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Schedule-Carrying Code

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Giotto

Giotto is a formal model/ high level programming language for RTS based on FLET and periodic tasks.

Advantages:

- Separation of functional and timing concerns
- Value and time determinism
- Predictability
- Platform-independence
- Multi-modal support (mode switching)
- Compossability

Schedule Carrying Code

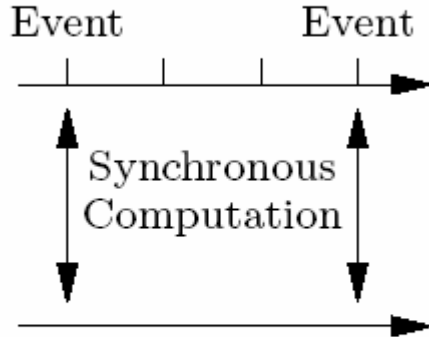
SCC is real time code annotated with the description of a schedule, which witnesses the schedulability of the code.

Advantages

- Produced by the compiler
- Produced once and revalidated and executed with each use, on a given platform.
- More efficient
- More flexible
- It is easier to prove time safety.
- Reuse of proofs

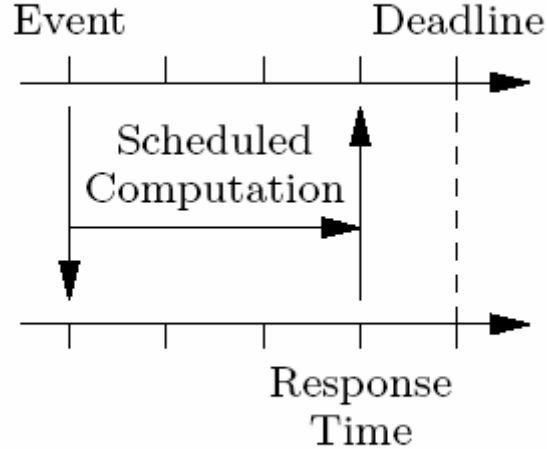
Models for Real Time Programming

Synchronous Model



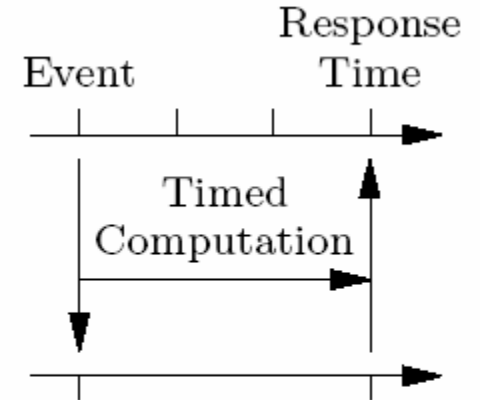
Soft-Time = 0

Scheduled Model



Soft-Time \leq Real-Time

Timed Model

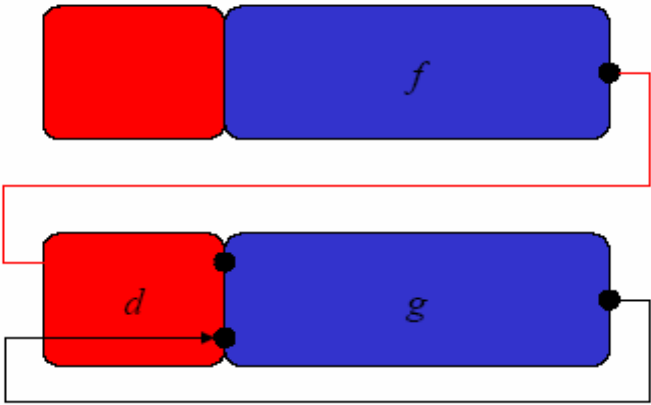
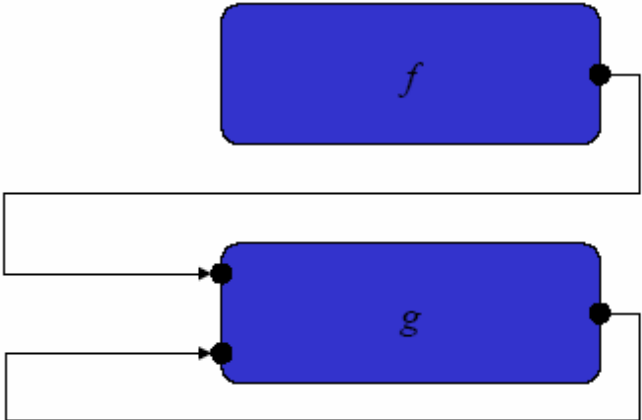
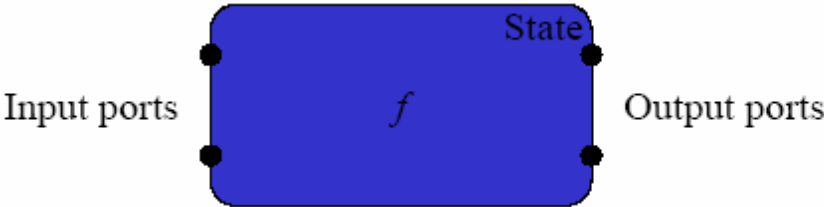


