{wcet}(t)$ 
   $T \leftarrow T \setminus T_c$ 
   $T_i \leftarrow T_i \circ \langle (T, \tau) \rangle$ 
end while
return  $T_i$ 
```

Algorithm 5 `merge_tasks(T)`

```
 $T_i \leftarrow \langle \rangle, T_r \leftarrow T$ 
while  $T_r \neq \langle \rangle$  do
   $T_r \leftarrow \langle (T, \tau) \rangle \circ T_r$ 
  if  $\tau \leq 0 \wedge T_r \neq \langle \rangle$  then
     $T_r \leftarrow \langle (D, \delta) \rangle \circ T_r$ 
     $T_r \leftarrow \langle (D \cup T, \delta + \tau) \rangle \circ T_r$ 
  else if  $\tau > 0 \wedge T = \emptyset \wedge T_i \neq \langle \rangle$  then
     $T_i \leftarrow T_i \circ \langle (D, \delta) \rangle$ 
     $T_i \leftarrow T_i \circ \langle (D, \delta + \tau) \rangle$ 
  else if  $T \neq \emptyset$  then
     $T_i \leftarrow T_i \circ \langle (T, \tau) \rangle \quad \{\tau \geq 0\}$ 
  end if
end while
return  $T_i$ 
```

Algorithm 6 `execute_tasks_early(T)`

```
 $T_i \leftarrow T, T_c \leftarrow \langle \rangle, T_r \leftarrow \langle \rangle \quad \{T = T_i \circ T_c \circ T_r\}$ 
 $\omega \leftarrow 0$ 
while  $T_i \neq \langle \rangle$  do
   $T_i \leftarrow T_i \circ \langle (T, \tau) \rangle$ 
   $T_c \leftarrow \langle (T, \tau) \rangle \circ T_c$ 
   $\omega \leftarrow \omega + \sum_{t \in T} \text{wcet}(t) - \tau$ 
  if  $\omega > 0$  then
     $T_r \leftarrow T_c \circ T_r$ 
     $T_c \leftarrow \langle \rangle$ 
     $\omega \leftarrow 0$ 
  end if
end while
return  $T_r$ 
```

Pseudo code (2)

Algorithm 1 `time_safety_check(A, T)`

```
if  $(A, T) \notin \mathcal{H}$  then
   $\mathcal{H} \leftarrow \mathcal{H} \cup \{(A, T)\}$ 
   $C \leftarrow \text{enum\_cond\_assignment}(\text{number of if instructions})$ 
  while  $C \neq \emptyset$  do
     $C \leftarrow C \cup \{C\}$ 
    if  $\text{is\_safe}(A, T, C) = \text{false}$  then
      time safety violation!
    end if
     $T_n \leftarrow \text{execute\_tasks}(A, T, C)$ 
     $T_n \leftarrow \text{schedule\_tasks}(A, T_n, C)$ 
     $A_n \leftarrow \text{future}(A, C)$ 
    time_safety_check( $A_n, T_n$ )
  end while
end if
```

Algorithm 2 `is_safe(A, T, C)`

```
 $T_c \leftarrow \text{completed}(A, C)$ 
 $T_r \leftarrow T, \omega \leftarrow 0$ 
while  $T_r \neq \emptyset$  do
   $T_r \leftarrow ((T, \tau)) \circ T_r$ 
   $\omega \leftarrow \omega + \sum_{t \in \text{gr}(T_r)} \text{wcost}(t) - \tau$ 
   $\omega \leftarrow \max(0, \omega)$ 
end while
return  $\omega = 0$ 
```

Results and future work

□ implemented as TimeChecker class in the current Giotto compiler

- without IF : fast decision

- with IF instructions :

- and explicit enumeration of program branching paths : reasonable response times if $n < 10$

- and some simple code analysis : fast decision

e.g. branching on task and driver guards can be avoided

□ future

- find patterns in configuration: simplified time safety proof

- compositional time safety check