

# PTIDES: A Programming Model for Time-Synchronized Distributed Real-time Systems

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# Motivation

- Implement distributed real-time systems
  - Deterministic
  - Lightweight
- by extending a modeling technique that has analyzable deterministic behavior
  - Discrete Event Modeling
- to enable static analysis of distributed real-time systems

# Distributed real-time systems

## Definition:

- **Multiple** computers connected on a network
- Computers **interact** with physical world through
  - Sensors
  - Actuators
  - and human computer interfaces
- Interact **with**/interact **through** the physical world
  - Passage of time becomes a central feature
- **Applications:** manufacturing, instrumentation, surveillance, multi-vehicle control, avionics systems, automotive systems, scientific experiments, ...
- Require high precision

# Distributed real-time systems

- Modeling distributed/embedded systems
  - OO programming using frameworks such as CORBA, SOAP, DCOM, ...
    - Heavyweight
    - Non-deterministic
  - Synchronous languages such as Esterel, Scade, Lustre, ...
    - Tight coordination difficult for distributed systems
  - Time-triggered languages and the logical execution time
    - Not only periodic tasks

# Discrete Event Modeling

## Event:

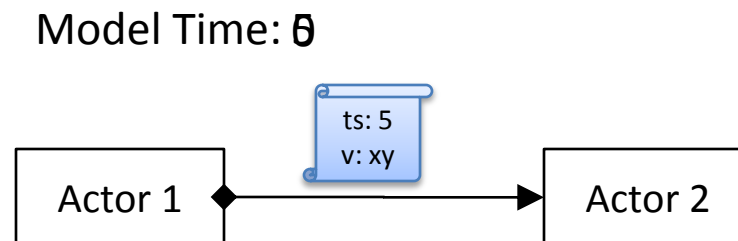
- Time stamp: when should an action be taken
- Value: kind of action

## Signal:

Sequence of events in chronological order

## Time:

Common notion of time in the whole system



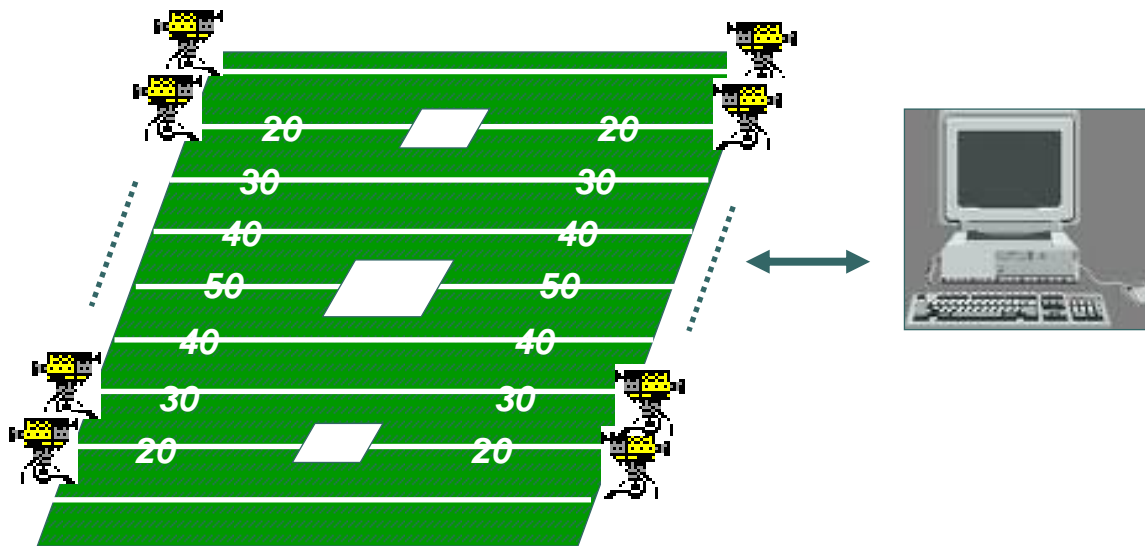
# Discrete Event Modeling

- Concurrent compositions of components that interact via *events* = time-stamped value, where time is “logical time” or “modeling time”
- Correct execution by ordering according to time stamps
- Analyzable deterministic behavior
- Simulation technology
  - 1) Conservative technique: total ordering of events  
waste of resources, does not meet realistic real-time constraints
  - 2) Optimistic technique: perform speculative execution and backtrack if necessary  
cannot backtrack physical interactions

## PTIDES:

- Application specification language
- Global common notion of time through network time synchronization
- Execution strategy:
  - Global coordination layer: can event be processed immediately or wait
  - Local resource scheduling layer: e.g. EDF
- For certain events, modeling time is mapped to physical time conservative approach, but looser coupling than with (1)
  - Partial order on events = relevant order
  - Release events out of their time stamp order

# Example: Camera application



## N cameras (= sensor and actuator)

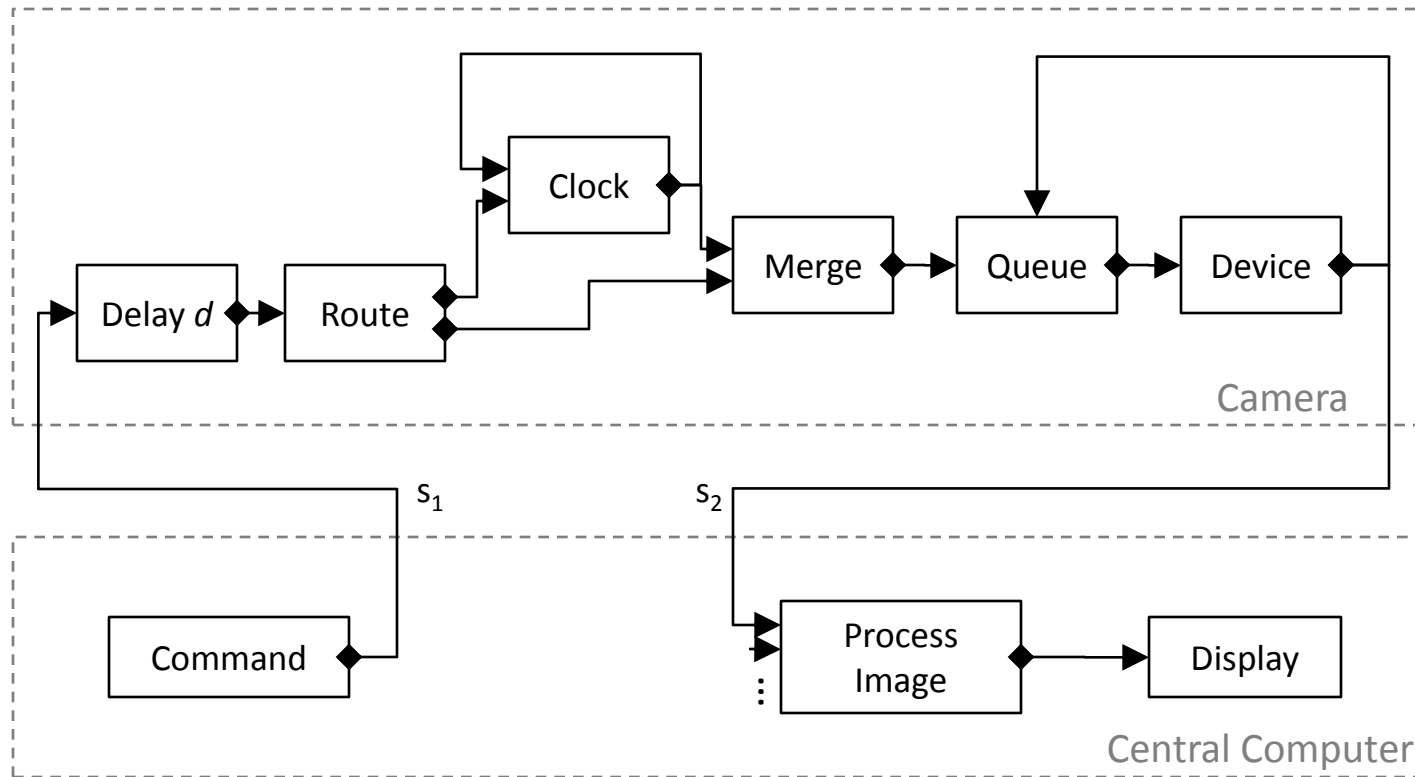
- synchronized clocks
- connected via Ethernet
- partial view of the field
- (simultaneous) take picture (time-stamped), zoom