Soft-Time = Real-Time

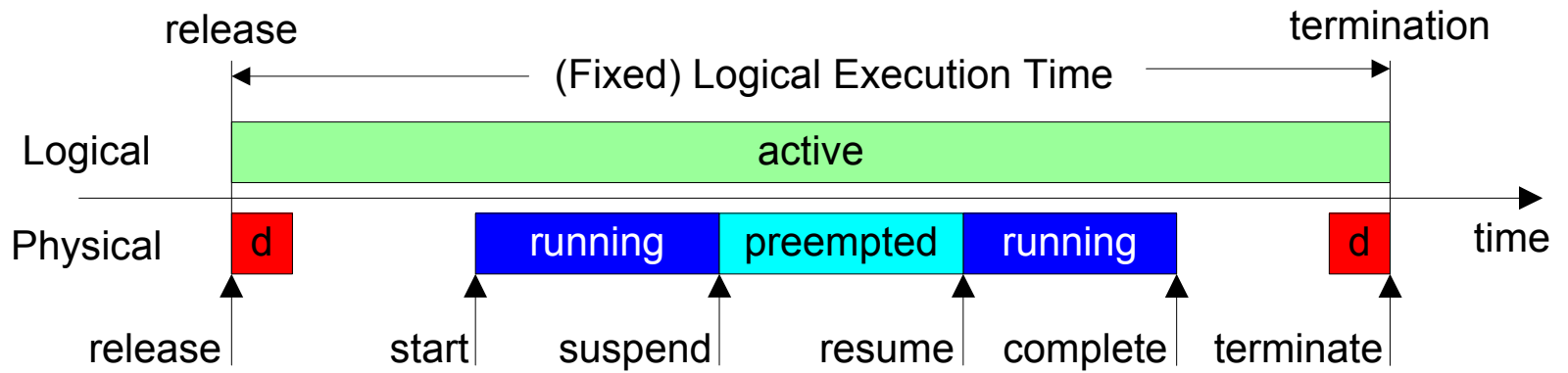
Elements of Formal Models for Real Time Systems

- Components and connectors
- Functional and control description of components
- Time issues
- Environment behavior description
- Processing issues
- Verification technique
- Complexity