## 1 central computer

- controls taking picture, zooming
- process pictures

**Challenge:** coordinate cameras to get precisely synchronized images

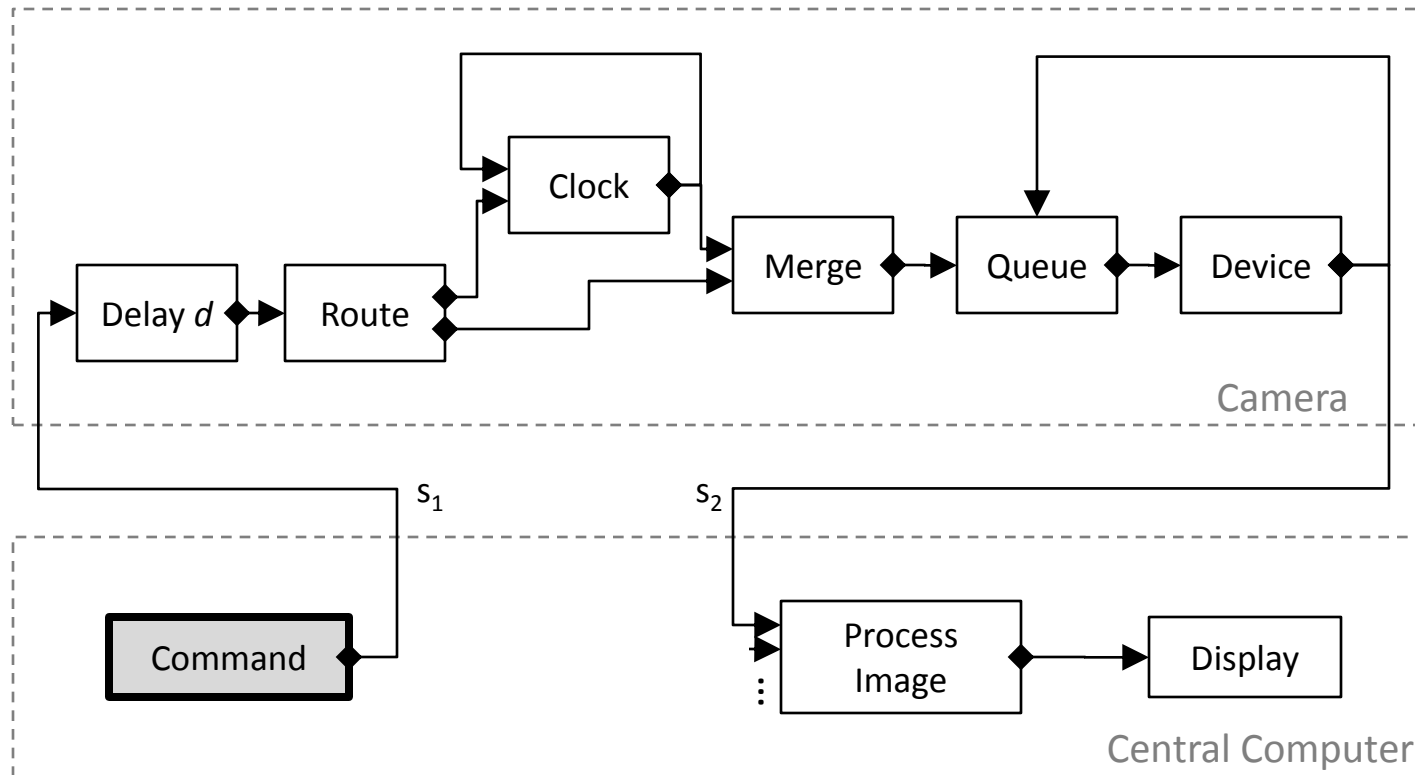
# Specification of the networked camera application



only communication via ports

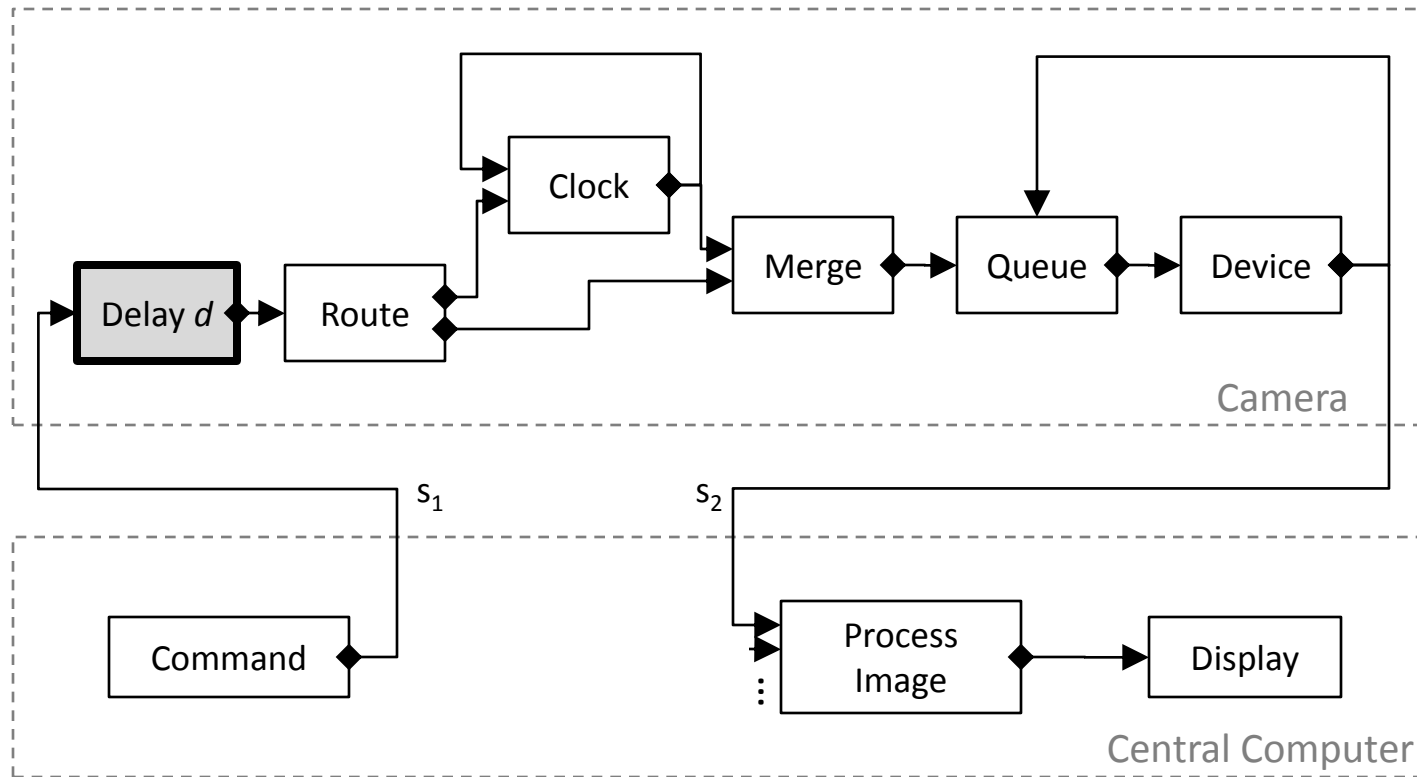


# Specification of the networked camera application



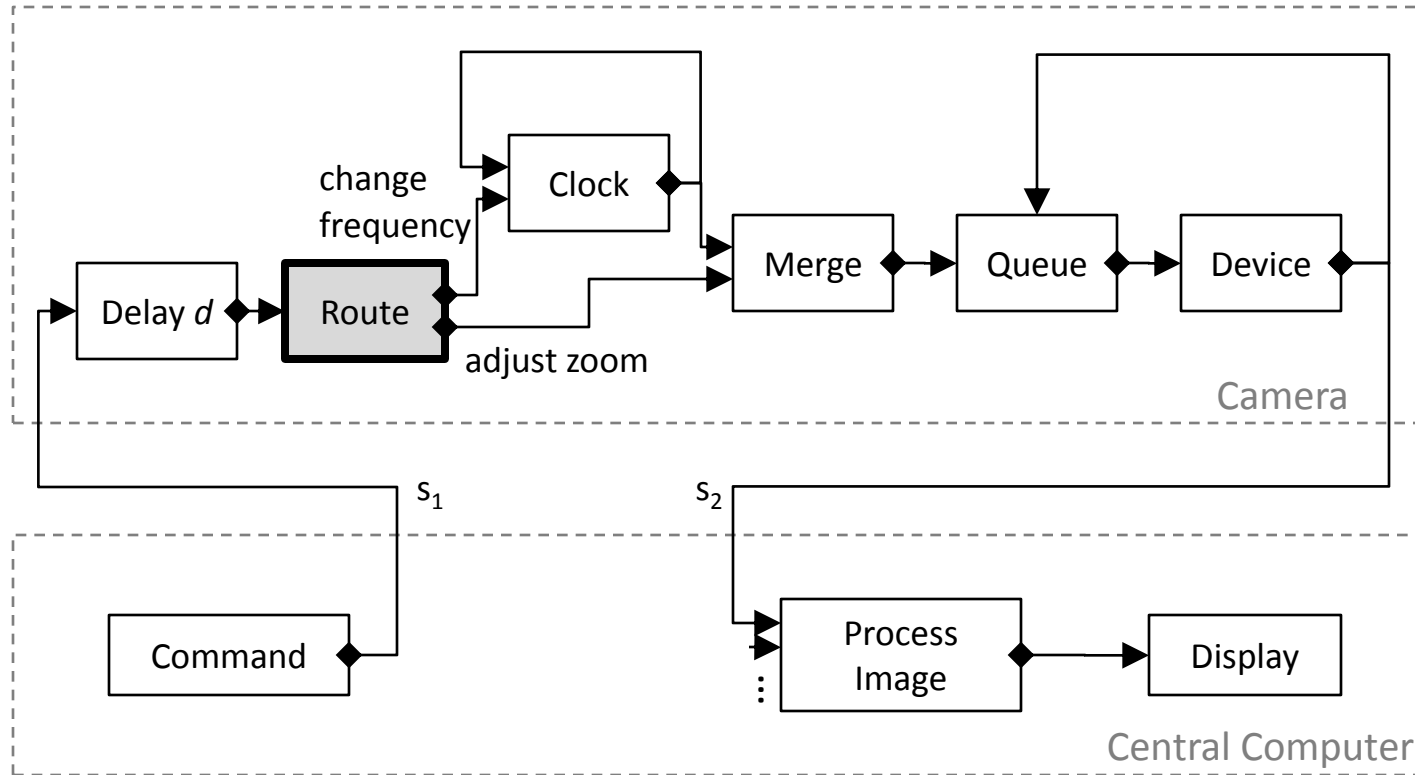
- Wraps interaction with UI device
- Sends event with current time stamp for each user input to all cameras

# Specification of the networked camera application



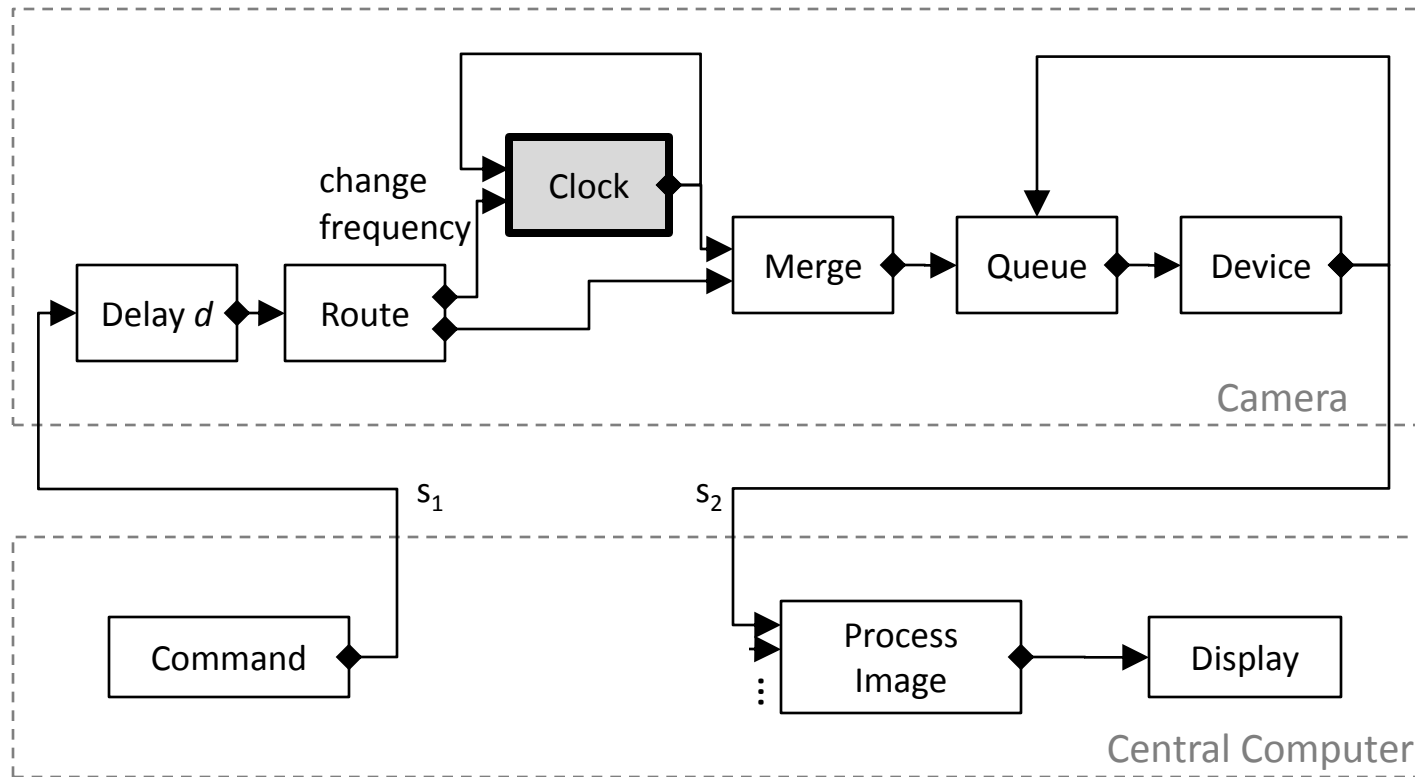
Produce event with timestamp  $t + d$  for event with time stamp  $t$