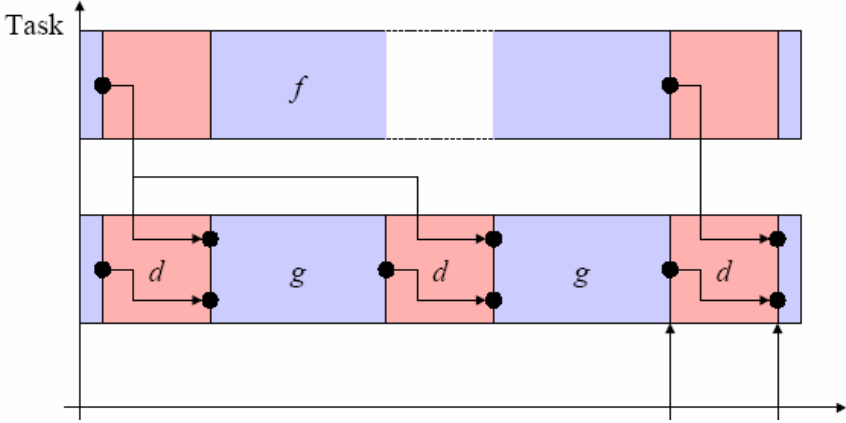
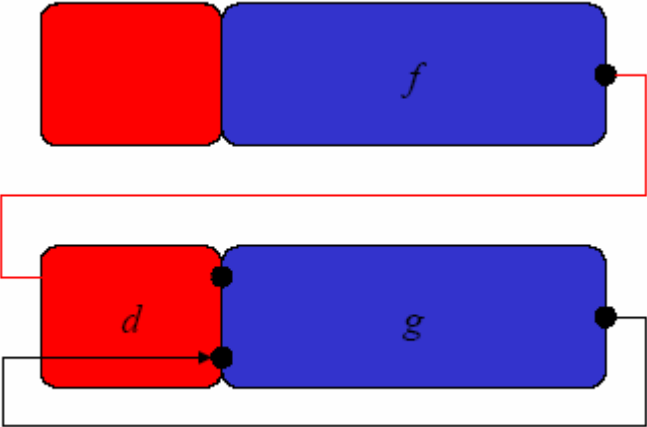
Giotto Model