# Specification of the networked camera application



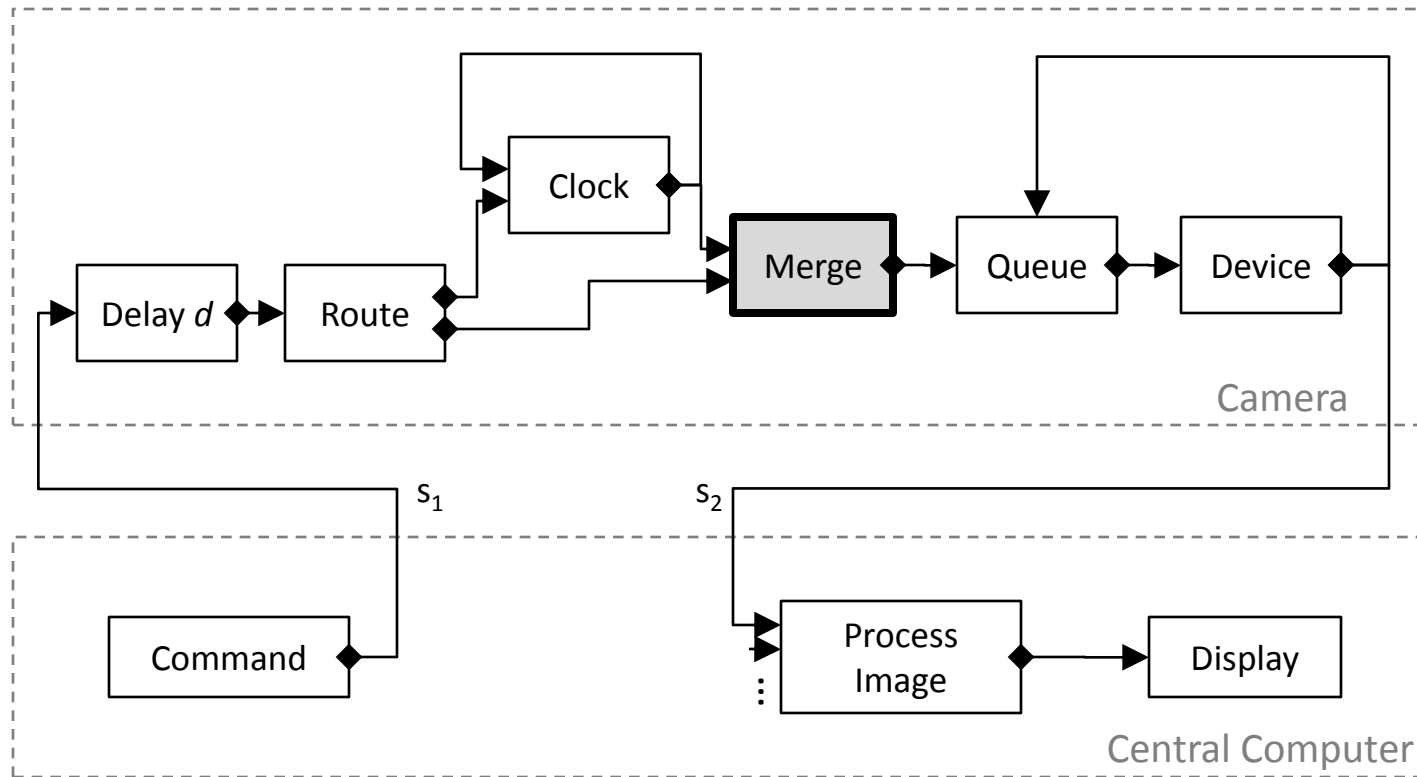
Separates commands

# Specification of the networked camera application



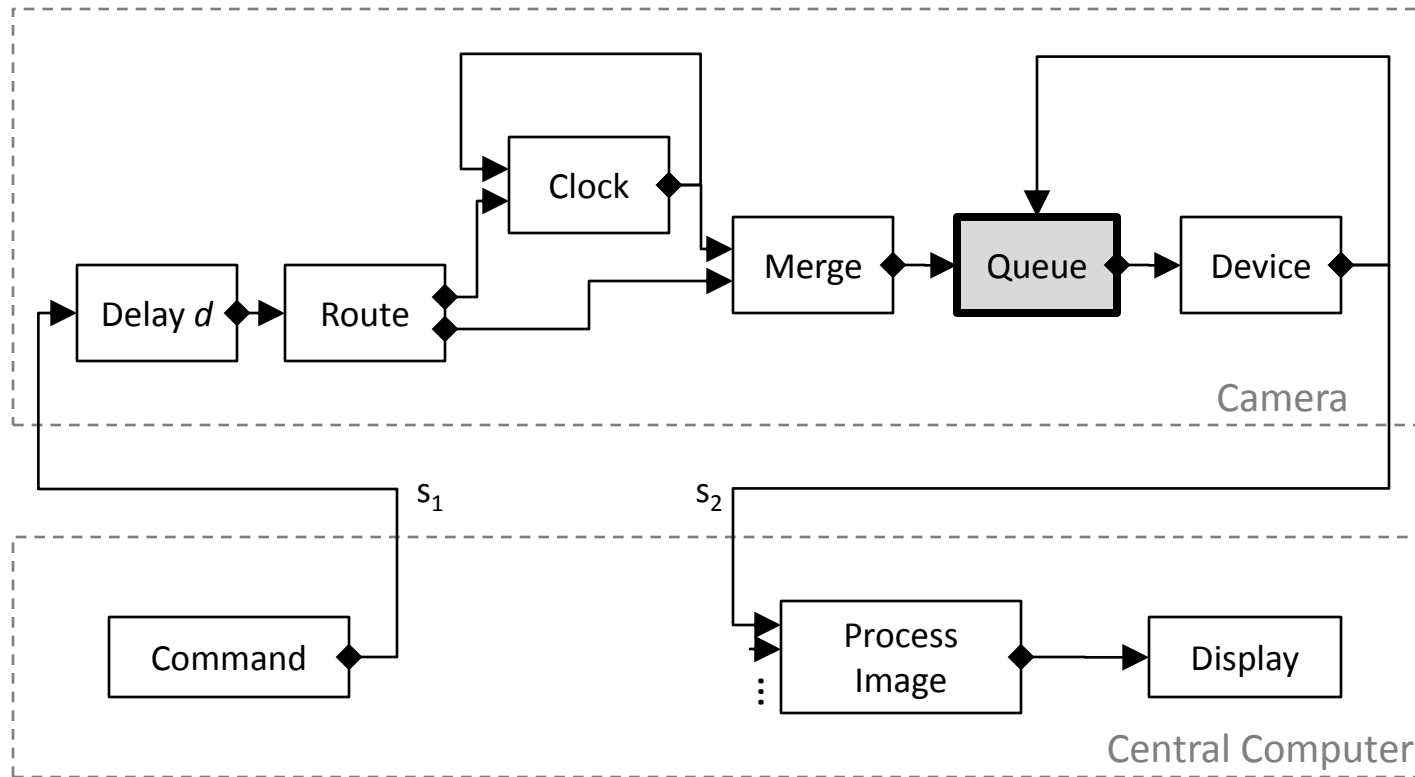
Control picture taking of camera by producing time-stamped outputs  
Change frequency on user request

# Specification of the networked camera application



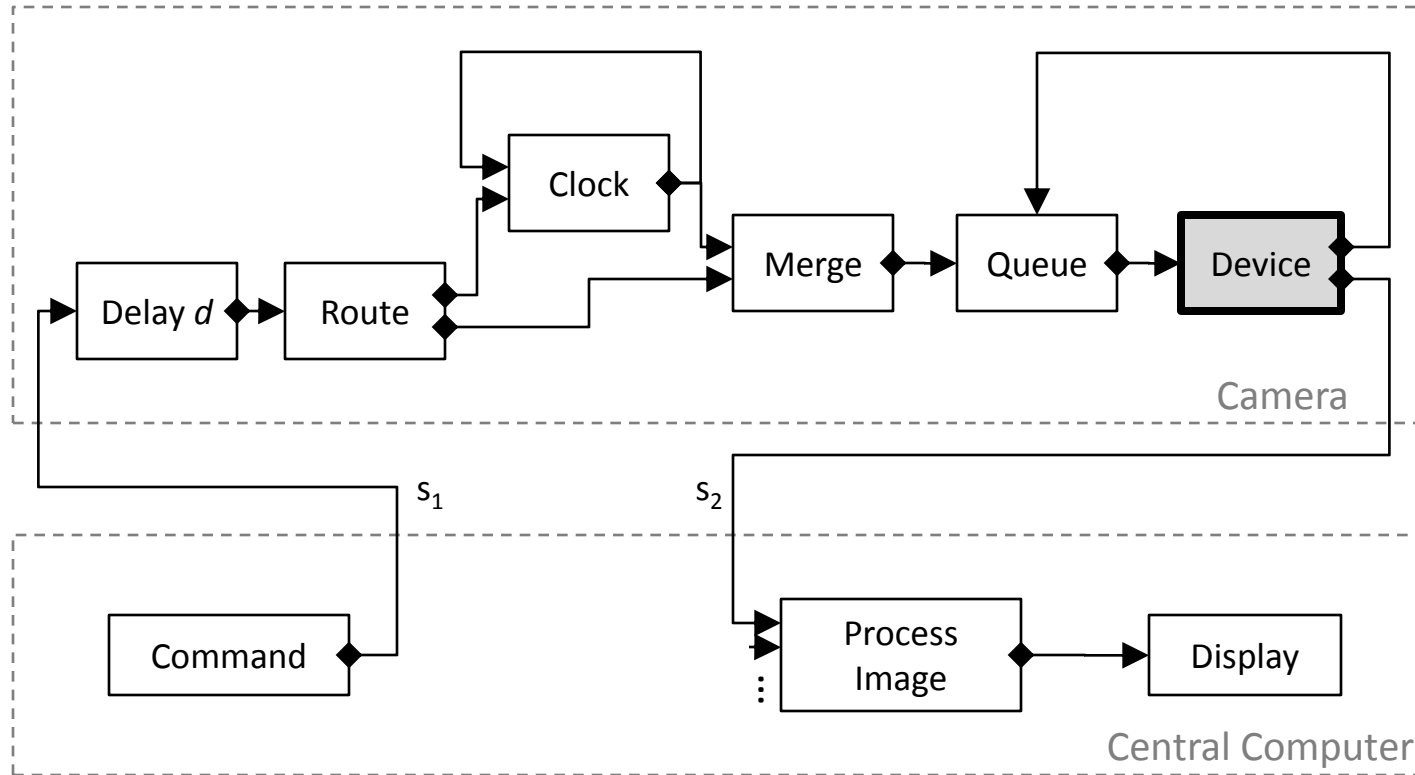
Merge events with priority for second input (to give user control)

# Specification of the networked camera application



Buffers events until device is ready

# Specification of the networked camera application

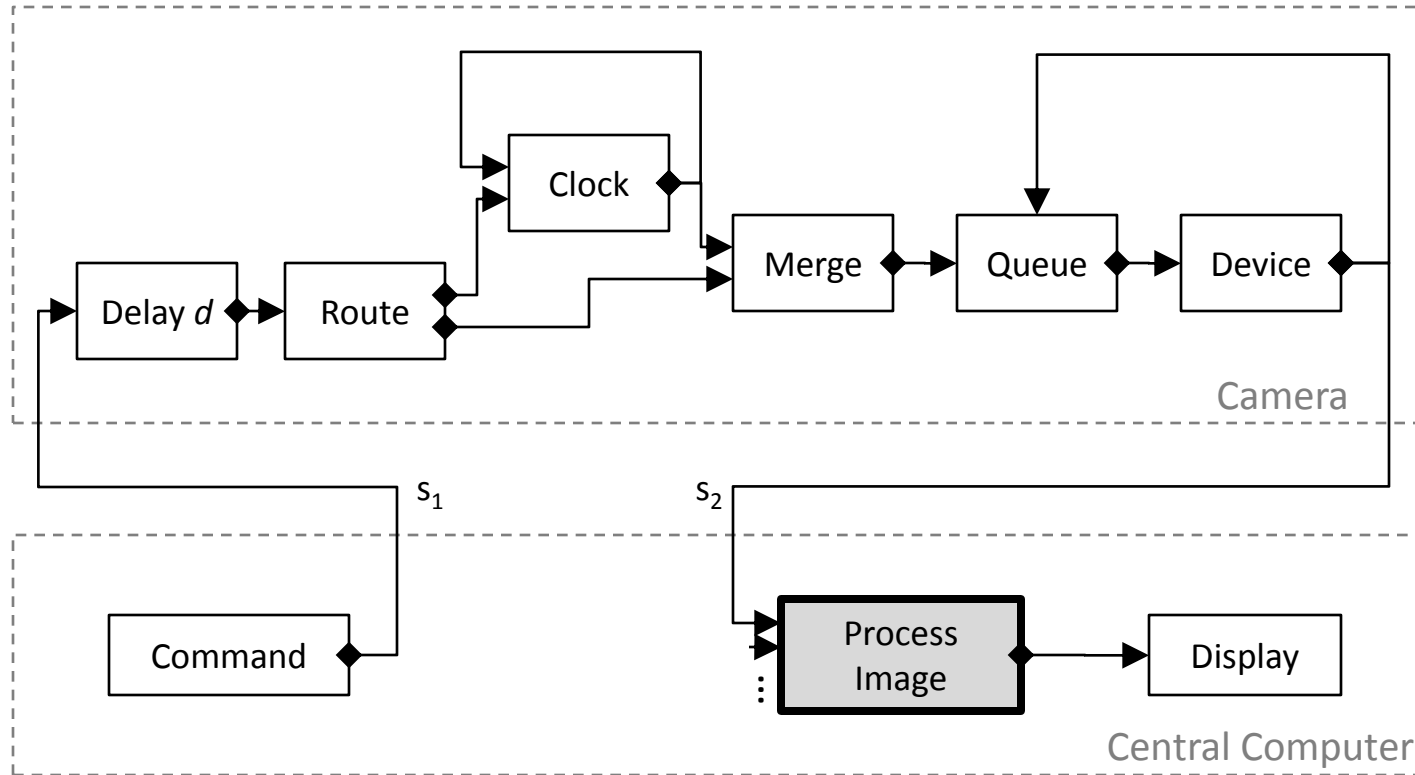


Wraps interaction with camera driver

1<sup>st</sup> output: value for each input event, time stamp  $> t$  (indicate physical action complete)

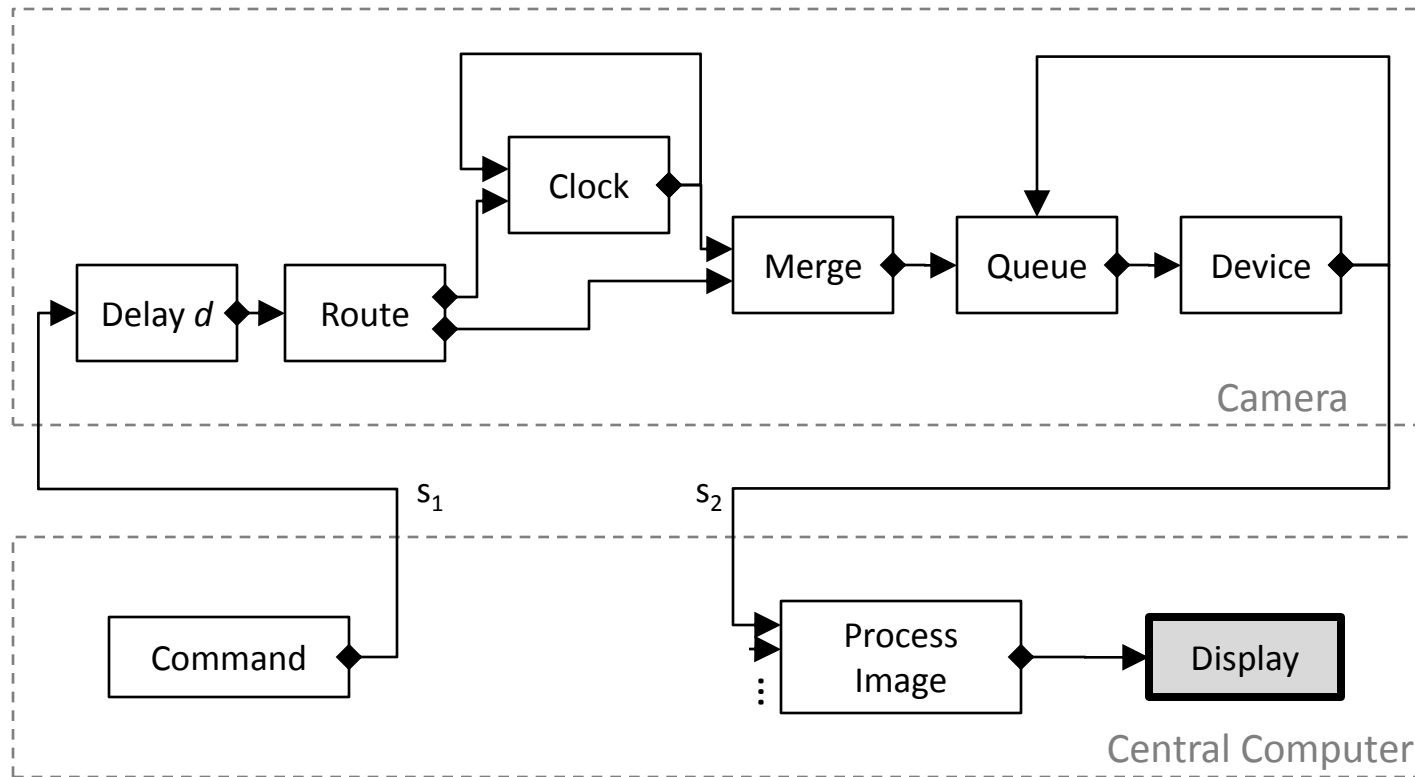
2<sup>nd</sup> output: time-stamped image

# Specification of the networked camera application





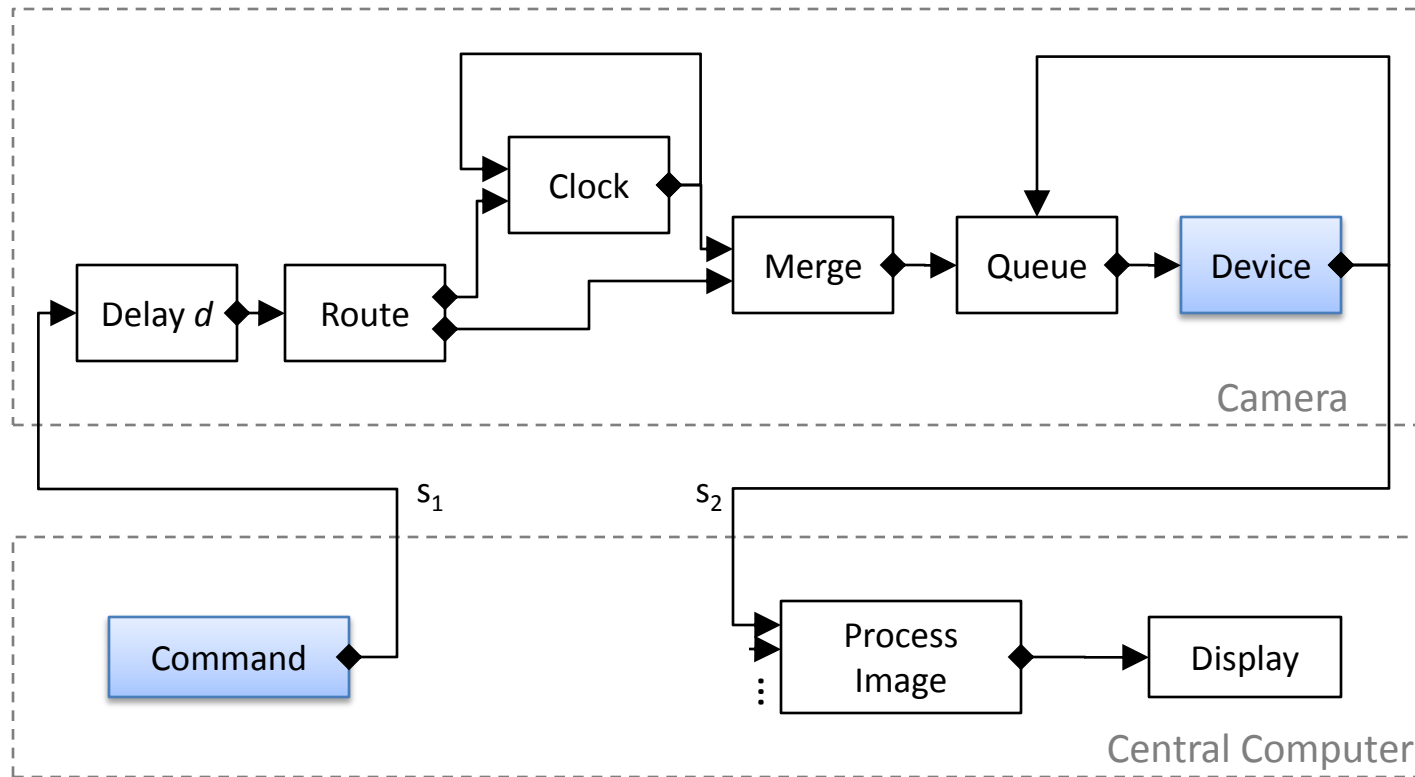
# Specification of the networked camera application