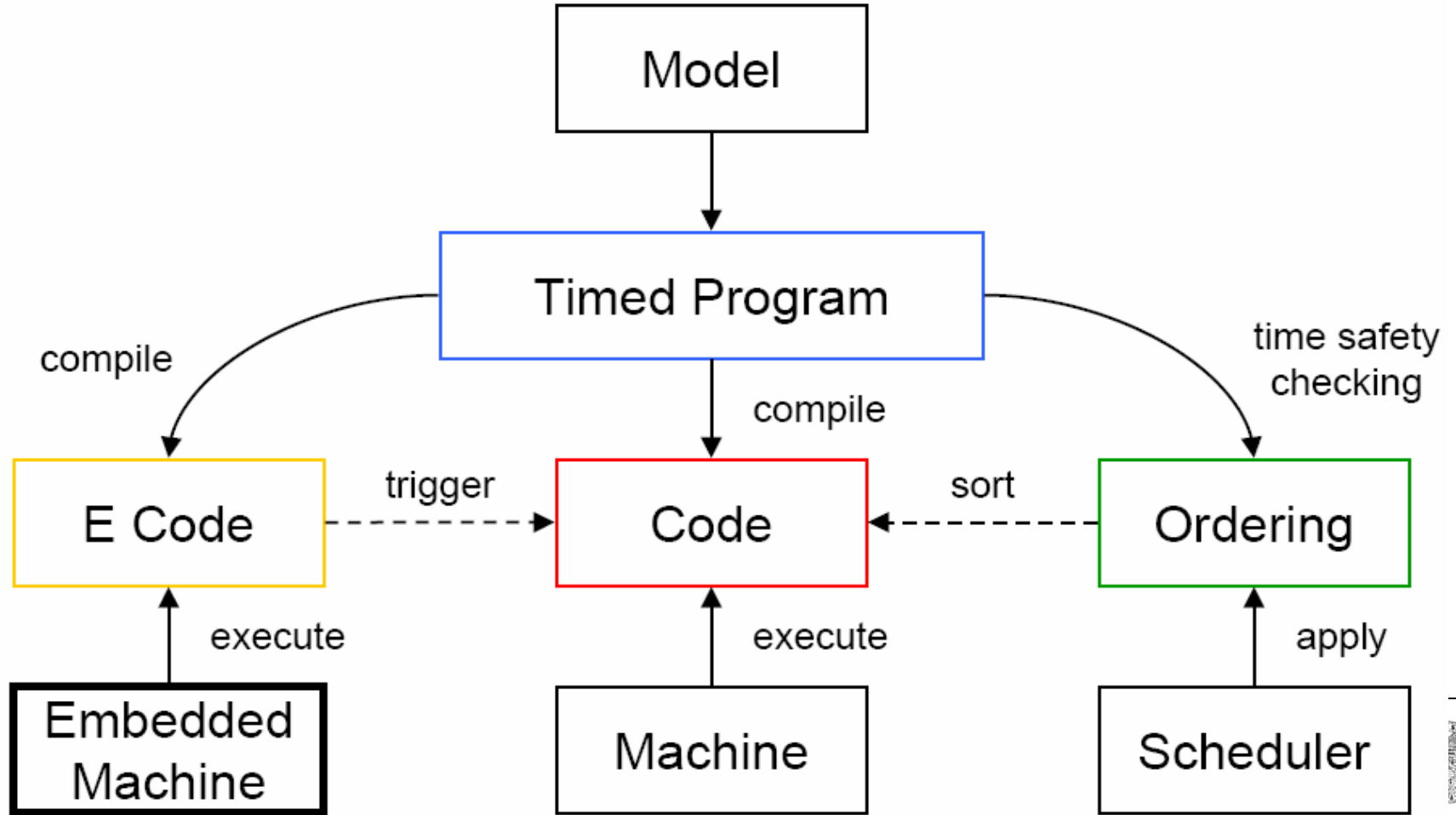
FLET – Task Execution Model



FLET – Communication Between Tasks



Giotto Tool Chain



E Code

E code

- Reactive/ timing code
- Manages the release times and deadlines of software tasks in reaction to environment events

E code is:

- *Portable*
- *Predictable*
- *Composable*

S Code

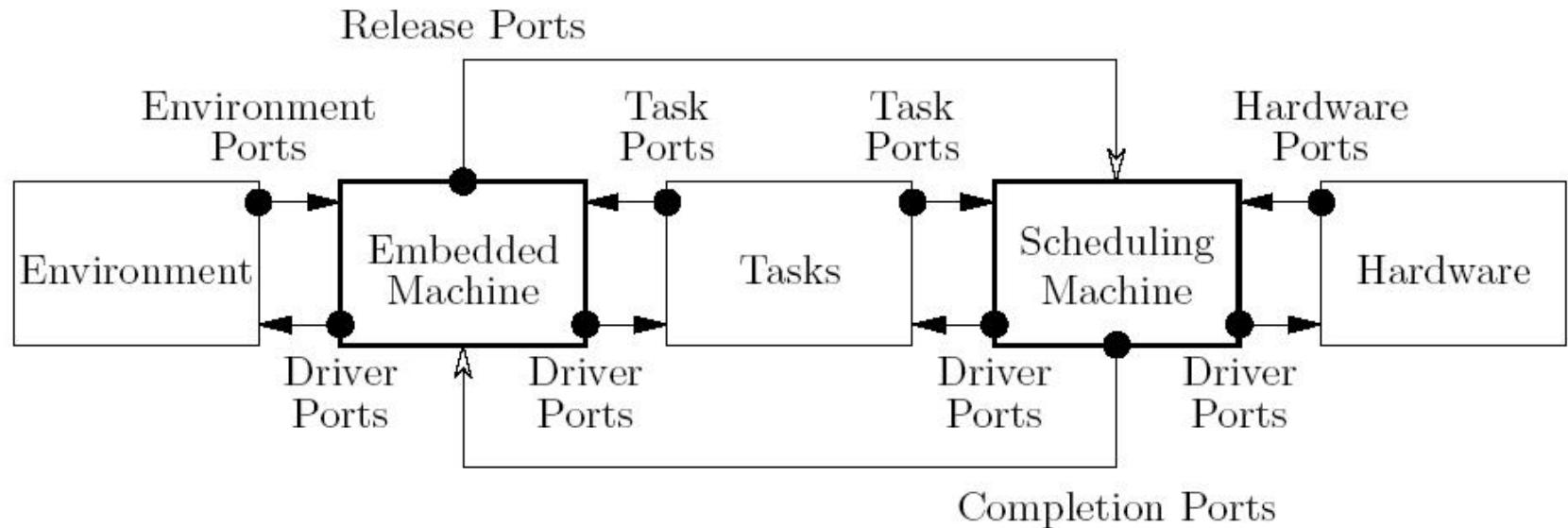
S code

- Proactive/ scheduling code
- Manages the execution of released tasks on available CPUs