# Specification of the networked camera application

React to an **input** event with time stamp  $t$  if physical time  $\tau \leq t$

Produce an **output** event with time stamp  $t'$  at physical time  $\tau' \geq t'$



setup time  $\sigma$  for real-time ports, react if  $\tau \leq t - \sigma$

# Challenge

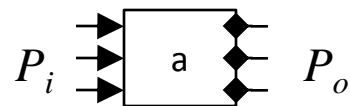
- First-come-first-serve strategy cannot be used
  - no deterministic DE semantics since network may alter order of events
- Brute-force implementation of a conservative technique might stall execution in the camera
- Out of order release of events
  - without losing determinism
  - without requiring backtracking
- Only process events in time-stamp order when they are causally related
- PTIDES (Programming Time-Integrated Distributed Embedded Systems):
  - Discrete-event semantics
  - Carefully chosen relations between model time and real time
  - Determinacy is preserved at runtime.
  - Does not depend on domain specific network architectures

# Causality Interface

## Causality relations among events:

- dependency that output events have on input events
- statically analyzed

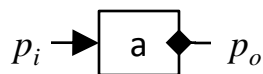
## Causality Interface:



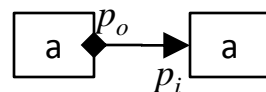
$$\delta_a: P_i \times P_o \longrightarrow D$$

- $D$  is an ordered set (algebra) with two binary operations for composition
  - $\oplus$ (=parallel; minimum)
  - $\otimes$ (= serial; addition)
- Elements of  $D$  are called **dependencies**  $\delta_a(p_1, p_2)$  ... dependency that port  $p_2$  has on  $p_1$
- minimum model-time delay between input events at  $p_1$  and resulting output events at  $p_2$
- Create dependency graph

$$\delta(p_i, p_o) < \infty$$



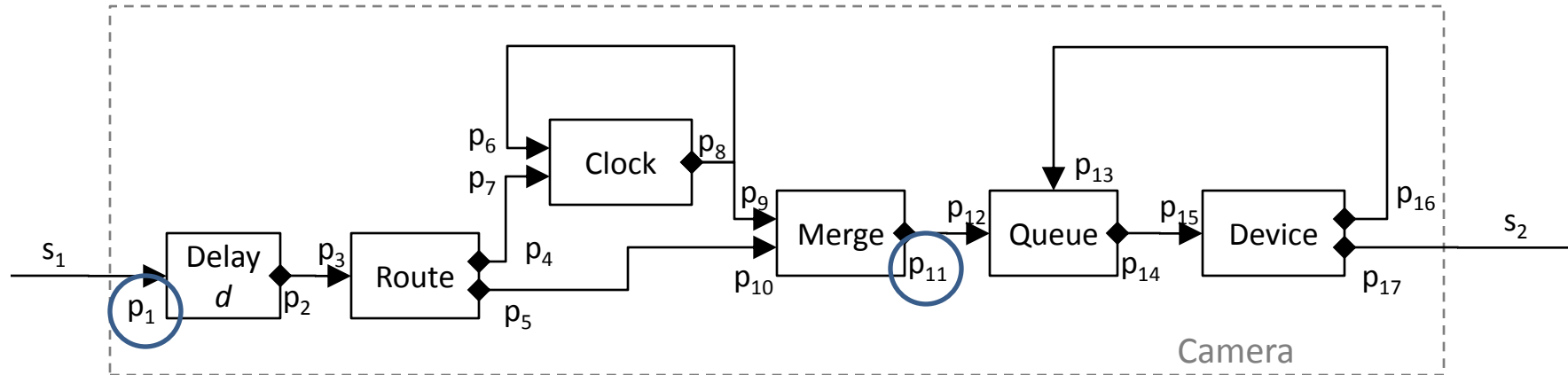
$$\delta(p_o, p_i) = 0$$



$$\text{else: } \delta(p_1, p_2) = \infty$$

$p_1$     ???     $p_2$

# Dependencies



Composition via  $\otimes$  and  $\oplus$

$\otimes$  ... serial, addition

$\oplus$  ... parallel, min

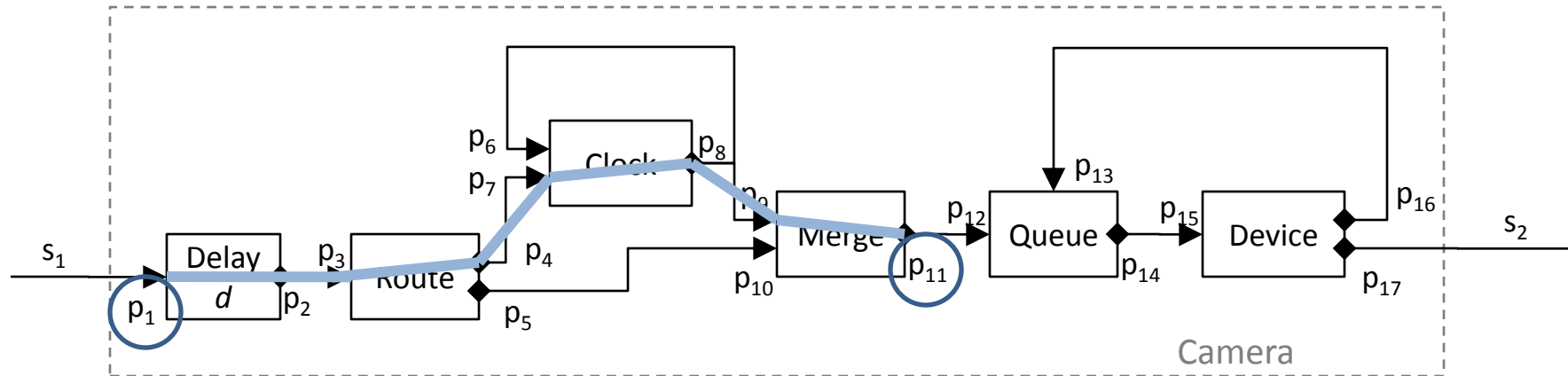
$\delta(p_1, p_{11}) = \min(ph_1, ph_2, ph_3)$  where

$$ph_1 = \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_4) + 0 + \delta_{Clock}(p_7, p_8) + 0 + \delta_{Merge}(p_9, p_{11}),$$

$$ph_2 = \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_5) + 0 + \delta_{Merge}(p_{10}, p_{11}),$$

$$ph_3 = \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_4) + 0 + \delta_{Clock}(p_7, p_8) + 0 + \delta_{Clock}(p_6, p_8) + 0 + \delta_{Merge}(p_9, p_{11})$$

# Dependencies



Composition via  $\otimes$  and  $\oplus$

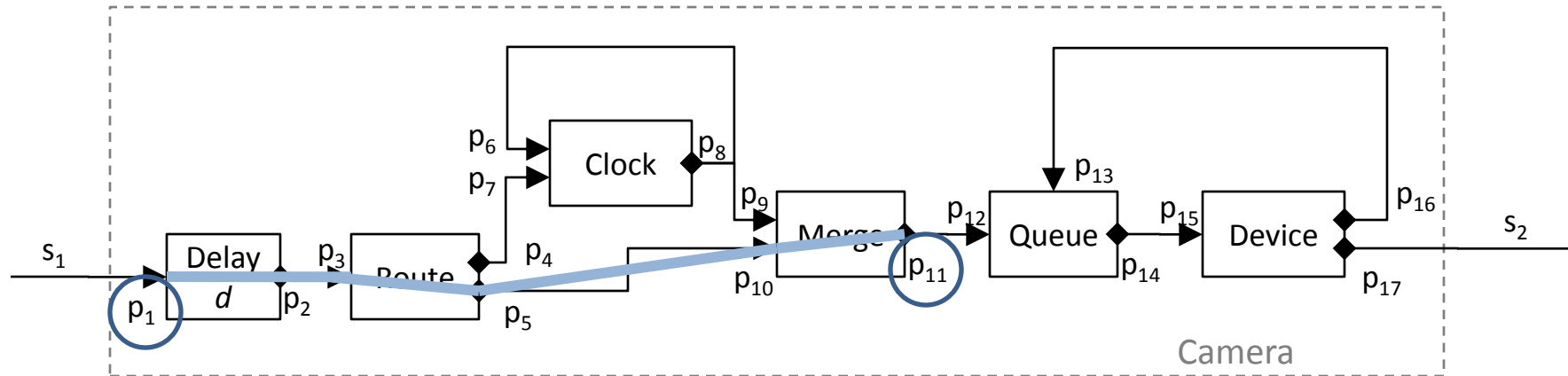
$\otimes$  ... serial, addition

$\oplus$  ... parallel, min

$\delta(p_1, p_{11}) = \min(ph_1, ph_2, ph_3)$  where

$$\begin{aligned} \Rightarrow ph_1 &= \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_4) + 0 + \delta_{Clock}(p_7, p_8) + 0 + \delta_{Merge}(p_9, p_{11}), \\ ph_2 &= \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_5) + 0 + \delta_{Merge}(p_{10}, p_{11}), \\ ph_3 &= \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_4) + 0 + \delta_{Clock}(p_7, p_8) + 0 + \delta_{Clock}(p_6, p_8) + \\ &\quad 0 + \delta_{Merge}(p_9, p_{11}) \end{aligned}$$