S code is:

- *Universal* – any scheduling strategy
- *Verifiable* – fast time safety checking
- *Supports distribution*

The E Machine and S Machine



- Tasks are preemptive, user level code, with non-negligible WCETs
- Drivers are system level code, with negligible WCETs
- E Machine monitors input events through triggers
- S Machine monitors input events through timeouts

E Code Instructions

- Call(d)
- Schedule(t)
- Future(g,a)

The E machine maintains a queue of trigger bindings (g,a,s).

- If (c,a)
- Return

The execution is *time safe* if once released, a task t completes:

- Before any driver accessed a port of t
- Before t is released again

E Code Interpreter

```
while ProgramCounter  $\neq \perp$  do  
  i := Instruction(ProgramCounter)  
  if call(d) = i then  
    if driver d accesses a port of a task t that has been released but not completed  
    then throw a time-safety exception else execute d  
  else if schedule(t) = i then  
    if task t has already been released but not yet completed  
    then throw a time-safety exception else emit a signal on the release port of t  
  else if future(g, a) = i then  
    append the trigger binding (g, a, s) to TriggerQueue, where s is the current  
    state of the input ports that occur in g  
  end if  
  ProgramCounter := Next(ProgramCounter)  
end while
```

S Code Instructions

Transient instructions:

- Call(d)
- Fork(a)

The execution is *time sharing* if only one task is dispatched to the CPU.
The S machine maintains a set of thread instances (t, b, h, a, s).

Timed instructions:

- Dispatch(t,h,a) with 2 possible outcomes. S machine proceeds with:
 - ☒ The next instruction (t completes, or has not been released)
 - ☒ S code at address a (h expires)
- Idle(h)

S Code Interpreter

```
while ProgramCounter  $\neq \perp$  do  
  i := Instruction(ProgramCounter)  
  ProgramCounter := Next(ProgramCounter)  
  if call(d) = i then  
    if driver d accesses a port of a task t that has been released but not completed  
    then throw a time-safety exception else execute d  
  else if dispatch(t, h, a) = i then  
    if there is a thread instance in ThreadSet with a non-idle task then  
      throw a time-sharing exception  
    else  
      insert the thread instance (t, ProgramCounter, h, a, ReferenceTime) into  
      ThreadSet and set ProgramCounter to  $\perp$   
    end if  
  else if idle(h) = i then  
    insert the thread instance (idle,  $\perp, h, ProgramCounter, ReferenceTime$ ) into  
    ThreadSet and set ProgramCounter to  $\perp$   
  else if fork(a) = i then  
    insert the thread instance (idle,  $\perp, true, a, s$ ) into ThreadSet, where s is the current  
    value of the system clock  
  end if  
end while
```

Example - Simplified Flight Control

Giotto

```
start hover {  
mode hover() period 120ms {  
  exitfreq 3 do cruise(switch);  
  taskfreq 1 do pilot();  
  taskfreq 2 do control();  
  taskfreq 3 do lieu(); }  
mode cruise() period 120ms {  
  exitfreq 2 do hover(switch);  
  taskfreq 1 do pilot();  
  taskfreq 2 do control();  
  taskfreq 4 do move(); }
```

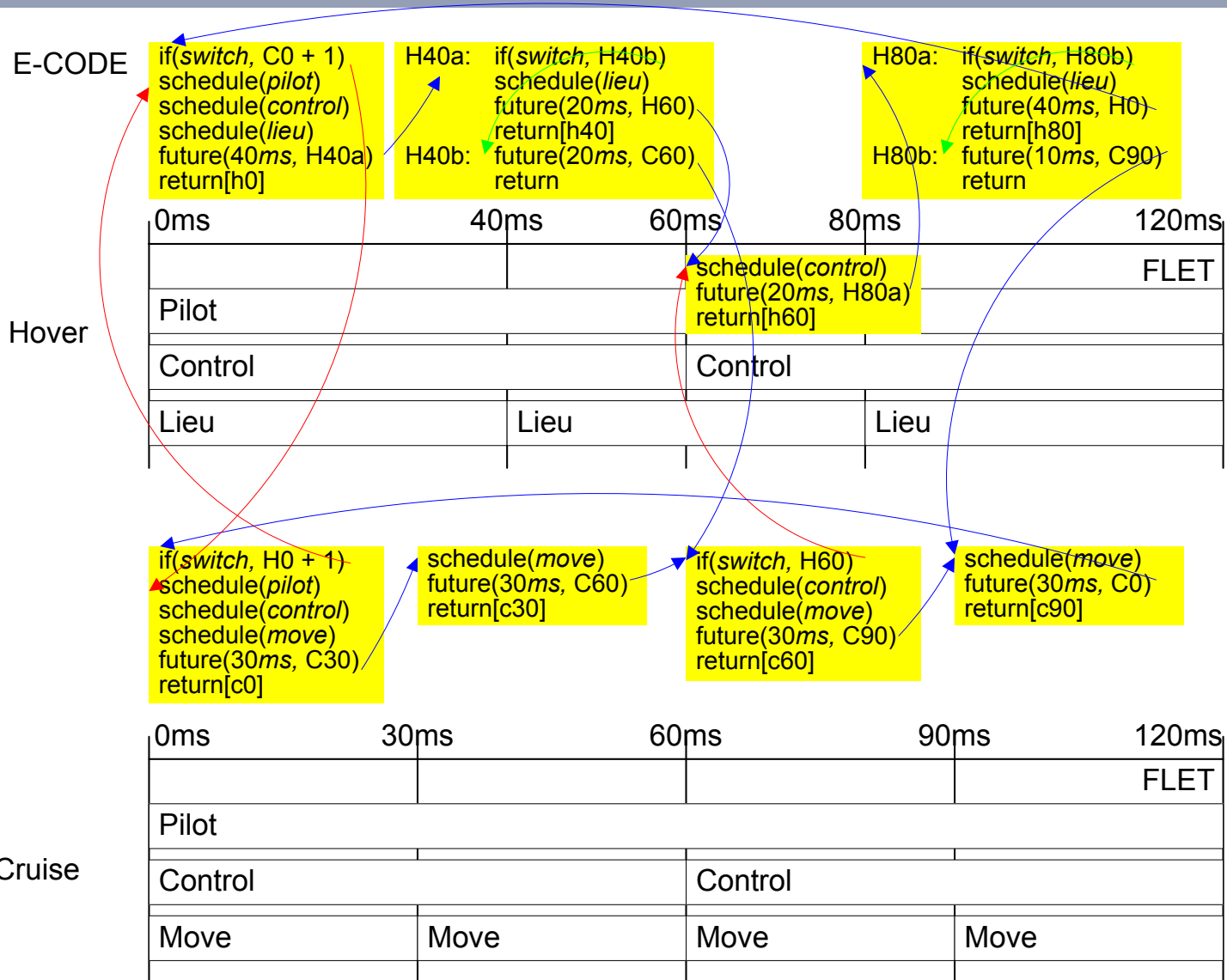
E Code

```
H0: if(switch, C0 + 1)  
  schedule(pilot)  
  schedule(control)  
  schedule(lieu)  
  future(40ms, H40a)  
  return[h0]  
H40a: if(switch, H40b)  
  schedule(lieu)  
  future(20ms, H60)  
  return[h40]  
H40b: future(20ms, C60)  
  return  
H60: schedule(control)  
  future(20ms, H80a)  
  return[h60]  
H80a: if(switch, H80b)  
  schedule(lieu)  
  future(40ms, H0)  
  return[h80]  
H80b: future(10ms, C90)  
  return
```

```
C0: if(switch, H0+ 1)  
  schedule(pilot)  
  schedule(control)  
  schedule(move)  
  future(30ms, C30)  
  return[c0]  
C30: schedule(move)  
  future(30ms, C60)  
  return[c30]  
C60: if(switch, H60)  
  schedule(control)  
  schedule(move)  
  future(30ms, C90)  
  return[c60]  
C90: schedule(move)  
  future(30ms, C0)  
  return[c90]
```