# Dependencies



Composition via  $\otimes$  and  $\oplus$

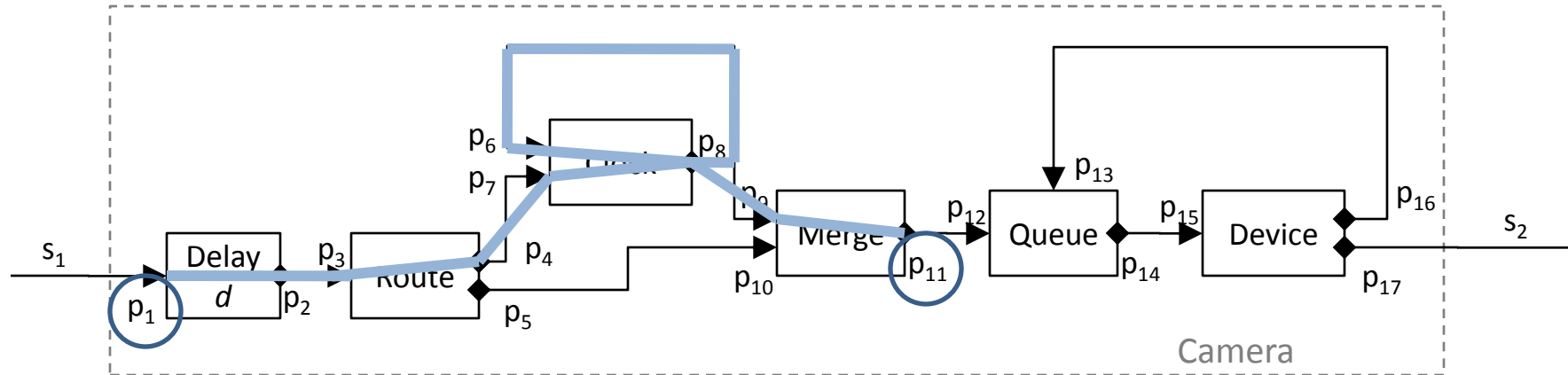
$\otimes$  ... serial, addition

$\oplus$  ... parallel, min

$\delta(p_1, p_{11}) = \min(ph_1, ph_2, ph_3)$  where

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# Dependencies



Composition via  $\otimes$  and  $\oplus$

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$\delta(p_1, p_{11}) = \min(ph_1, ph_2, ph_3)$  where

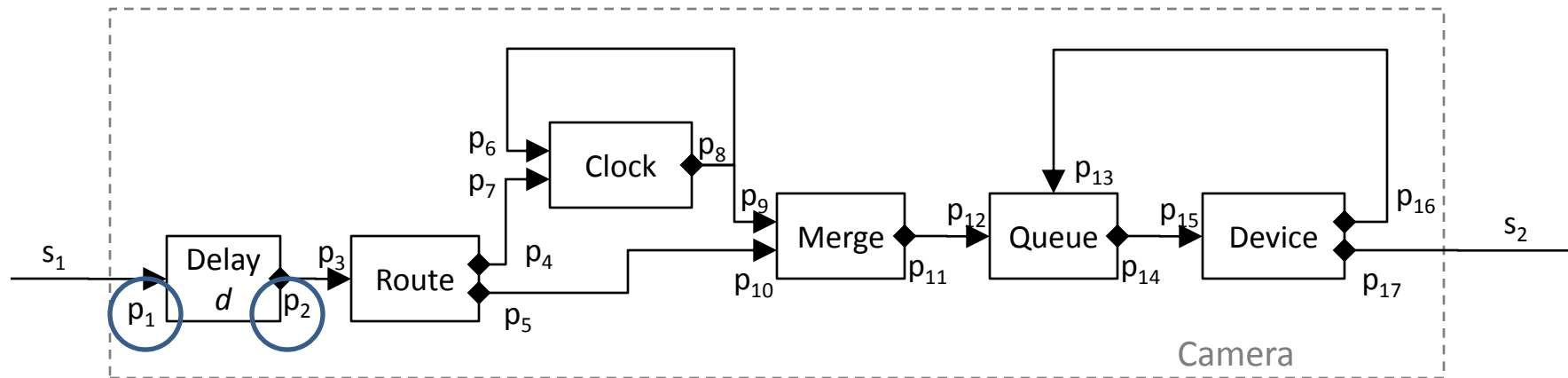
$$ph_1 = \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_4) + 0 + \delta_{Clock}(p_7, p_8) + 0 + \delta_{Merge}(p_9, p_{11}),$$

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$$\rightarrow ph_3 = \delta_{Delay}(p_1, p_2) + 0 + \delta_{Router}(p_3, p_4) + 0 + \delta_{Clock}(p_7, p_8) + 0 + \delta_{Clock}(p_6, p_8) + 0 + \delta_{Merge}(p_9, p_{11})$$