Simplified Flight Control - E code



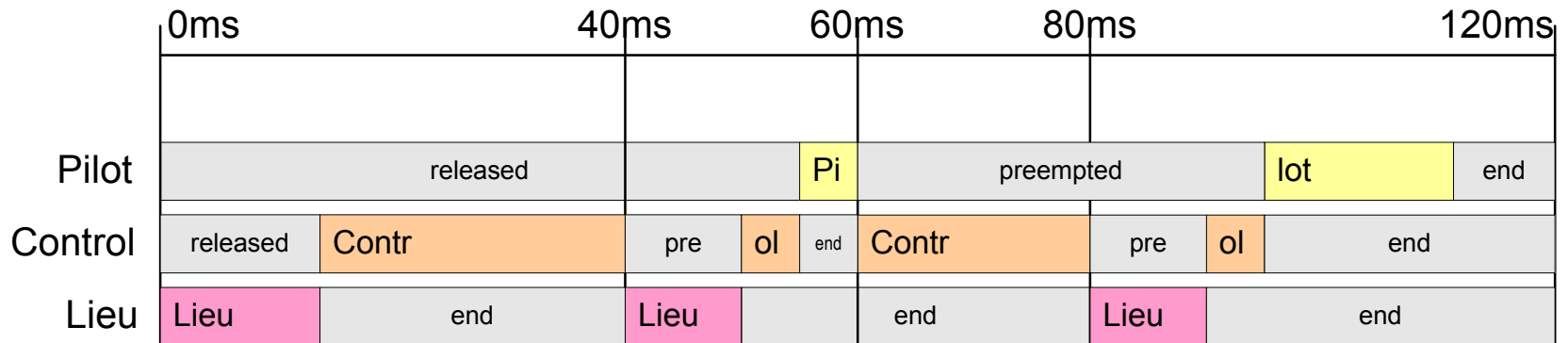
Simplified Flight Control - S Code Variants - RM

Rate Monotonic

```

RM: dispatch(lieu, +4)
    dispatch(control, +3)
    dispatch(pilot, +2)
    idle()
    fork(RM)
    return
    
```

Hover mode
(RM scheduling)



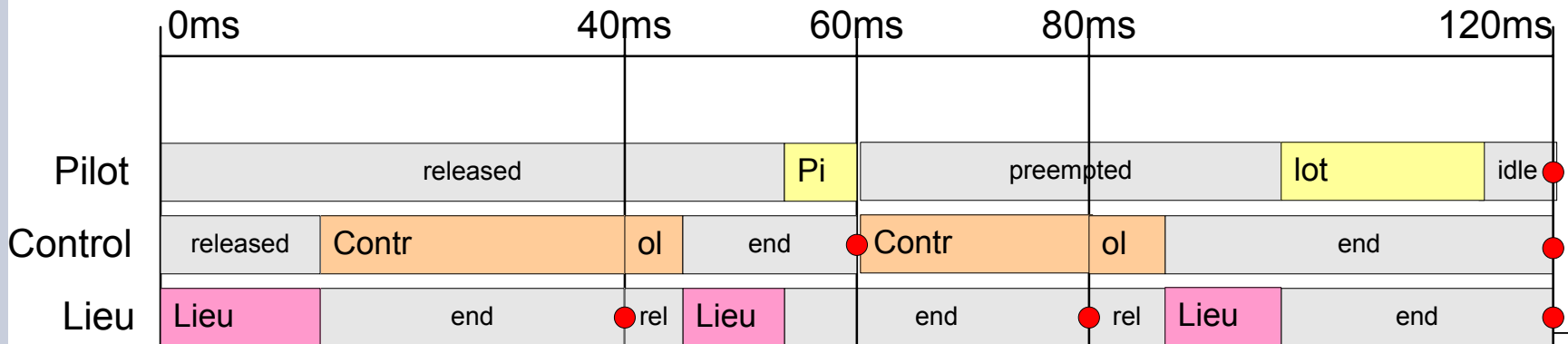
Simplified Flight Control - S Code Variants - EDF