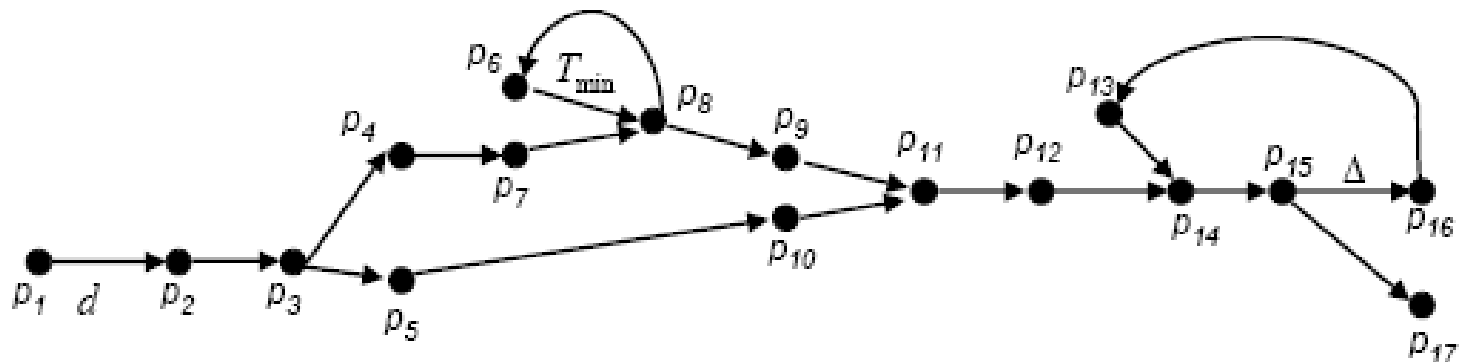


# Dependencies



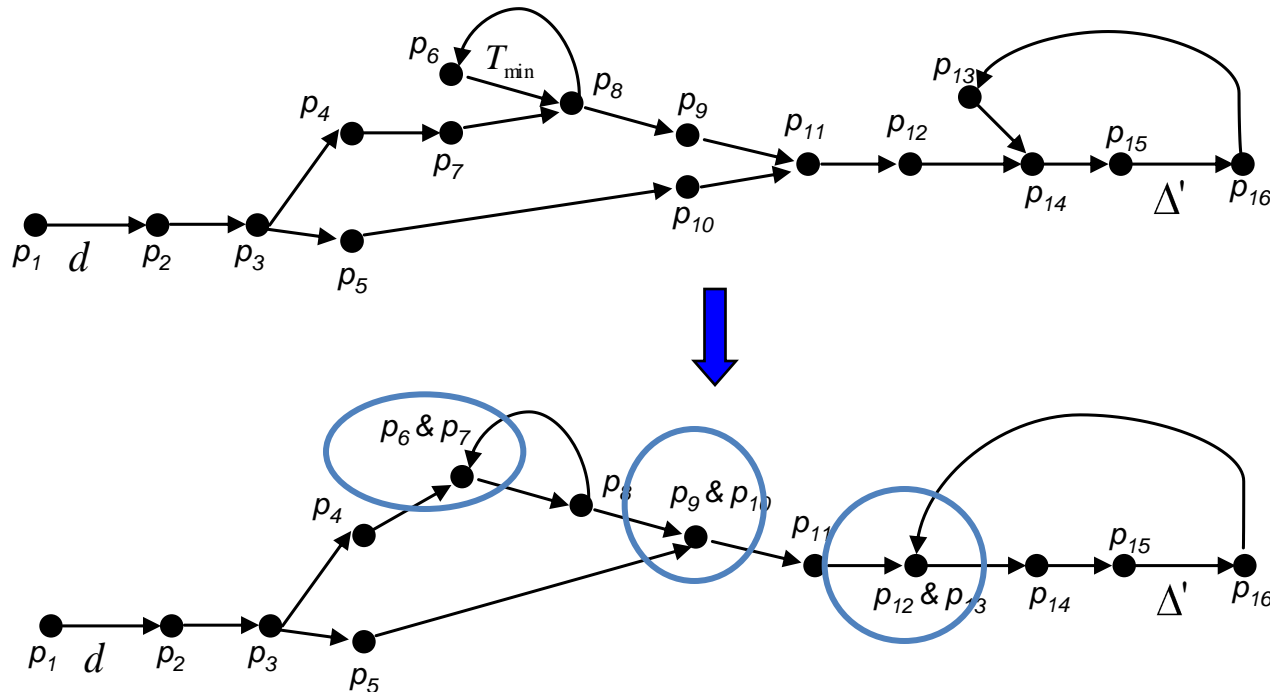
Dependency graph:

$\delta(p_1, p_2) = d$  means any event with time stamp  $t$  at  $p_2$  can be processed when all events at  $p_1$  are known up to time stamp  $t - d$



# Dependencies

- If an event at  $p_1$  will affect an output signal that may also depend on an event at  $p_2$ ,  $p_1$  and  $p_2$  are equivalent.
- $\exists_p \in P_o$ , such that  $\delta(p_1, p) < \infty$  and  $\delta(p_2, p) < \infty$

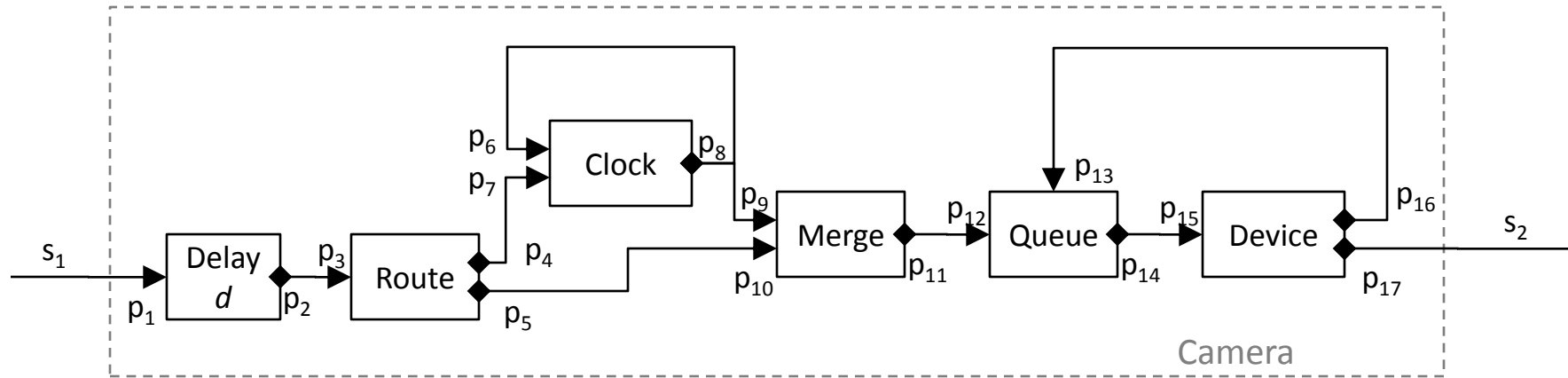


# Relevant Dependency

$$d: Q \times Q \longrightarrow D$$

- $Q$  ... set of equivalence classes of input ports in a composition
- Examine weights of relevant dependency graph
- Indicates how much we can advance time at a port without knowing all events on the other ports in a composition

# Relevant Dependency



## Causality Interface of each actor:

$$\delta_{Delay}(p_1, p_2) = d,$$

$$\delta_{Router}(p_3, p_4) = 0, \quad \delta_{Router}(p_3, p_5) = 0,$$

$$\delta_{Clock}(p_6, p_8) = T_{min}, \quad \delta_{Clock}(p_7, p_8) = 0,$$

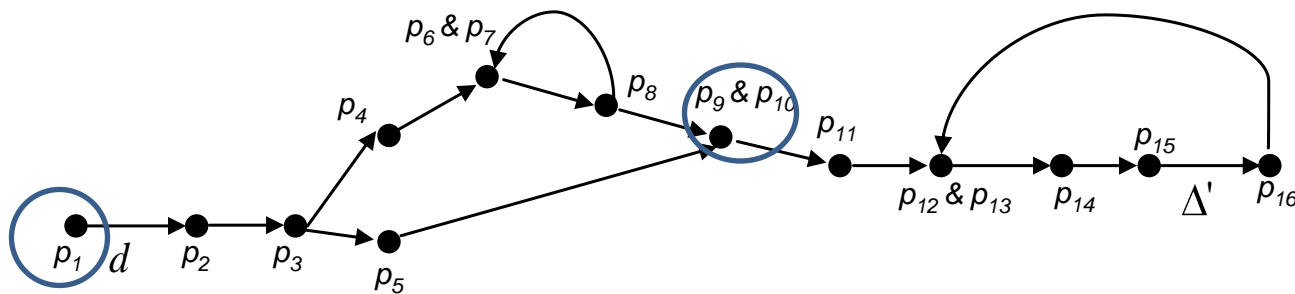
$$\delta_{Merge}(p_9, p_{11}) = 0, \quad \delta_{Merge}(p_{10}, p_{11}) = 0,$$

$$\delta_{Queue}(p_{12}, p_{14}) = 0, \quad \delta_{Queue}(p_{13}, p_{14}) = 0,$$

$$\delta_{Device}(p_{15}, p_{16}) = \Delta, \quad \delta_{Device}(p_{15}, p_{17}) = 0$$

# Relevant Dependency

- E.g.  $d(p_1, p_{9,10})$



any event with time stamp  $t$  at port  $p_9$  can be processed when all events at port  $p_1$  are known up to time stamp  $t - d$

# Relevant Order

## Partial order on events

$e_1$  event with time stamp  $t_1$  at port in  $q_1$

$e_2$  event with time stamp  $t_2$  at port in  $q_2$

$$e_1 <_r e_2 \Leftrightarrow t_1 + d(q_1, q_2) < t_2$$

$<_r$  ... relevant order

If neither  $e_1 <_r e_2$  nor  $e_2 <_r e_1$  then  $e_1 \parallel_r e_2$

# Execution Strategy

... based on relevant order

1. Start with  $E$ , a set of events in the event queue.
2. Choose  $r \subset E$  so that each event in  $r$  is *minimal* in  $E$ .  
( $e$  is minimal when  $\forall e' \in E, e <_r e'$  or  $e \parallel_r e'$ )
3. Process events in  $r$ , which may produce a set of new events  $E'$ .
4. Update  $E$  to  $(E \setminus r) \cup E'$ .
5. Go to 2.

# Execution Strategy

... based on relevant order

1. Start with  $E$ , a set of events in the event queue.
2. Choose  $r \subset E$  so that each event in  $r$  is *minimal* in  $E$  and **we have seen all events that are less than events in  $r$  in the relevant order.**
3. Process events in  $r$ , which may produce a set of new events  $E'$ .
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Consider:

- network delay: network ports receive events from other computers or external I/O



# Execution Strategy

... based on relevant order

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3. Process events in  $r$ , which may produce a set of new events  $E'$ .
4. Update  $E$  to  $(E \setminus r) \cup E'$ .
5. Go to 2.

Consider:

- network delay: network ports receive events from other computers or external I/O
- synchronization errors on the clocks
  - Wait for the physical time to be the estimated phys time + error

# Conclusion

- Key requirement in a PTIDES program for preserving runtime determinism:  
*each event  $e$  with model time  $t$  at a real-time port must be received before the physical time exceeds  $t - \sigma$ , where  $\sigma$  is the setup time of the real-time port.*
- A PTIDES program is deployable if this requirement can be guaranteed.