Earliest-deadline-first

EDF0/60: dispatch(*lieu*, +4)
 dispatch(*control*, +3)
 dispatch(*pilot*, +2)
 idle()
 fork(EDF40/80)
 return

EDF40/80: dispatch(*control*, +4)
 dispatch(*lieu*, +3)
 dispatch(*pilot*, +2)
 idle()
 fork(EDF0/60)
 return

Hover mode
 (EDF scheduling)



Simplified Flight Control - S Code Variants

Non-Preemptive S Code for the cruise mode

Is time safe if $w(\text{move}) + w(\text{control}) \leq 30\text{ms}$ and $2 \cdot w(\text{move}) + w(\text{pilot}) \leq 60\text{ms}$

NP0: dispatch(*move*)
dispatch(*control*)
idle()
fork(NP30)
return

NP30: dispatch(*move*)
dispatch(*pilot*, NP60)
idle()
fork(NP60)
return

NP60: dispatch(*pilot*)
dispatch(*move*)
idle()
fork(NP90)
return

NP90: dispatch(*control*)
dispatch(*move*)
idle()
fork(NP0)
return

SCC Rules

- An *SCC program* is a pair (E, S) consisting of an E program that shares a set of tasks with an S program

Rules

- if there is an enabled thread instance that contains a completed task, then the S machine must handle that thread instance before the E machine handles any enabled triggers
- if there is an enabled trigger binding, then the E machine must handle that trigger binding before the S machine handles any expired timeouts.

Generating vs Checking SCC

- Use path-insensitive program analysis to check SCC, based on abstract semantics.
- Searching the state space is exponential.
- Checking the Time Safety is simpler for Giotto generated and simplified SCC.
- It is NP hard to generate non-preemptive or distributed schedules for Giotto programs.
- But simple Giotto generated SCC program can be checked in time linear with the size of the E code and frequency of events.

Time Safety Checking

- We can use classical Time Safety Checking for known algorithms.
- EDF schedulability of a single mode can be checked by solving a utilization equation.
- For multimode Giotto programs, if each mode in isolation is time-safe under EDF scheduling, then the whole program is time-safe under EDF
- It can be proved in linear size with the Giotto program that a SCC program corresponds to a certain algorithm

Optimality for schedulers

- A set of tasks is *schedulable* or *feasible* if all deadlines are met by some algorithm.
- A scheduling algorithm A is optimal among a category of scheduling algorithms if:

Any systems that A cannot schedule cannot be scheduled by any other scheduling algorithms in the same category

Optimal Scheduling Algorithms

Rate Monotonic Scheduling (RM)

- Priority = rate = $1/\text{period}$
- Tasks with smaller periods have higher priorities
- Optimal among all fixed-priority algorithms

Earliest Deadline First (EDF)

- Priority = absolute deadline
- Tasks with earlier deadlines have higher priorities
- Optimal dynamic (varying priority) scheduling algorithm

Processor Utilization - Time Safety Check

- The *processor utilization* factor is the fraction of the processor time spent in the execution of the task set:

$$U = \sum_{i=1}^n \frac{C_i}{T_i}$$

C_i – computation time, WCET
 T_i – period

Time safety check: for a given algorithm A , we can compute the *least upper bound* $U_{\text{lub}}(A)$

- If $U > 1$ no scheduling algorithms can guarantee the schedulability
- If $U \leq U_{\text{lub}}(A)$ the tasks are schedulable by algorithm A

This condition *sufficient but not necessary*:

- If $U_{\text{lub}}(A) < U \leq 1$, nothing can be said on the feasibility of the task set.



Processor Utilization -Time Safety Check

EDF Utilization Bound

- $U_{lub} = 1$
- TSC: $U \leq 1$
- EDF is optimal among all algorithms

RM Utilization Bound

- for n tasks: $U_{lub}(n) = n(2^{1/n} - 1)$
- $U_{lub}(2) = 0.828$
- $\lim_{n \rightarrow \infty} U_{lub}(n) = \ln 2 = 0.693$
- TSC: $U \leq U_{lub}$
- How do we test schedulability for RM when $U_{lub} < U \leq 1$?